

# The Cosmic Ray Spectrum above $10^{17}$ eV Measured by the Telescope Array and TALE Fluorescence Telescopes

JiHee KIM  
PhD defense  
2018/09/21



# OUTLINE

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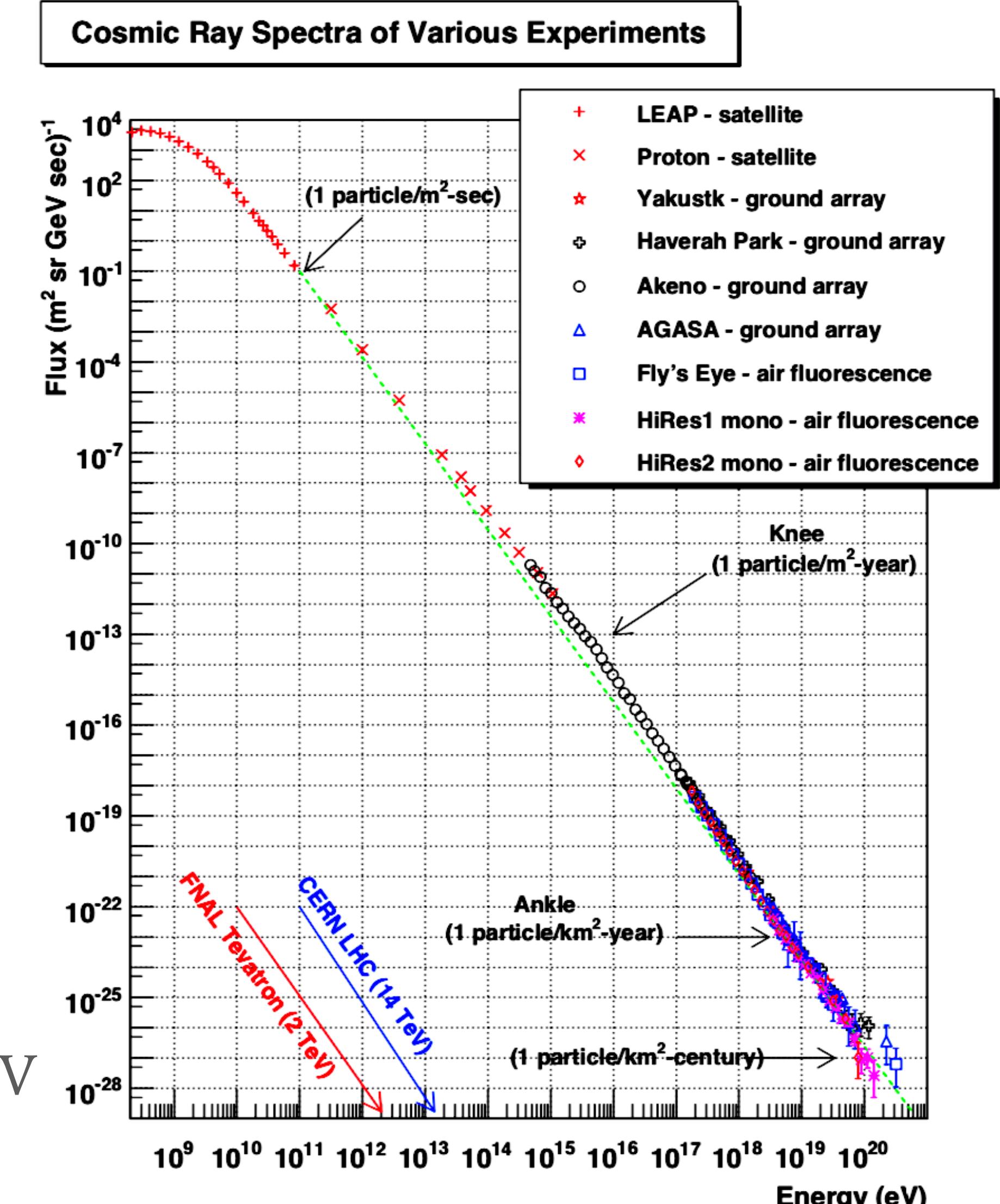
- Introduction - Cosmic Rays
- Telescope Array and TALE Experiments
- Extensive Air Shower
- Monte Carlo Simulation
- Event Reconstruction
- Data/MC Comparison
- Energy Spectrum Measurement
- Conclusions (take-home message)

# INTRODUCTION - COSMIC RAYS

- Cosmic rays : Energetic particles accelerated by astrophysical sources.



- Solar cosmic rays below  $\sim$  a few  $10^9$  eV
- Galactic cosmic rays below  $\sim 10^{17}$  eV, extragalactic cosmic rays above
- Ultra-High Energy Cosmic Rays (UHECRs) above  $10^{18}$  eV
  - In 1991, Fly's Eye Experiment observed  $3.2 \times 10^{20}$  eV
  - At present, Large Hadron Collider (LHC) reaches  $1.3 \times 10^{13}$  eV



# INTRODUCTION - COSMIC RAY MEASUREMENTS

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There are three main topics of cosmic ray research:

➤ **Cosmic Ray Energy Spectrum**

- Flux follows a simple power law :  $\text{Flux}(E) \sim E^{-\gamma}$ ,  $\gamma$  is spectral index
- Spectral features where spectral indices change

➤ **Cosmic Ray Composition**

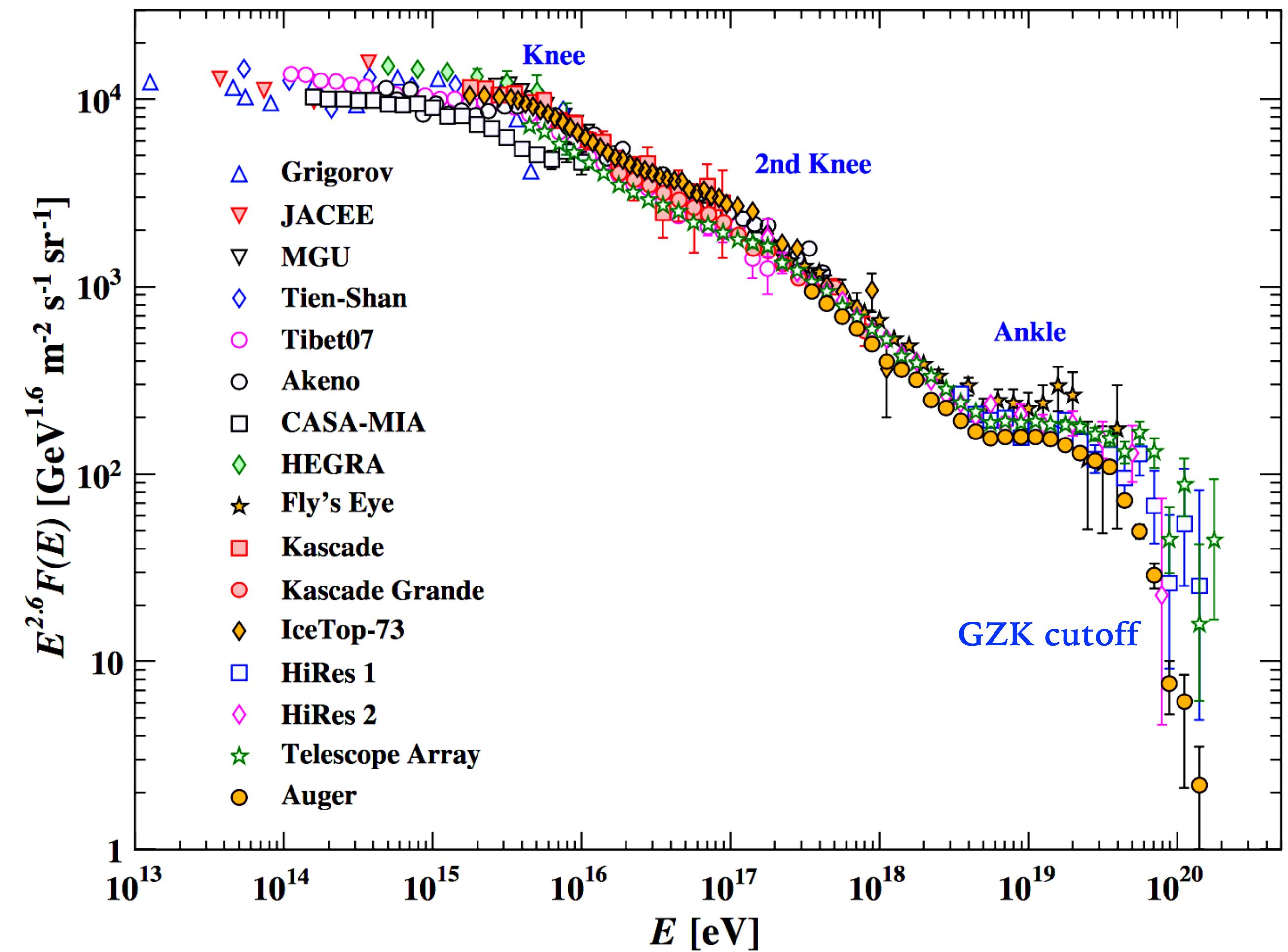
- Chemical composition of cosmic rays: nuclei type

➤ **Cosmic Ray Sources**

- Arrival direction of cosmic rays and correlation with possible sources

# INTRODUCTION - COSMIC RAY ENERGY SPECTRUM

- Near  $E \sim 10^{15.6}$  eV, “Knee”  
 $\gamma$  changes from 2.7 to 3.0
- Near  $E \sim 10^{16.2}$  eV, “Dip”
- Above  $10^{17}$  eV,  
“2nd Knee” or “Iron Knee”
- At  $E \sim 10^{18.7}$  eV, “Ankle”  
becomes less steep
- At  $E \sim 10^{19.8}$  eV, “GZK cutoff”  
flux drops dramatically



# INTRODUCTION - COSMIC RAY ENERGY SPECTRUM

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- “Knee”,  $E \sim 10^{15.6}$  eV
  - Associated with galactic sources: Supernova Remnants (SNRs); shock fronts
  - Maximum energy of galactic cosmic ray protons
  - Acceleration through magnetic fields, rigidity dependent

$$E_{\max}(Z) = Ze \times R_c = Z \times E_{p \max}, \quad \text{where } R_c = E/Ze$$

- Rigidity-dependent effect: heavy charged nuclei can achieve  $Z$  times higher energy than a proton when accelerated in a magnetic field

- “2nd Knee” or “Iron Knee”,  $E \sim 10^{17.1}$  eV
  - $10^{17}$  decade in energy region may be a transition from galactic cosmic rays to extragalactic cosmic rays (heavy nuclei to light nuclei)

# INTRODUCTION - COSMIC RAY ENERGY SPECTRUM

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- “Ankle”,  $E \sim 10^{18.7}$  eV
  - Dip in the flux of cosmic ray particles; origin not yet fully resolved
    1. Pair production from ultra-high energy protons :  $p + \gamma_{\text{CMB}} \rightarrow p + e^- + e^+$
    2. Galactic/extragalactic transition
    3. Rigidity-dependent cycle
- “GZK cutoff”,  $E \sim 10^{19.8}$  eV
  - Theoretical upper limit on energy of cosmic rays coming from sources:  $5-6 \times 10^{19}$  eV
  - Cosmic rays traveling over distances  $> 50$  Mpc likely collide and form  $\Delta$  resonance
$$p + \gamma_{\text{CMB}} \rightarrow \Delta^+ \rightarrow p + \pi^0 \quad \text{or} \quad p + \gamma_{\text{CMB}} \rightarrow \Delta^+ \rightarrow n + \pi^+$$

# INTRODUCTION - COSMIC RAY MEASUREMENTS

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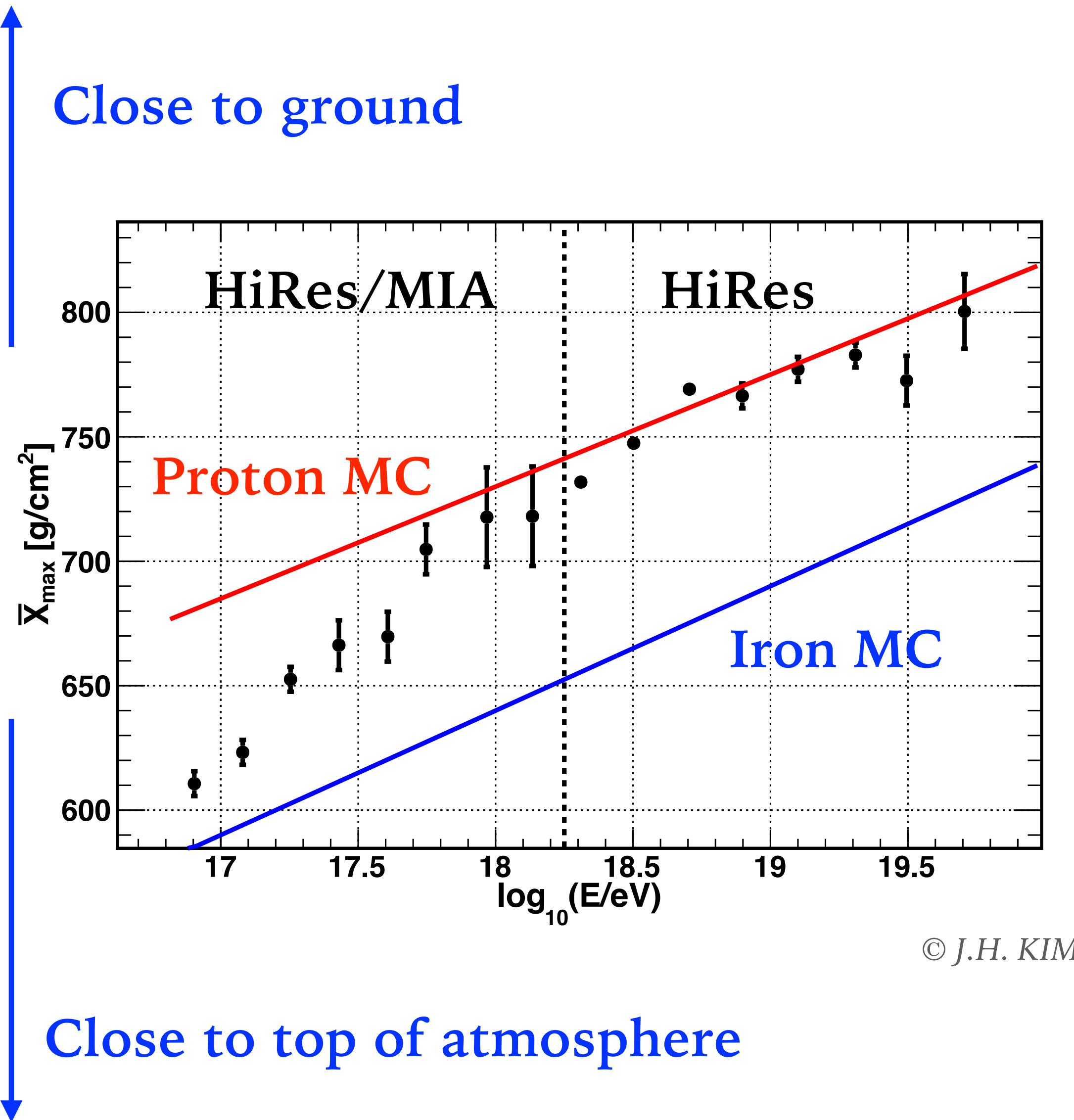
➤ **Cosmic Ray Composition**

- Chemical composition of cosmic rays: nuclei type

➤ **Cosmic Ray Sources**

- Arrival direction of cosmic rays and correlation with possible sources

# INTRODUCTION - COSMIC RAY COMPOSITION



- Study depth of shower max,  $X_{\max}$ , maximum number of charged particles, in extensive air shower
- Chemical composition determines average characteristics of the shower development
  - Proton penetrates deeper
  - Iron interacts w/ air molecules earlier (superposition of 56 nucleons)
- **Previous composition result will be used for my study**

# INTRODUCTION - COSMIC RAY MEASUREMENTS

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There are three topics of cosmic ray research:

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- Spectral features where spectral indices change

➤ **Cosmic Ray Composition**

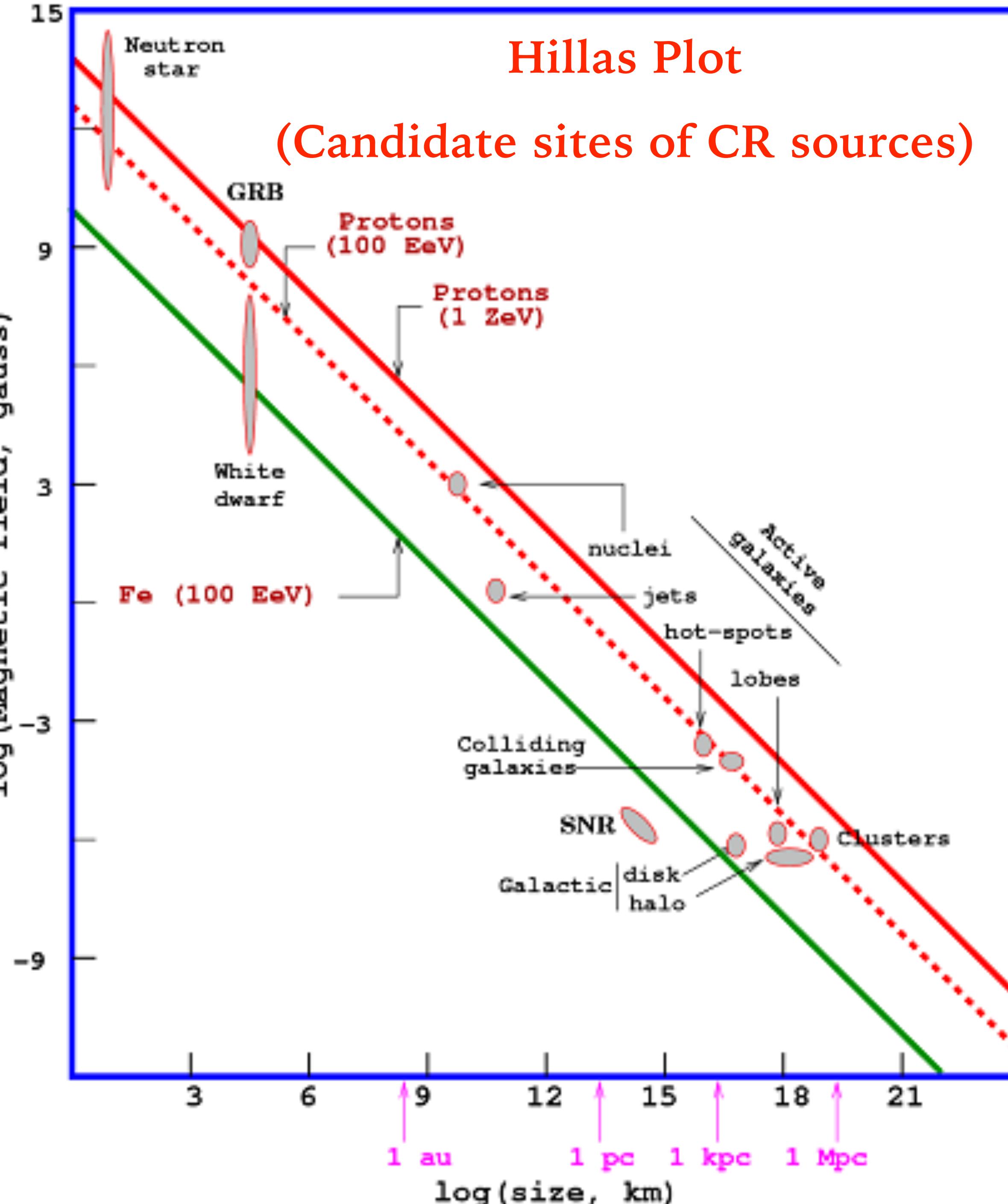
- Chemical composition of cosmic rays: nuclei type

➤ **Cosmic Ray Sources**

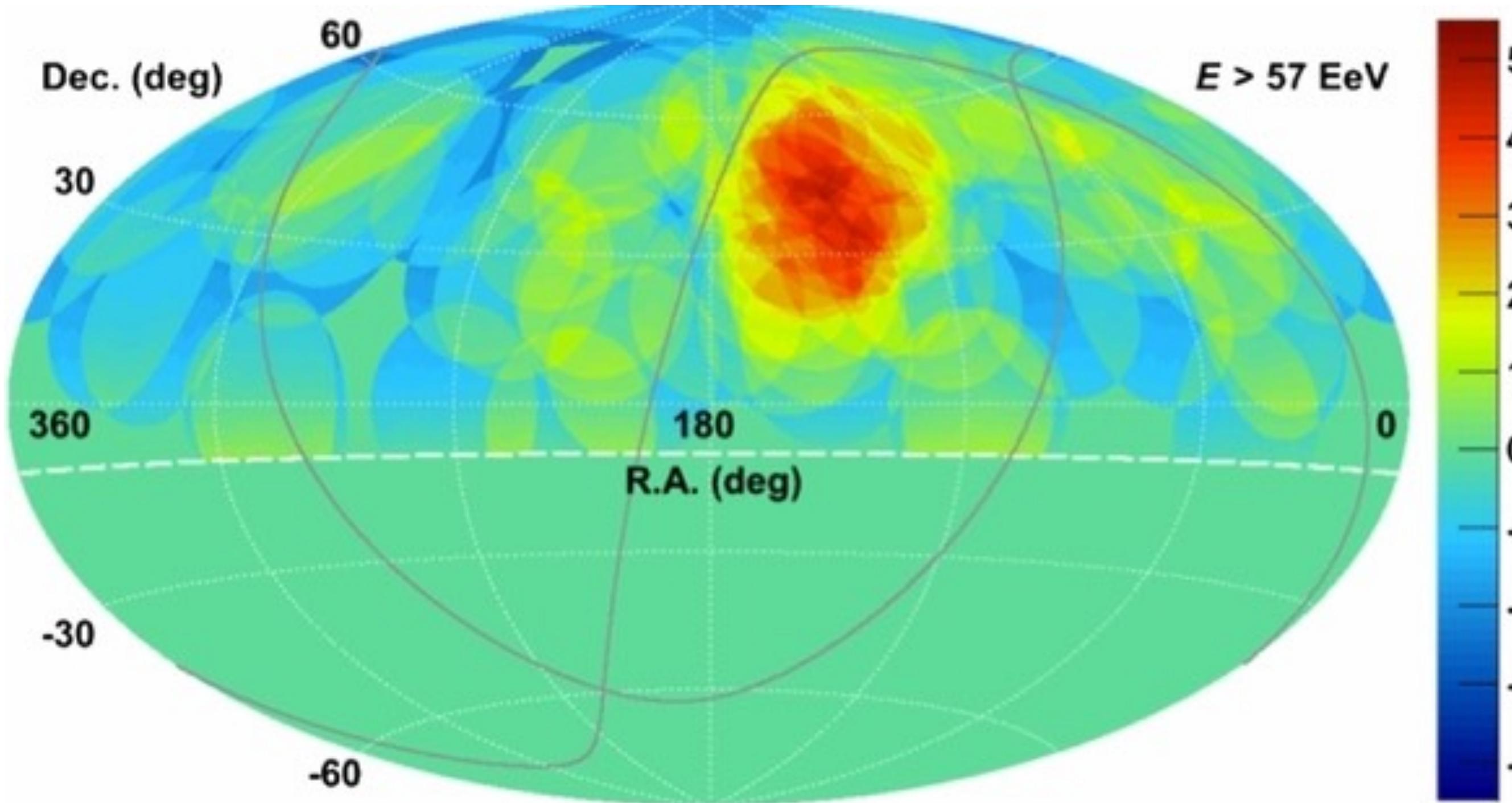
- Arrival direction of cosmic rays and correlation with possible sources

# INTRODUCTION - COSMIC RAY SOURCES

- Ultra-high energy cosmic ray sources remain unknown
- Strong magnetic fields and large size to accelerate particles over longer periods of time required to get to Ultra-high energy
- Possible sources:  
Super Massive Black Hole, Gamma Ray Burst, Star Burst Galaxies, etc



# INTRODUCTION - COSMIC RAY SOURCES



- Energy range :  $10^{18}$  to  $10^{18.5}$
- Isotropic - no excess along the galactic plane
- $E > 5.7 \times 10^{19}$  eV, The HotSpot
  - A local cluster of high energy events (26% of events fall in 6% of visible sky)
  - Near Ursa Major

# INTRODUCTION - COSMIC RAY ENERGY SPECTRUM IS **FOCUS OF MY DISSERTATION**

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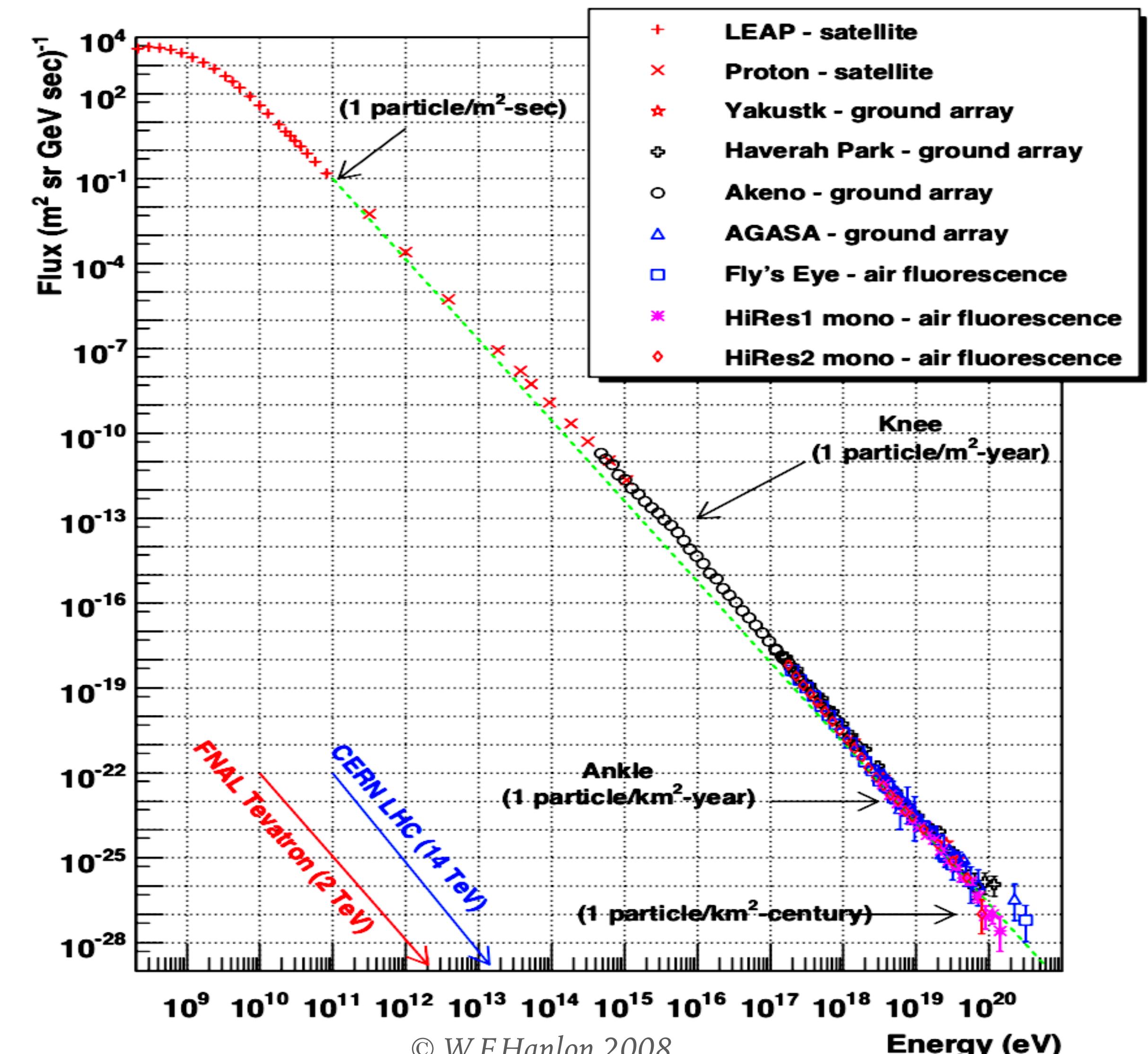
- This analysis focused on particles  $10^{17} < E < 10^{18}$  eV
  - Transition region
  - Heavy galactic component dying off/leaking out
  - Light extragalactic particles starting to leak in to the galaxy
- Technique - 4 ring\* analysis: combined TA MD and TALE telescope data (Optimal)
  - FOV:
    - Elevation : 3- 59°
    - Azimuthal : 115°
  - Observation full shower development

\*ring : a set of telescopes shared the same elevation

# INTRODUCTION - COSMIC RAY ENERGY SPECTRUM

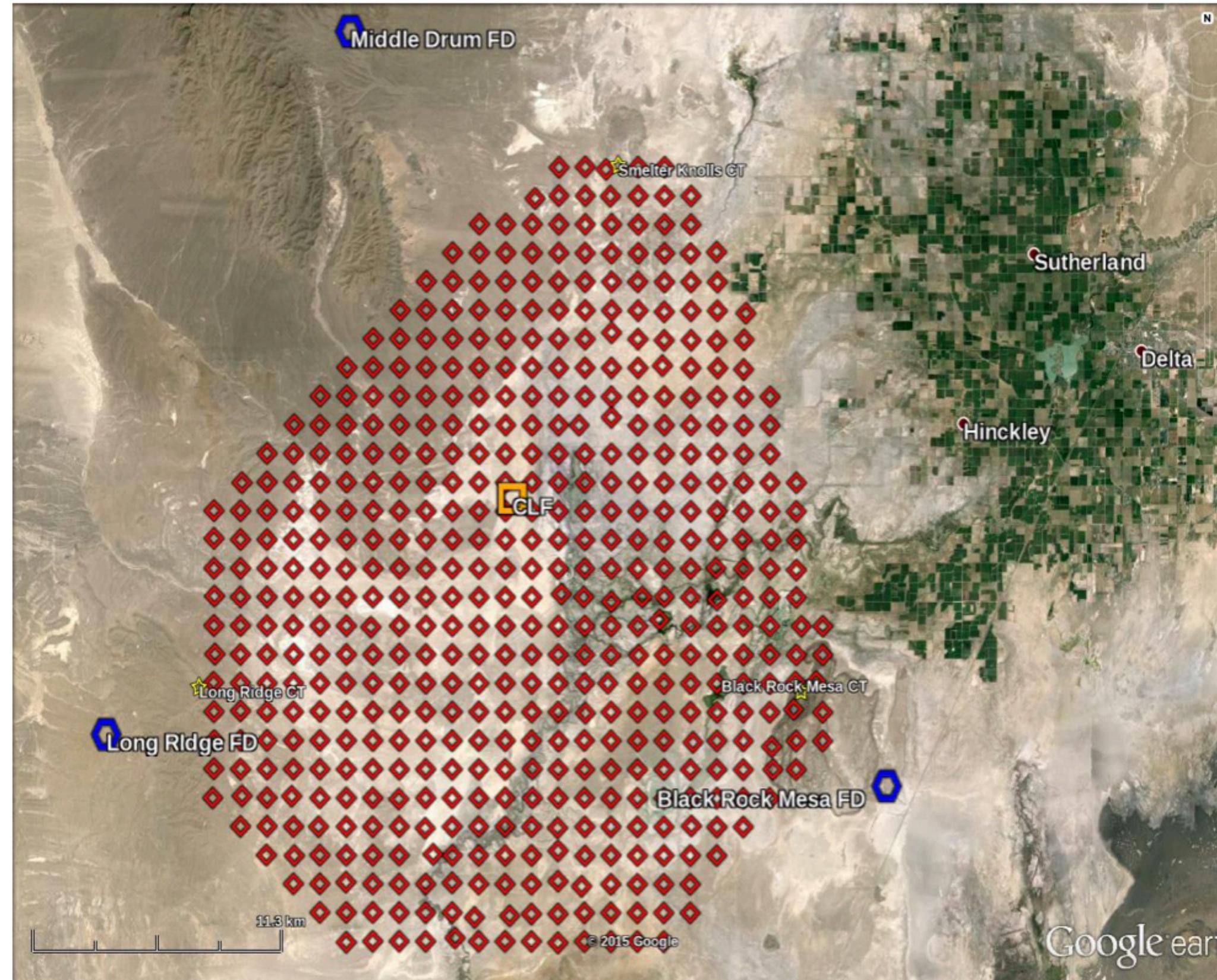
- Steep spectrum
- Near  $E \sim 10^{15.6}$  eV, “Knee”  
*1 particle/m<sup>2</sup>/year*
- At  $E \sim 10^{18.7}$  eV, “Ankle”  
*1 particle/km<sup>2</sup>/year*
- At  $E \sim 10^{19.8}$  eV, “GZK cutoff”  
*1-2 particle(s)/km<sup>2</sup>/century*

**Cosmic Ray Spectra of Various Experiments**



# EXPERIMENT - TELESCOPE ARRAY (TA)

- Telescope Array - Largest cosmic ray observatory in the Northern hemisphere
- West Desert, Millard County, Utah - About 2.5 hrs south of UofU



- International Collaboration: US, Japan, Korea, Russia, Belgium (130 people)
- Observes cosmic rays  $E > 10^{19}$  eV
  - 3 telescope stations (○)
  - overlooking an array of 507 scintillator surface detectors (◇)
  - Central Laser Facility (□) (Atm calib)
  - Area :  $\sim 700 \text{ km}^2$  ( $300 \text{ mi}^2$ )

# EXPERIMENT - TA FLUORESCENCE DETECTOR (FD)

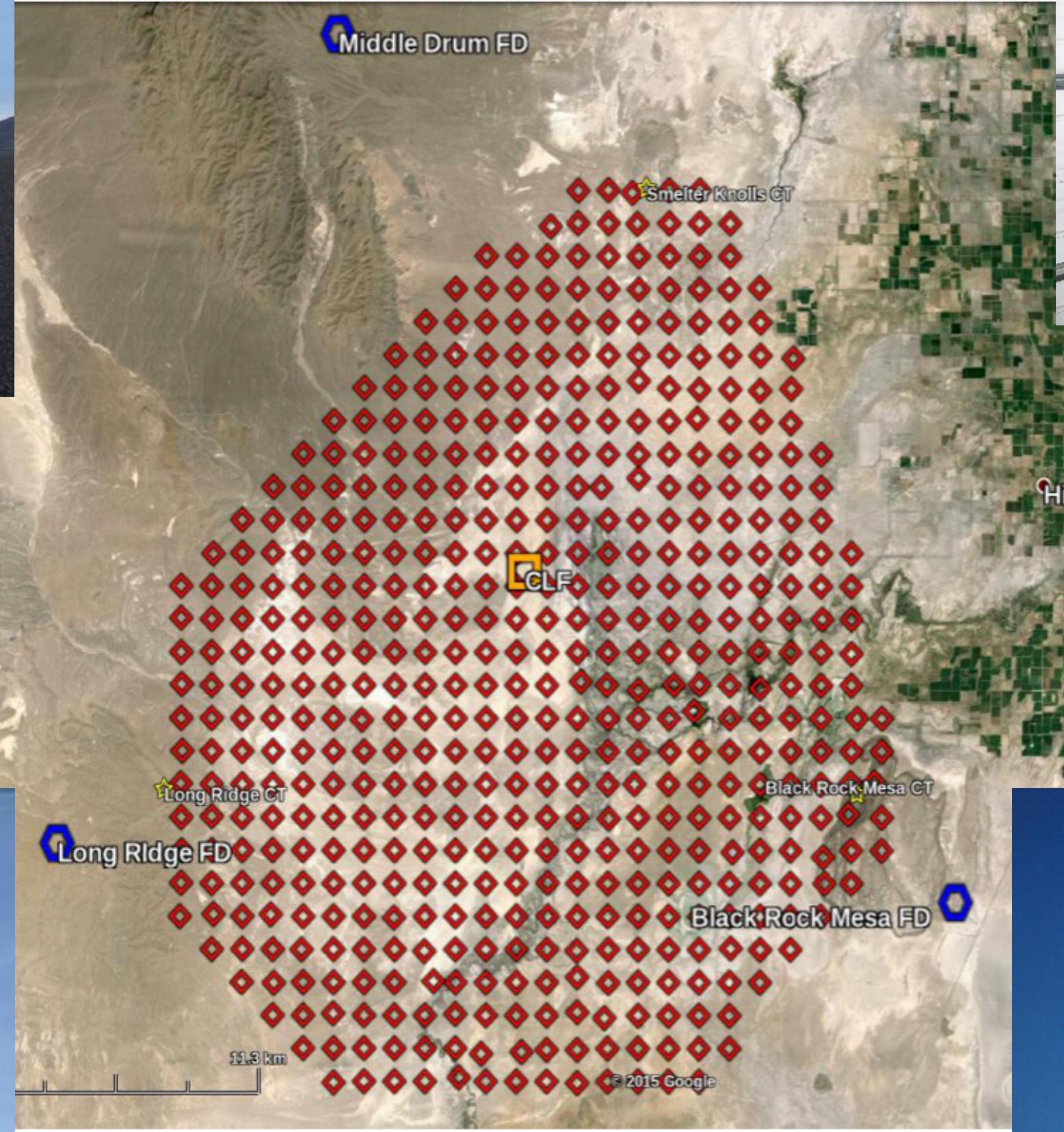


Middle Drum (MDFD)

© J.N.Matthews



Long Ridge (LRFD)



12 telescopes @ station  
new telescopes

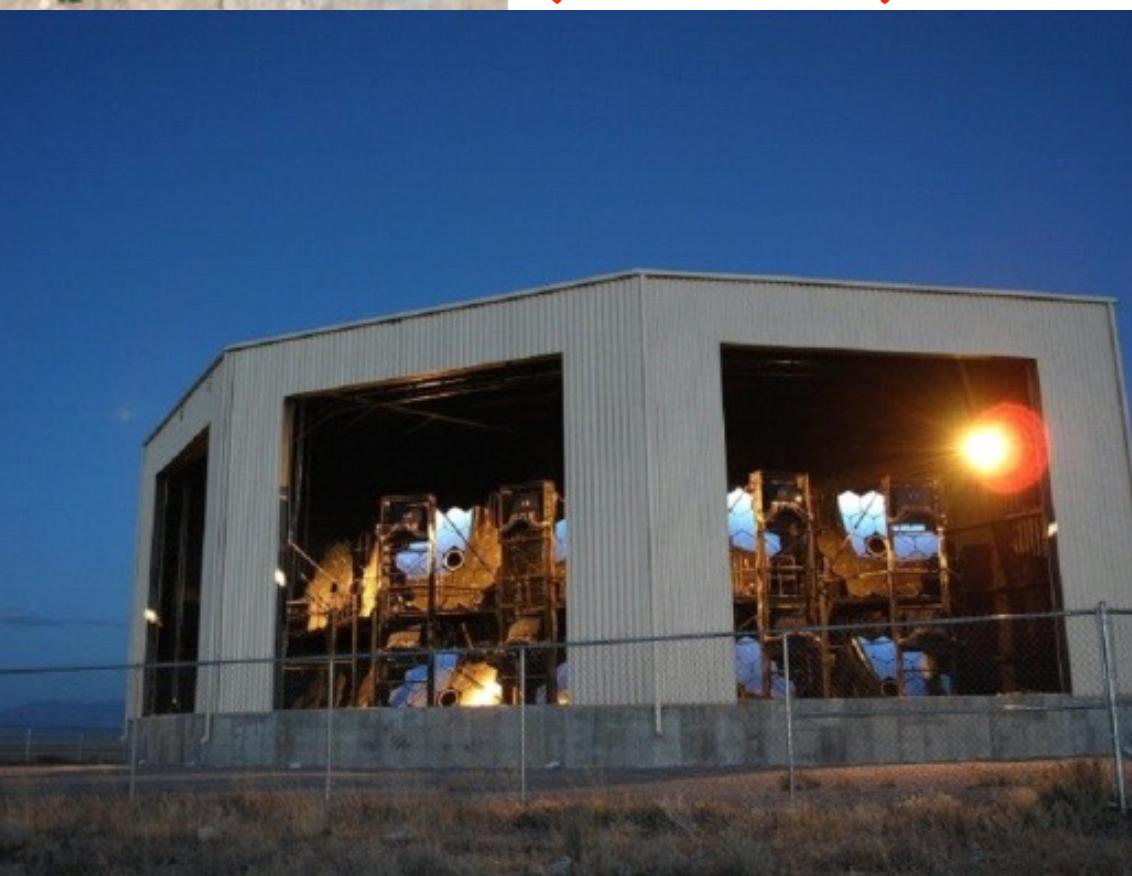
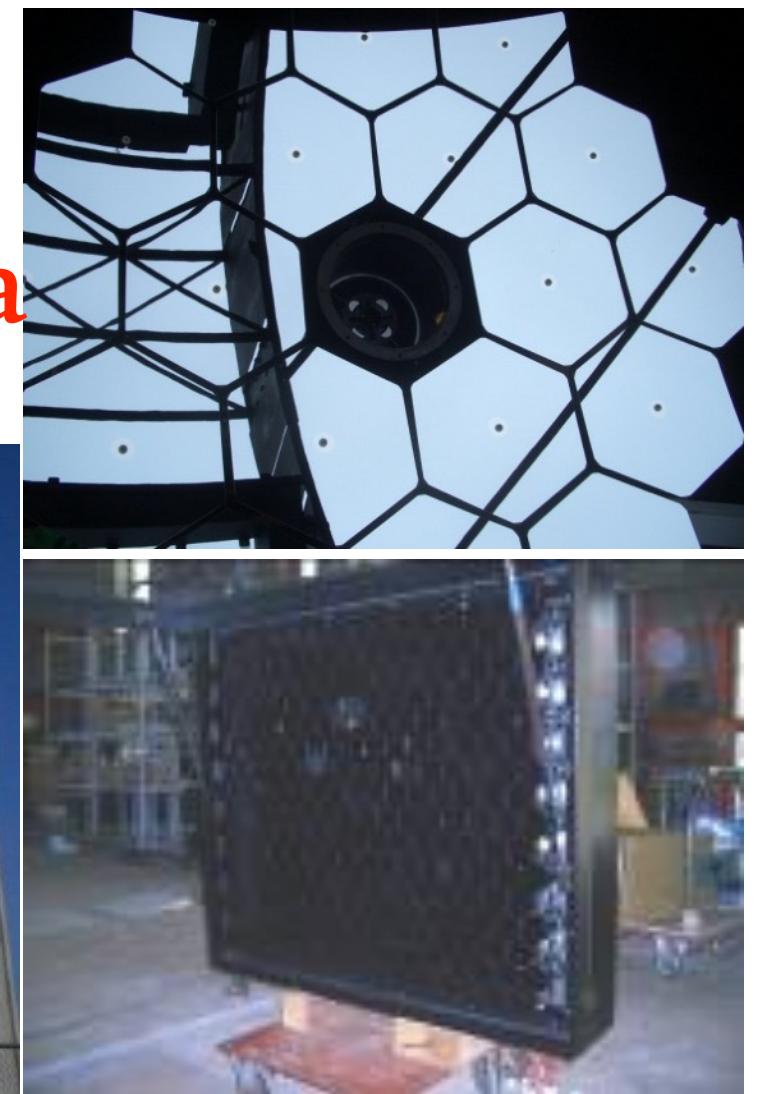
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14 telescopes @ station  
Reutilized from HiRes-1



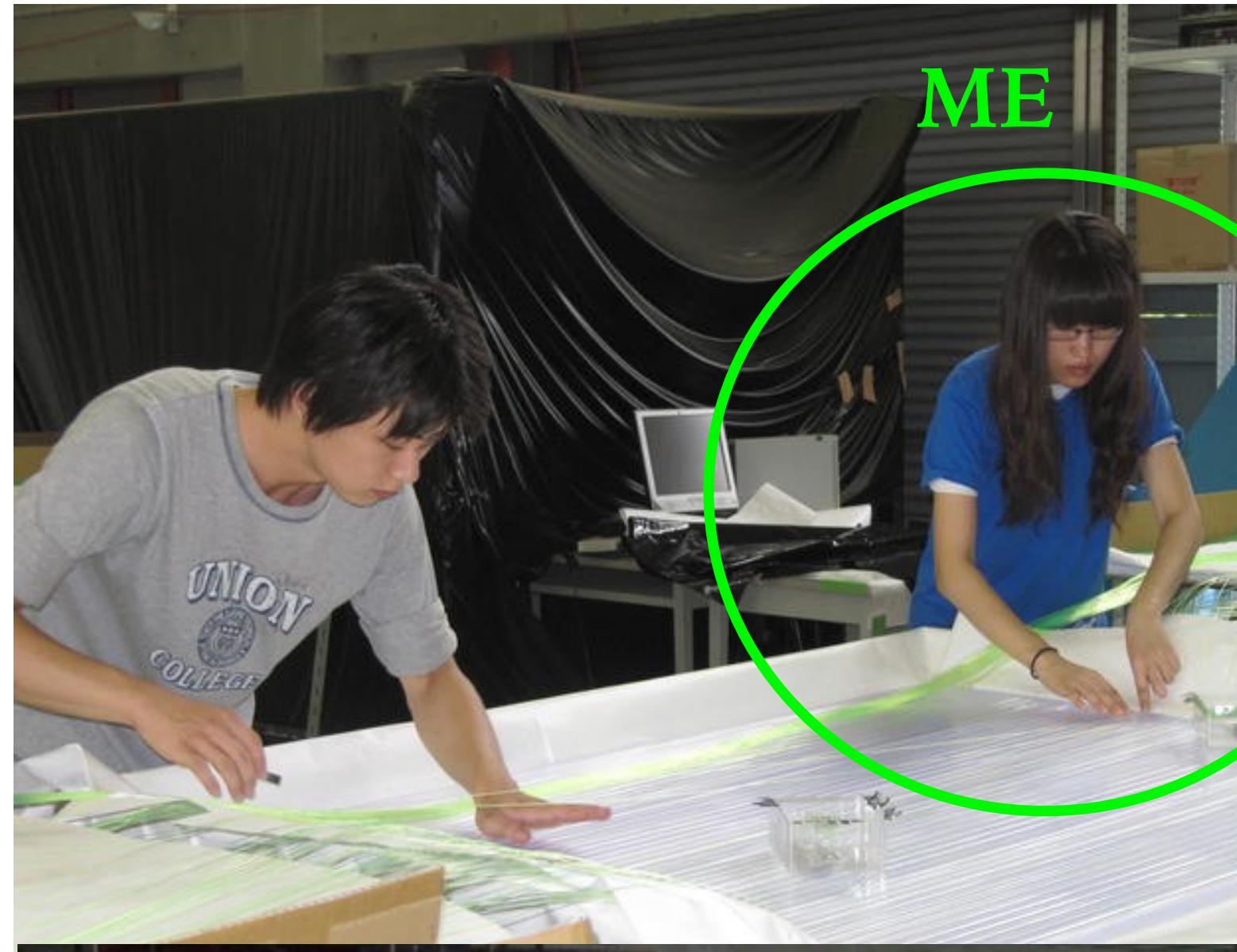
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Black Rock Mesa  
(BRFD)

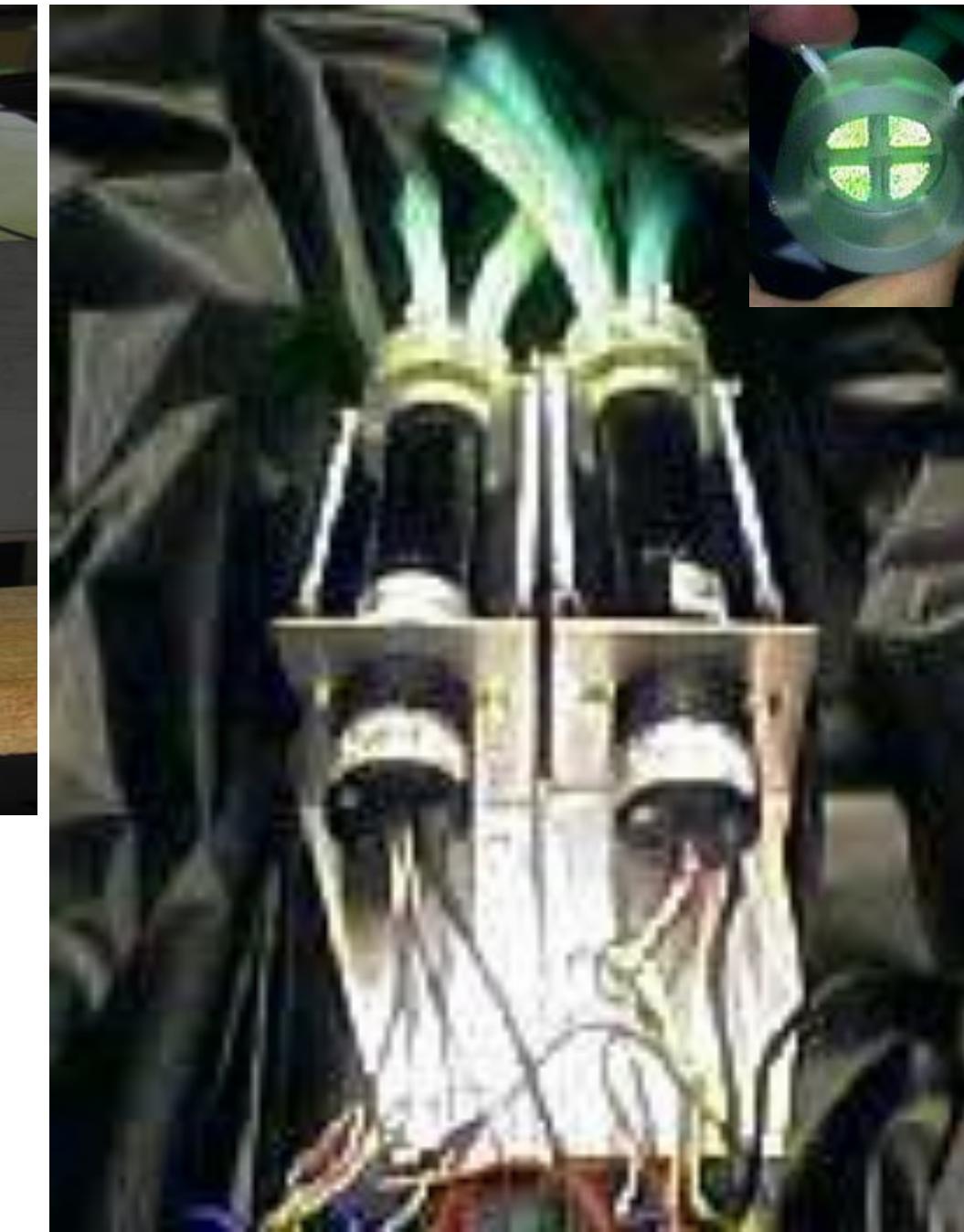


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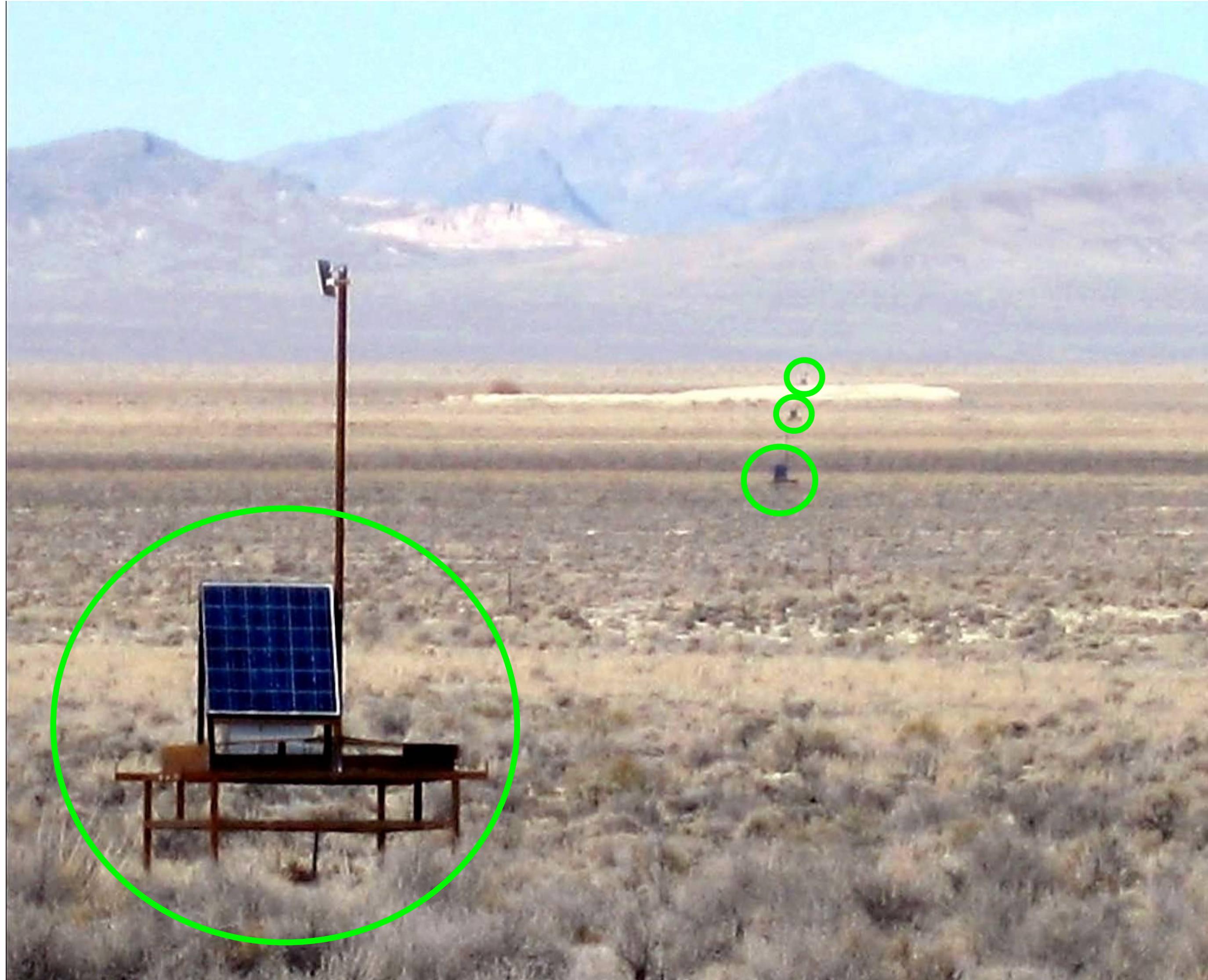
# EXPERIMENT - TA SURFACE DETECTOR (SD)



2 layers scintillator  
1.25 cm thick, 3 m<sup>2</sup> area  
Optical fibers to PMTs



# EXPERIMENT - TA SURFACE DETECTOR (SD)



© M.Fukushima

1.2 km spacing  
radio communication/trigger  
Solar/Battery power  
24/7 operation

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# EXPERIMENT - TA SURFACE DETECTOR (SD)

TALE SD (103) Deployment



TAX4 SD (560) Site Staking

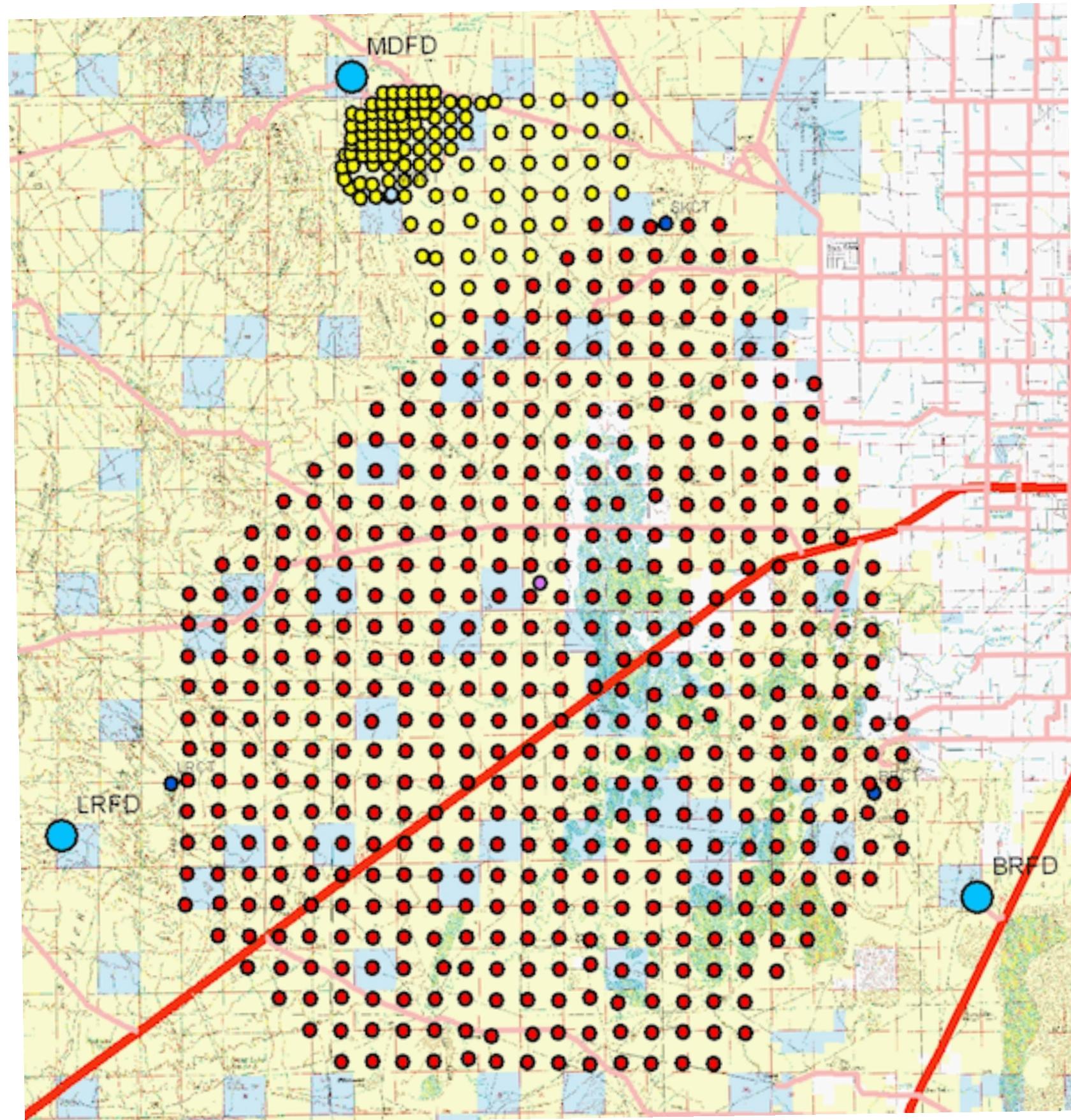


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# EXPERIMENT - TA + TA LOW ENERGY EXTENSION (TALE)

- Low energy particles are not as bright - closer
- Low energy particles develop higher up



© R.Cady

- 10 new telescopes looking higher in the sky at MDFD site
- 103 surface detectors (○)



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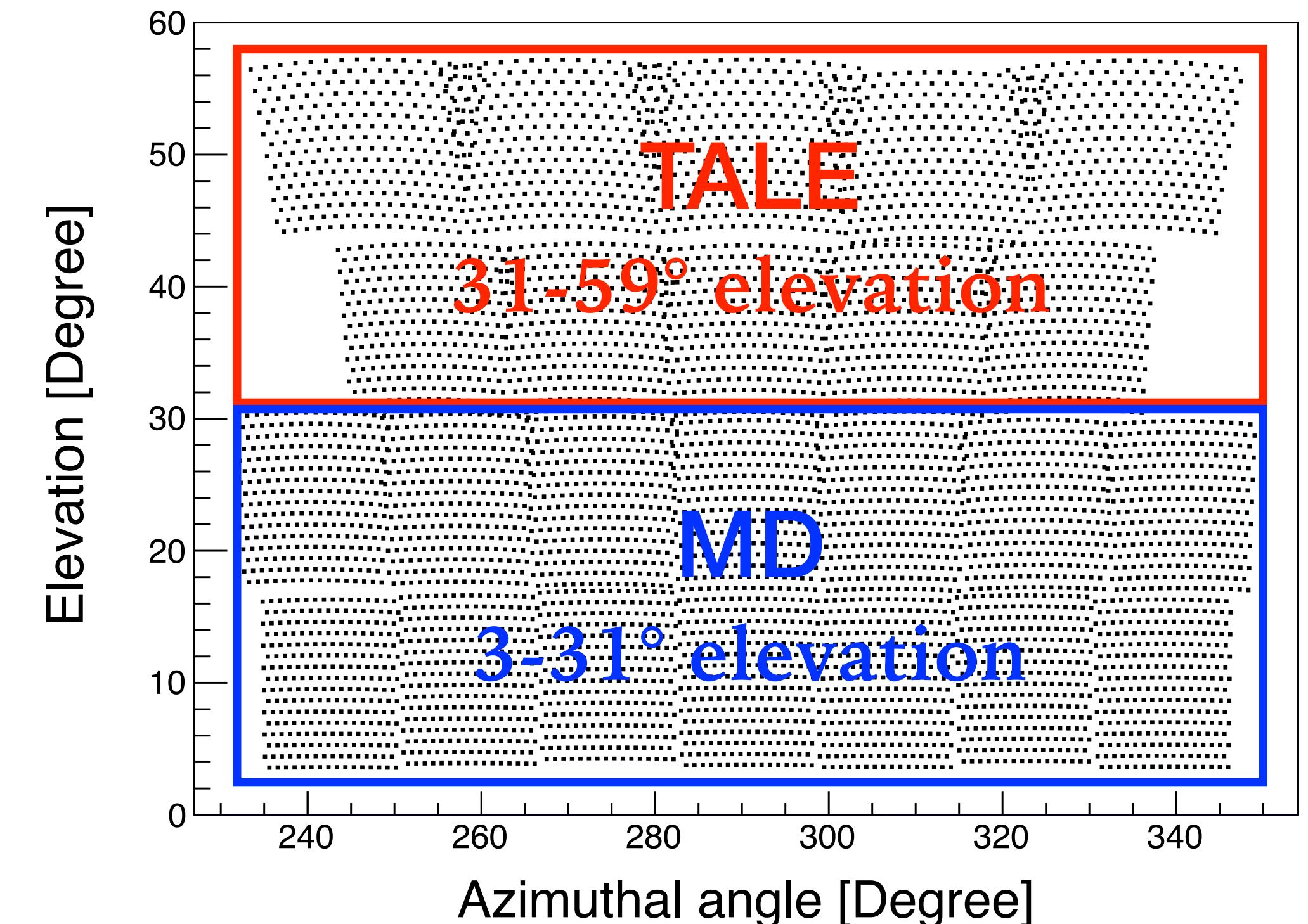
# EXPERIMENT - TA + TA LOW ENERGY EXTENSION (TALE)



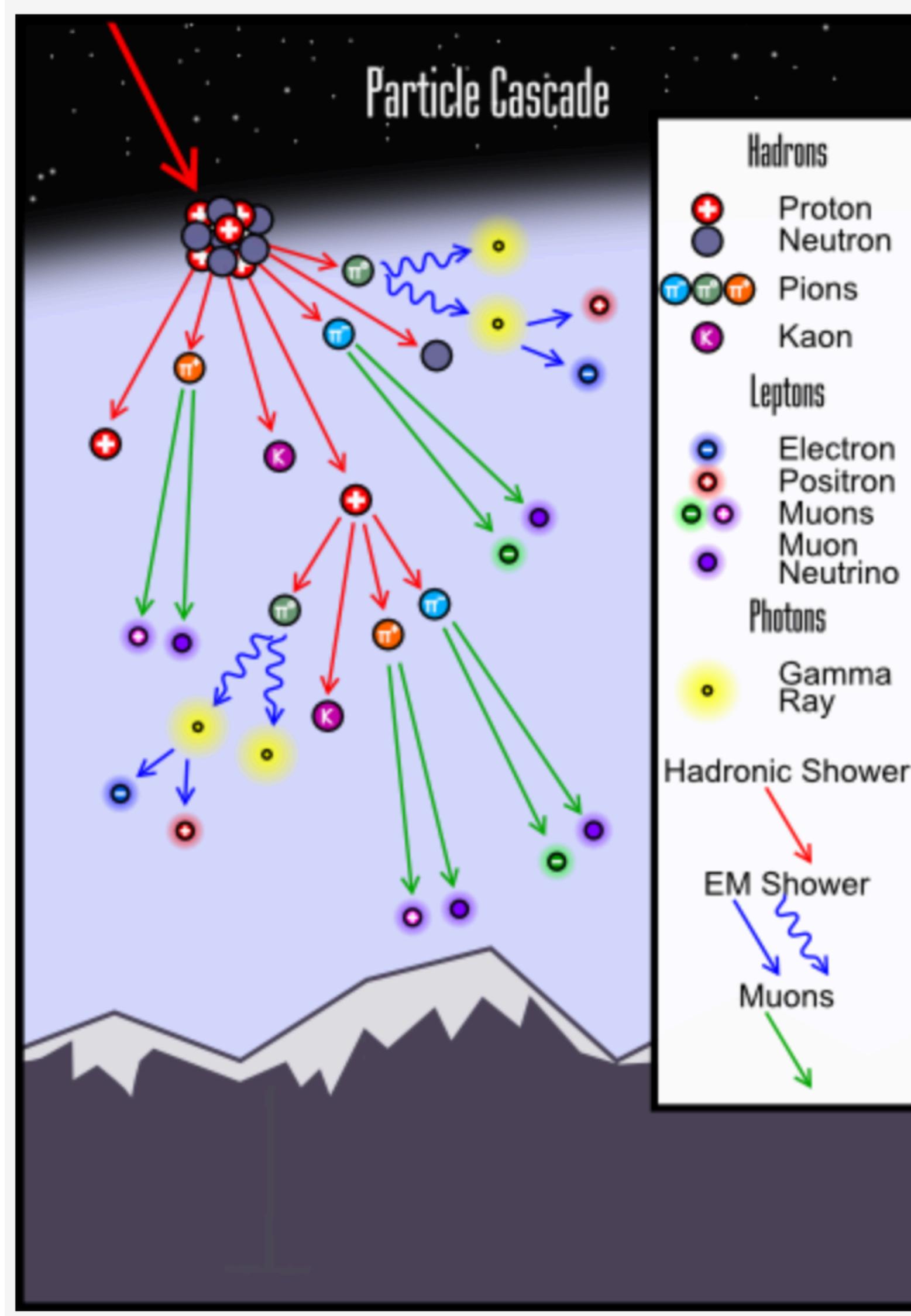
Field of View

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- Monocular reconstruction of combined MD and TALE telescope data
- MD (**2 rings**) and TALE (**2 rings**) FDs
- Enable us to observe the full development of showers

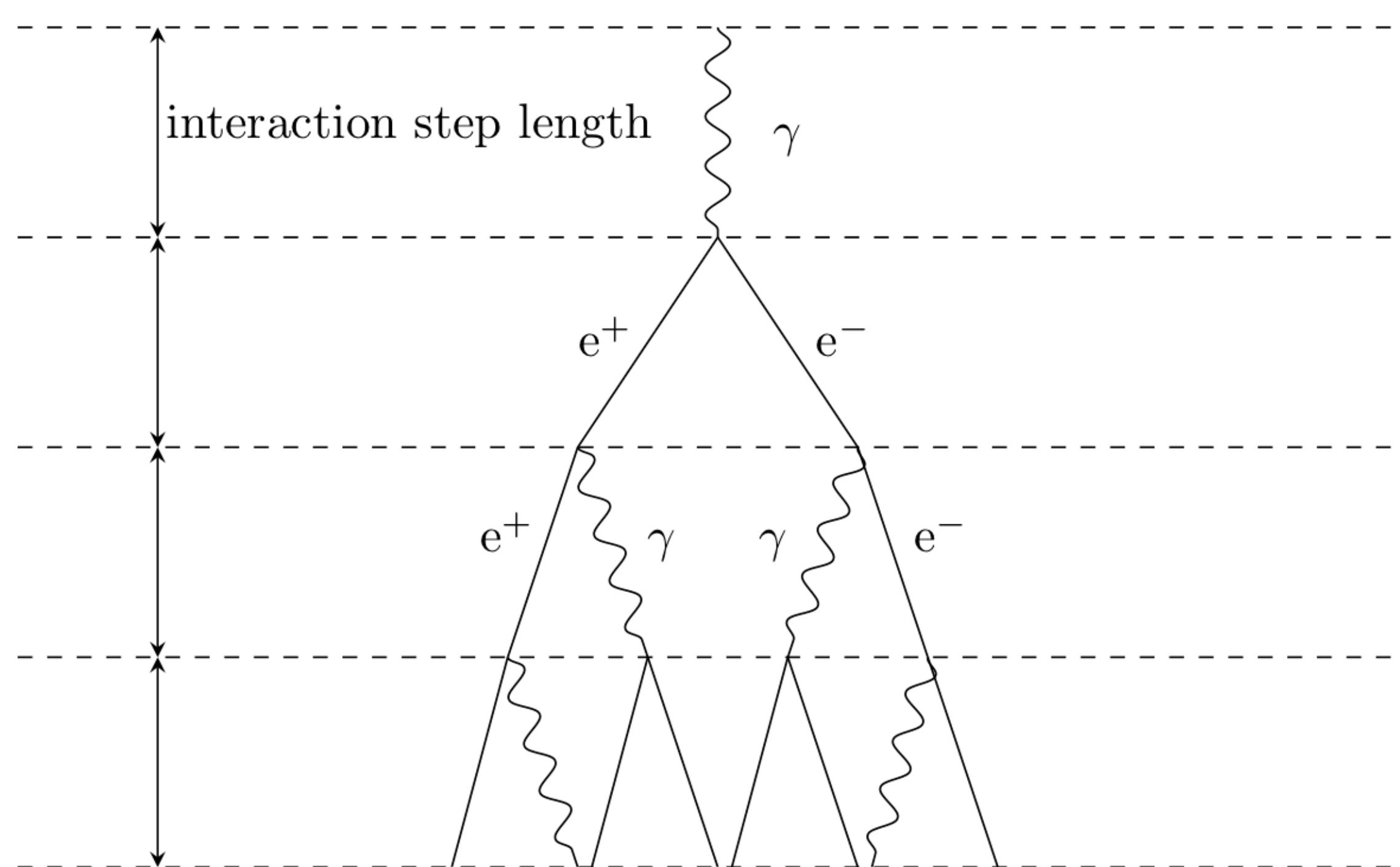


# EXTENSIVE AIR SHOWER (EAS)



- High Energy Cosmic Rays induce a cascade of secondary particles when they collide with air molecules high in the atmosphere. Called as Extensive Air Shower (EAS)
- For  $10^{19}$  eV, about  $10^{10}$  charged particles are created at shower maximum
  - 85% of total energy ( $e^\pm$  and  $\gamma$ )
  - 10% of total energy ( $\mu^\pm$ )
  - 4% of total energy ( $\pi^\pm$ )
  - the remainder ( $\nu$ )

# EXTENSIVE AIR SHOWER - ELECTROMAGNETIC SHOWERS

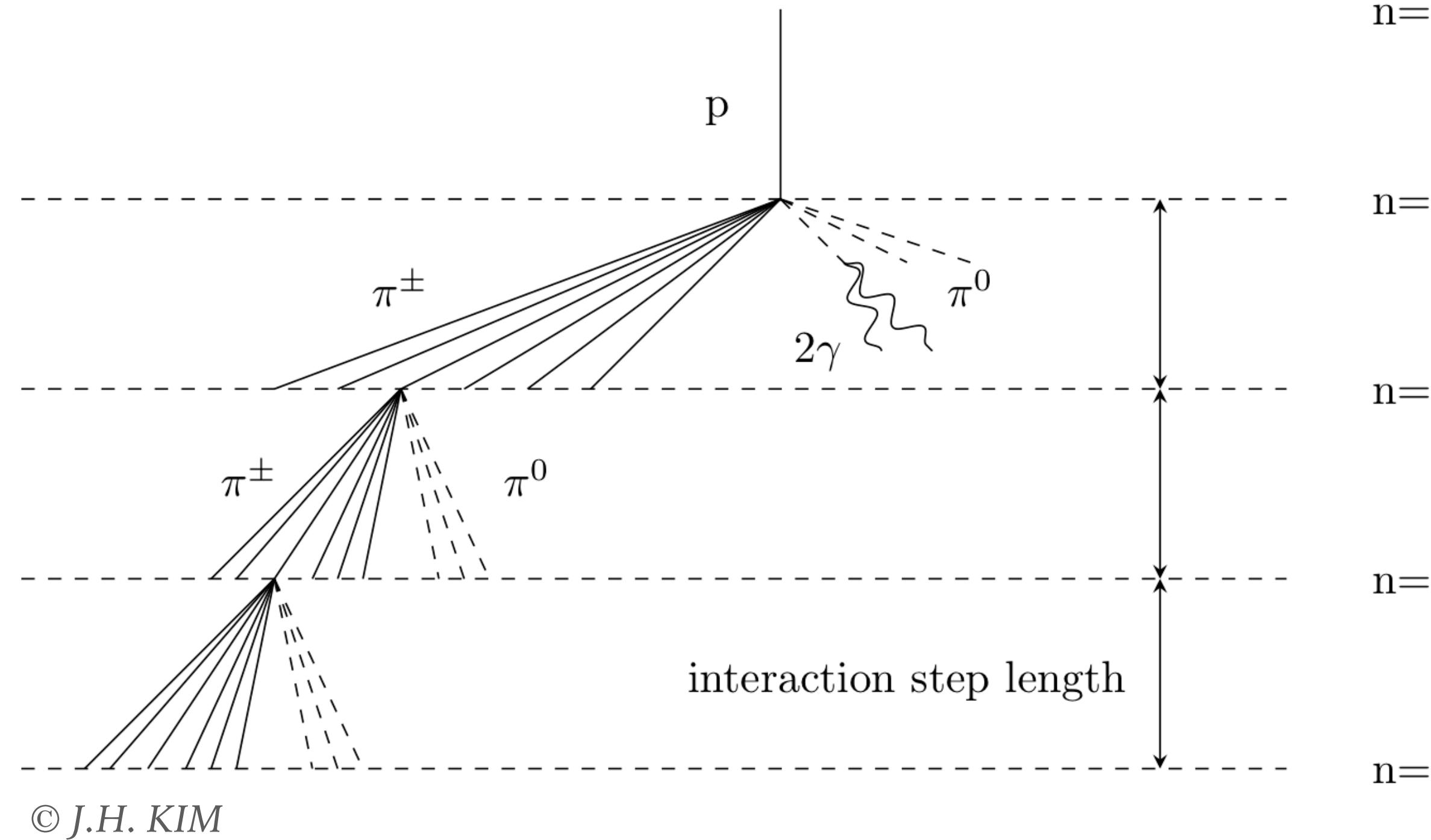


- n=0    ➤ Heitler model: very simple model
- n=1    ➤ Only e<sup>±</sup> and  $\gamma$
- n=2    e<sup>±</sup> : bremsstrahlung  
 $\gamma$  : pair production
- n=3    ➤ Each interaction
  - # of particles doubled
- n=4    - energy of particles divided equally

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- # of particles at shower maximum :  $N_{\max} = E_0/\epsilon_c$  (  $\epsilon_c$  : critical energy)
- Depth of shower maximum :  $X_{\max} = X_0 \ln(E_0/\epsilon_c)$

# EXTENSIVE AIR SHOWER - HADRONIC SHOWERS



- n=0 ➤ Heitler-like model: very simple model
- n=1 ➤ Cosmic ray proton with a total energy,  $E_0$ , collides with air molecule
- n=2 ➤ Each interaction
  - $N_{ch}$  of  $\pi^\pm$  &  $1/2 N_{ch} \pi^0$
  - $\pi^\pm (2/3 E_0)$  and  $\pi^0 (1/3 E_0)$

- $\pi^0 \rightarrow 2\gamma$  (electromagnetic sub showers), while a few  $\pi^\pm$  decay to  $\mu$  and  $\nu_\mu$
- $X_{max}$  for a nuclei with mass number A :  $X_{max} = X_{p\ max} - X_0 \ln(A)$ ; higher than proton
- Iron showers :  $\sim 40\%$  more muons than proton showers

$\langle X_{max} \rangle$  : 80-100 g/cm<sup>2</sup> shallower

# MONTE CARLO (MC) SIMULATION

- For Fluorescence Detector (FD) measurement, the aperture depends significantly on energy
  - High energy events - more particles/brighter, seen from greater distances
  - Lower energy events only visible nearby
- Aperture ( $A\Omega$ )

$$A\Omega = \frac{N_{\text{Reconstructed}}(E)}{N_{\text{Thrown}}(E)} \times A_0\Omega_0$$

$N_{\text{Reconstructed}}(E)$  # of reconstructed MC events

$N_{\text{Thrown}}(E)$  # of thrown MC events

$A_0$  effective area

$\Omega_0$  solid angle

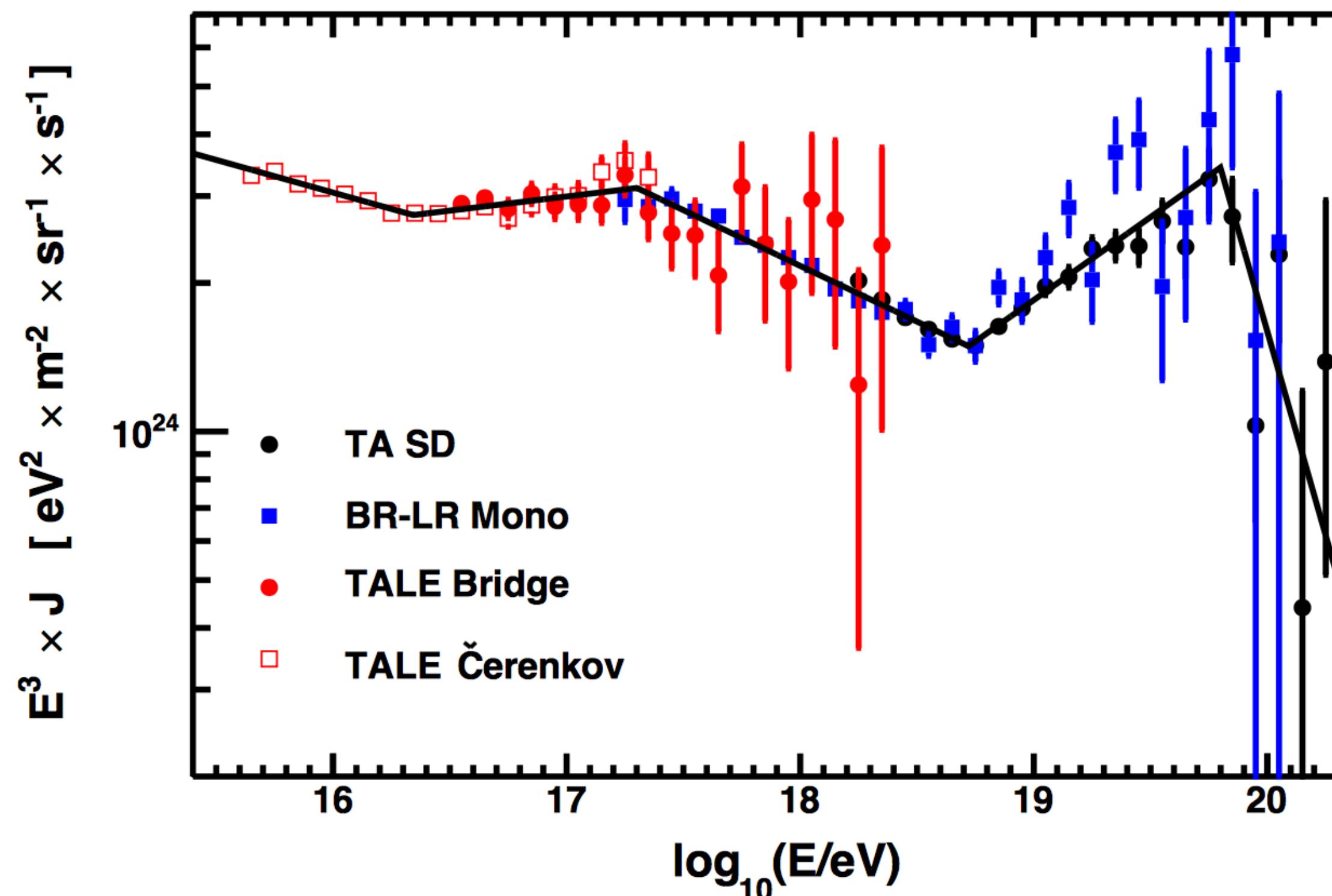
# MONTE CARLO (MC) SIMULATION

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1. Input previous measurement such as the energy spectra and compositions
2. Generate showers using CORSIKA (COsmic Ray Simulations for KAscade) program
3. Undergo light generation, atmospheric scattering and light transmission
4. Detector response, trigger, and readout then write MC events into the same format as the data
5. Analyze MC event with the exact same programs as are used for data analysis
6. Compare analyzed data with the analyzed MC.

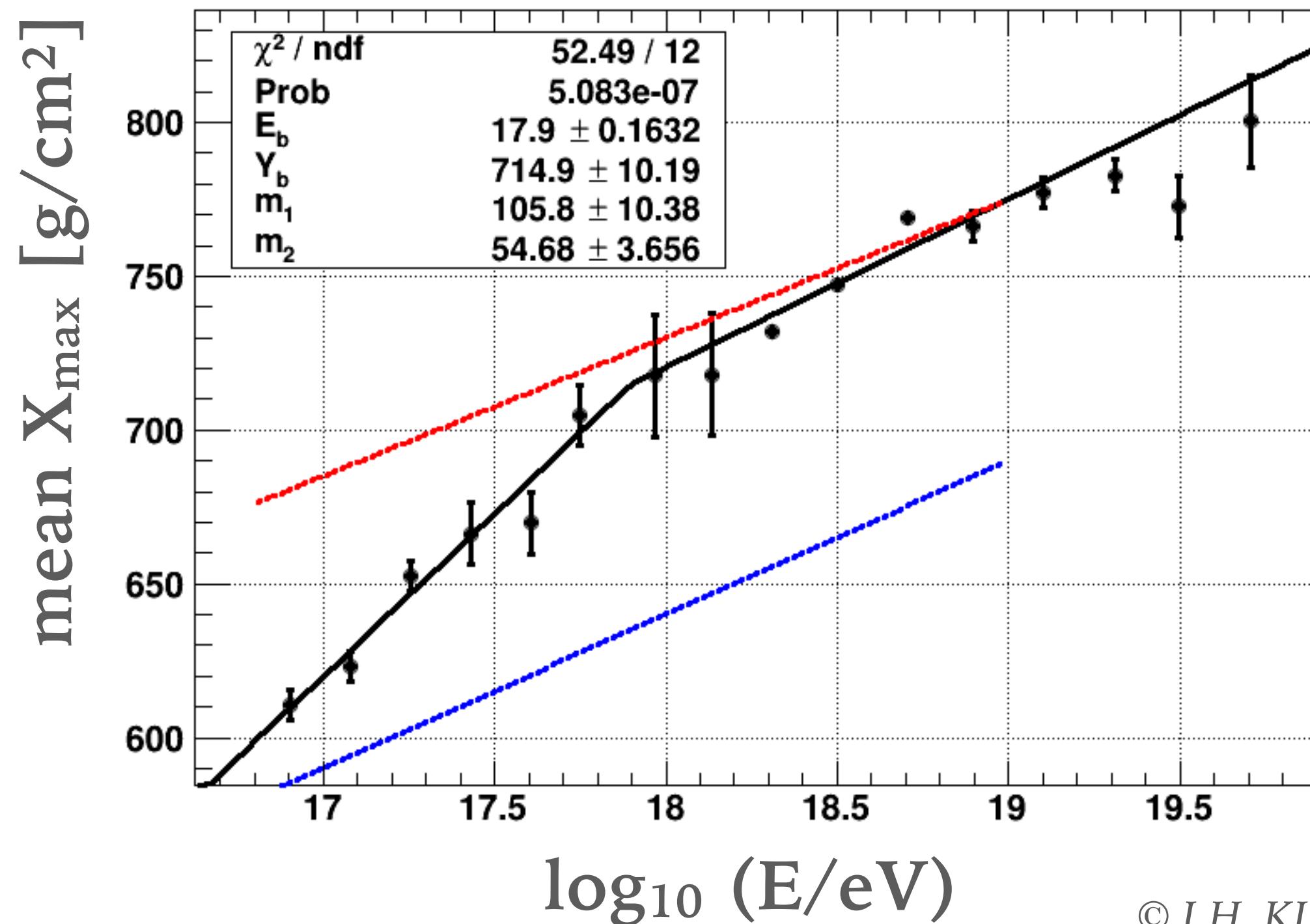
# MONTE CARLO (MC) SIMULATION - INPUT SPECTRUM

- To make the MC events more realistic
- As the spectral reference, we used Telescope Array energy spectrum which presented in the International Cosmic Ray Conference (ICRC) 2015.
- Including 2nd knee, ankle, and GZK cutoff above  $10^{16}$  eV.

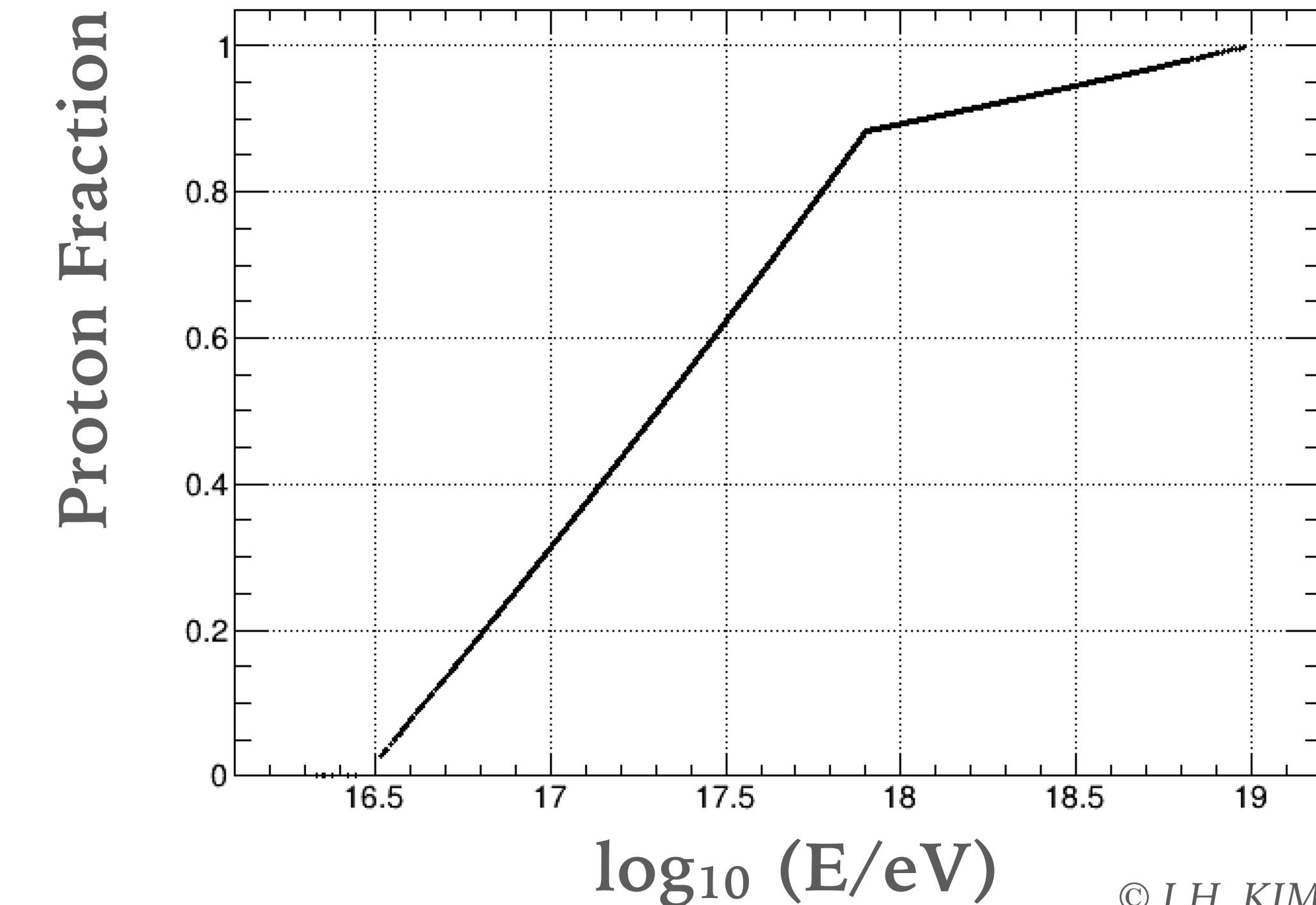


# MONTE CARLO (MC) SIMULATION - INPUT COMPOSITION

- To make the MC events more realistic
- As a composition reference, HiRes/MIA and HiRes  $X_{\max}$  results
- Translated to proton fraction as a function of energy



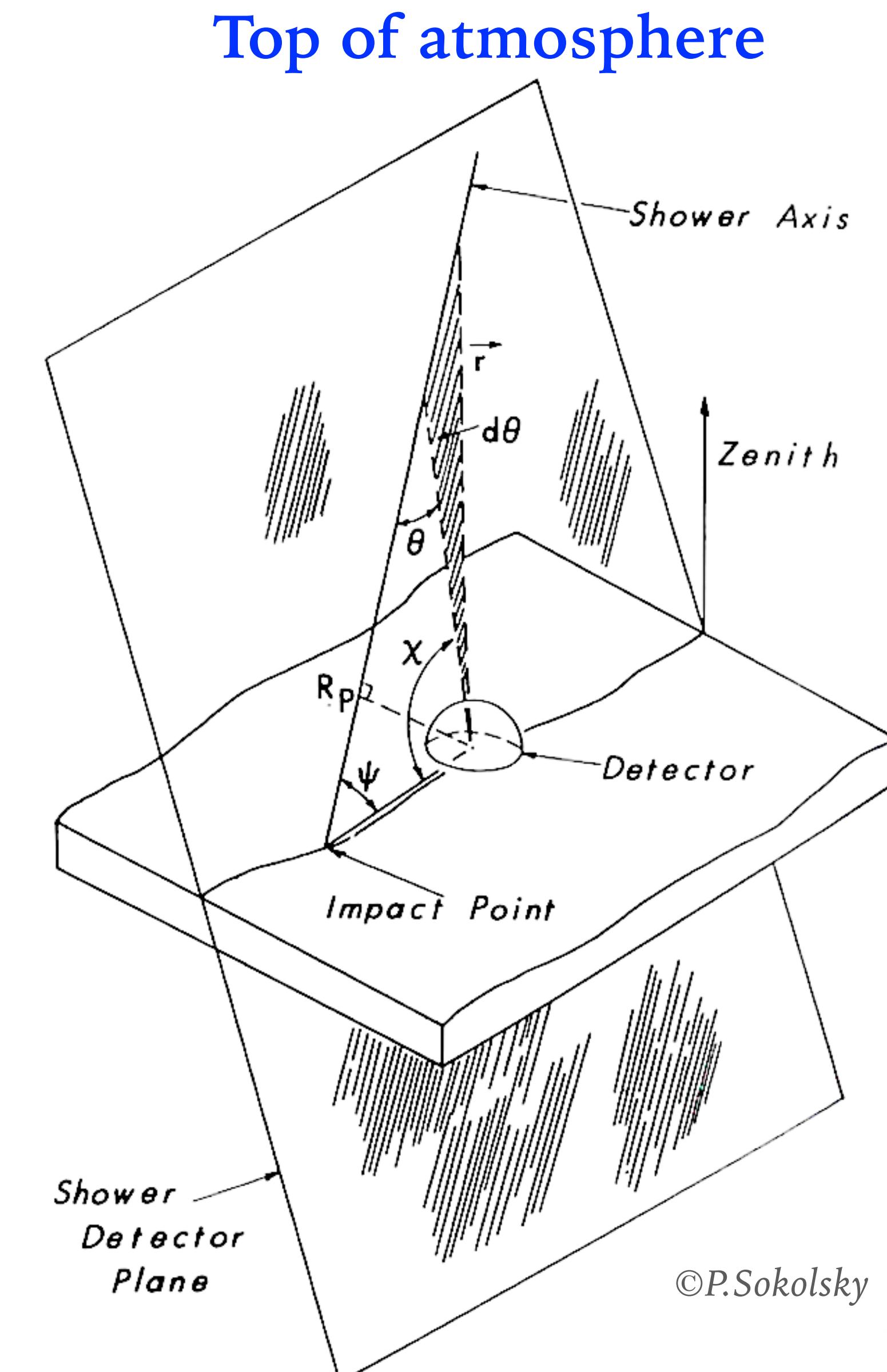
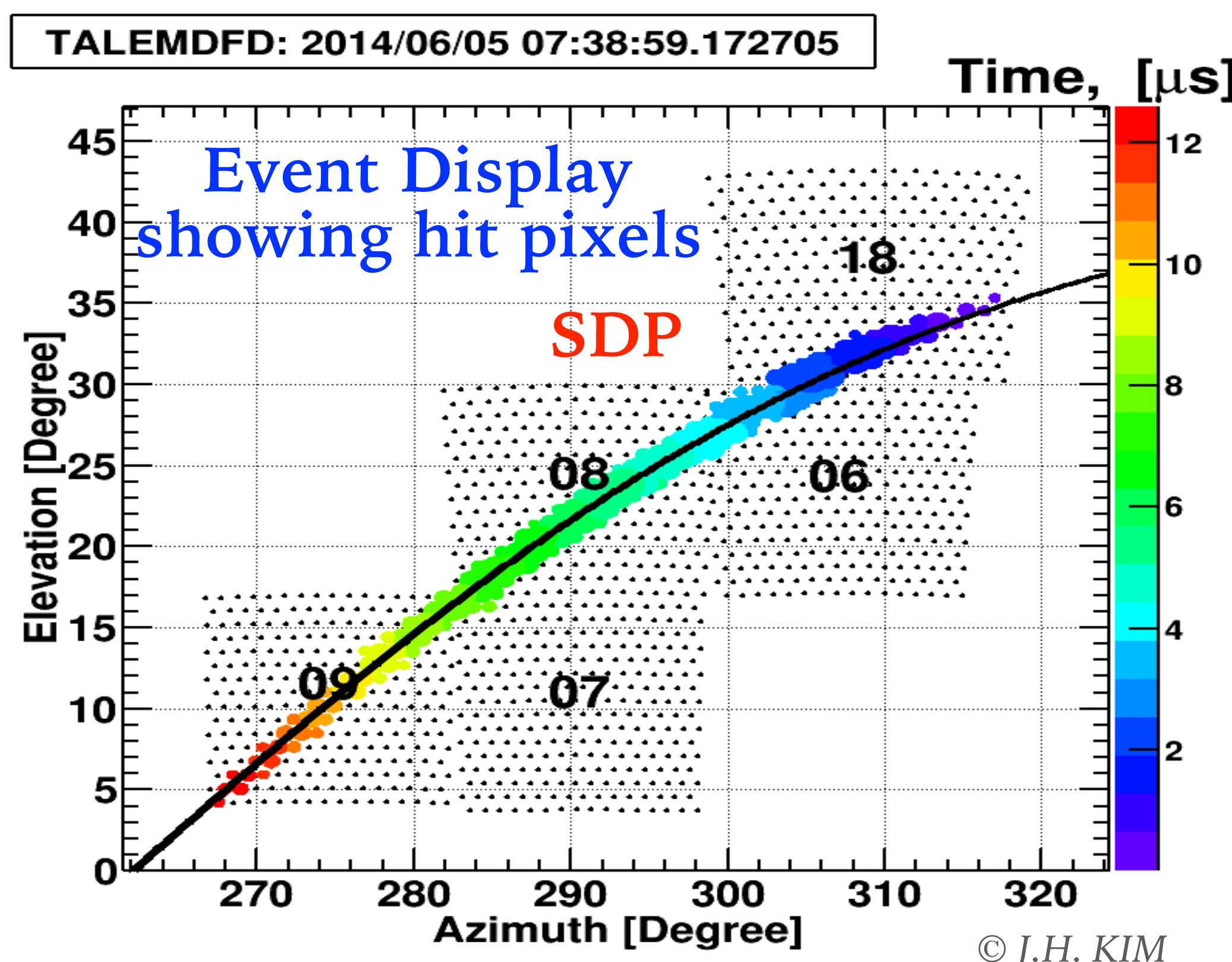
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# EVENT RECONSTRUCTION - GEOMETRY OF EXAMPLE EVENT

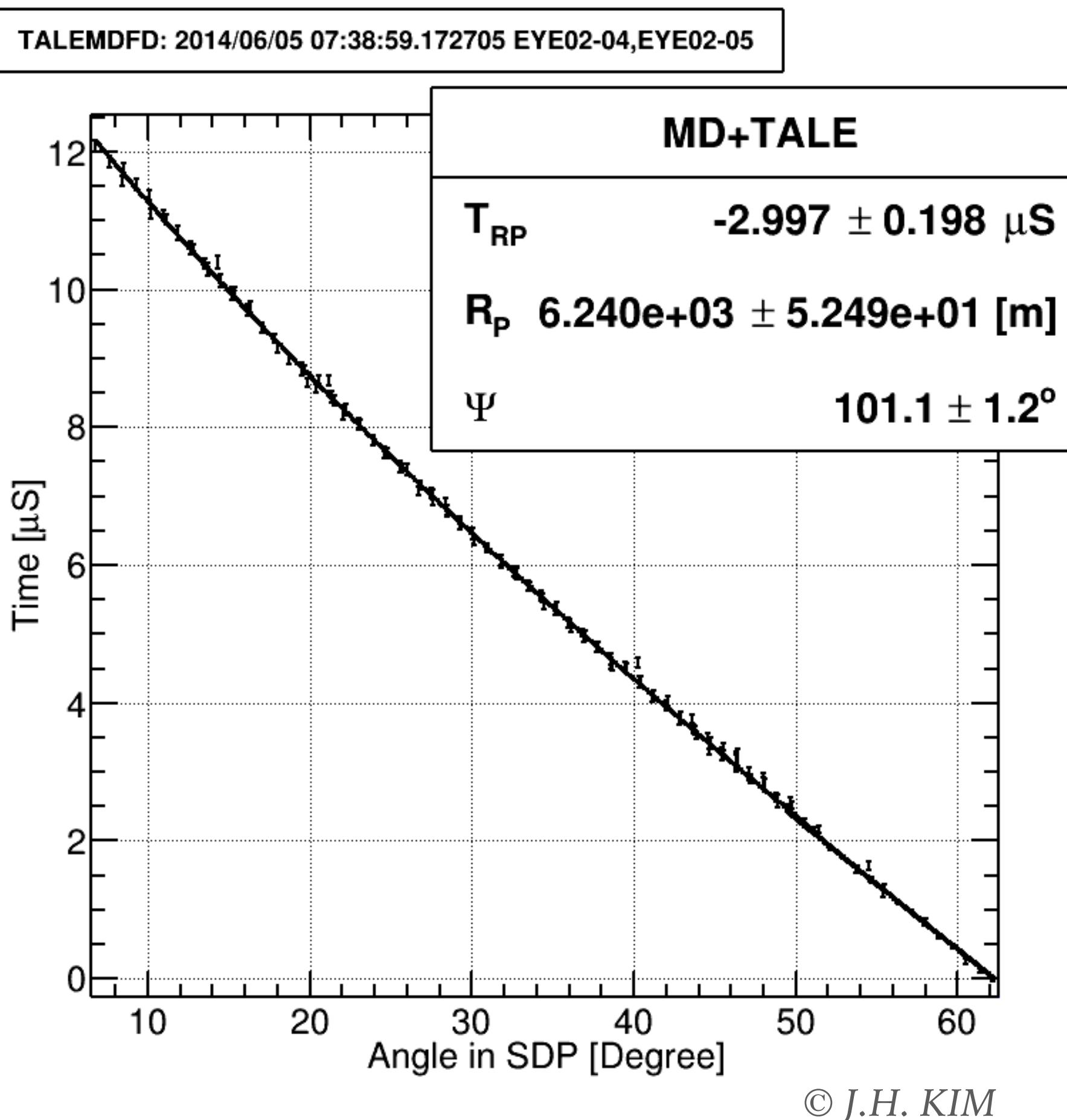
- To determine a shower detector plane
- Triggered tube's pointing direction
- Detector position



# EVENT RECONSTRUCTION - GEOMETRY OF EXAMPLE EVENT

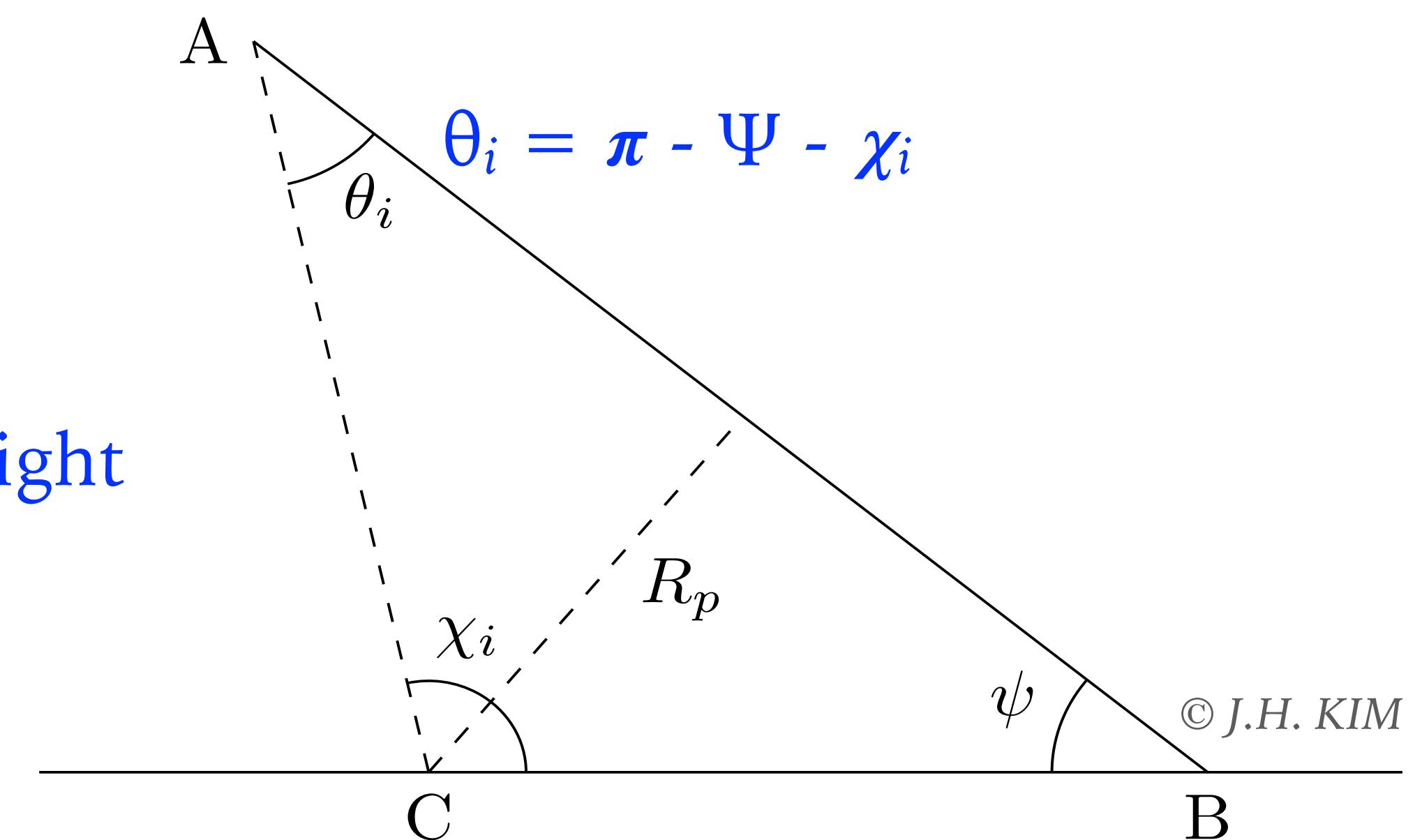
- Time vs. Angle Fit

$$t_i = t_{R_p} + \frac{R_p}{c} \cdot \tan\left(\frac{\pi - \psi - \chi_i}{2}\right)$$



Arrival times of light  
fit vs angle

$t_i$  trigger time of tube  $i$   
 $\chi_i$  pointing direction of tube  $i$   
 $\Psi$  in-plane angle  
 $R_p$  impact parameters  
 $c$  speed of light  
 $t_{RP}$  time at  $R_p$



# EVENT RECONSTRUCTION - PROFILE FIT

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- The Gaisser-Hillas parameterization formula

$$N_e(x) = N_{\max} \cdot \left[ \frac{x - X_0}{X_{\max} - X_0} \right]^{\frac{X_{\max} - X_0}{\lambda}} \cdot e^{\frac{X_{\max} - x}{\lambda}}$$

$N_e(x)$  # of charged particles at given depth,  $x$

$X_{\max}$  depth of shower max, g/cm<sup>2</sup>

$N_{\max}$  max # of particles

$X_0$  related to depth of the first interaction ( $X_0 = -100$  g/cm<sup>2</sup> set)

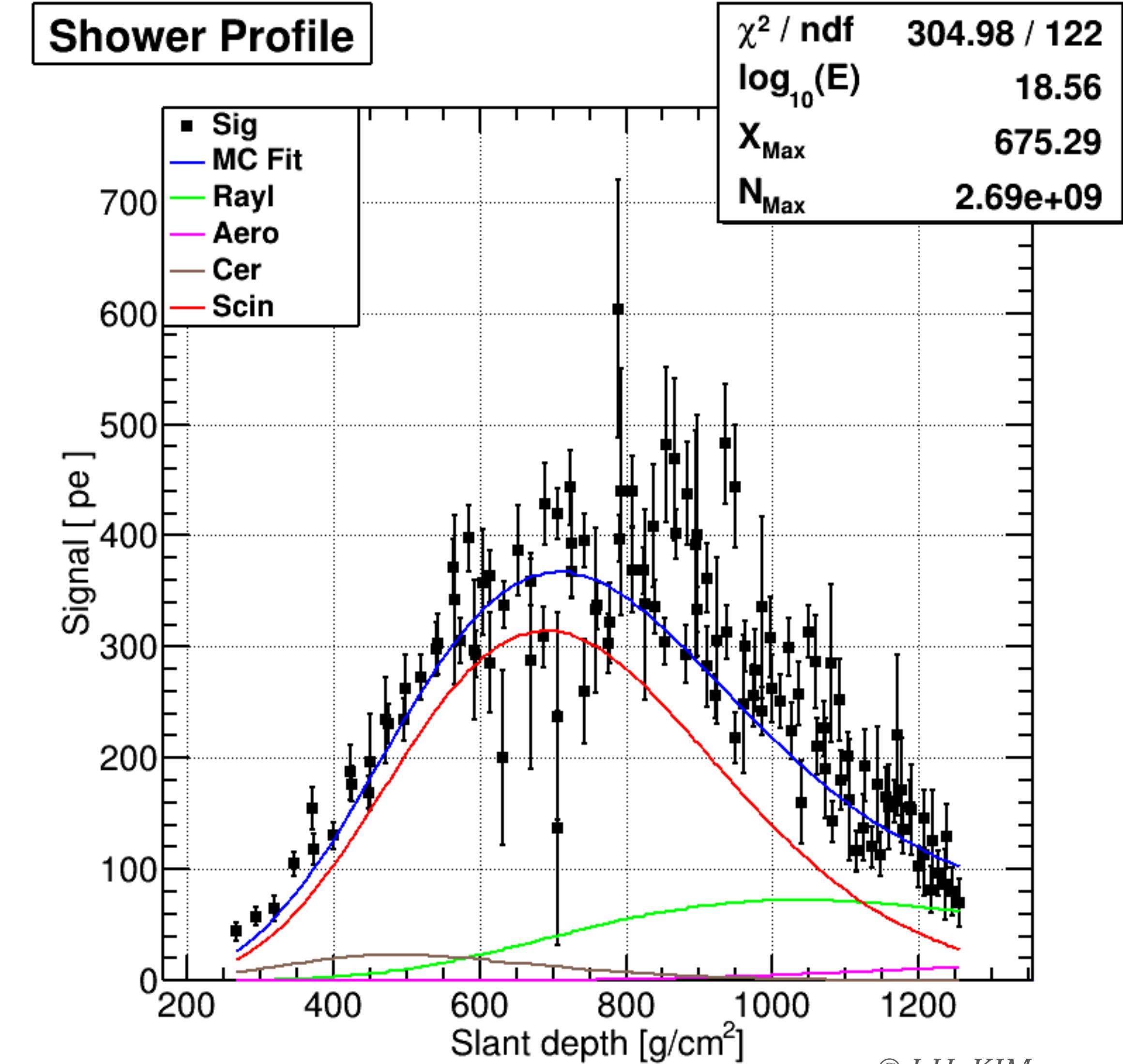
$\lambda$  related to width of the shower profile ( $\lambda = 70$  g/cm<sup>2</sup> set)

- The mean energy deposit parameterization (light generated/particle)
- Integrating Gaisser-Hillas parameterization with mean energy deposition, estimate calorimetric energy of visible part of shower

# EVENT RECONSTRUCTION - PROFILE FIT OF EXAMPLE EVENT

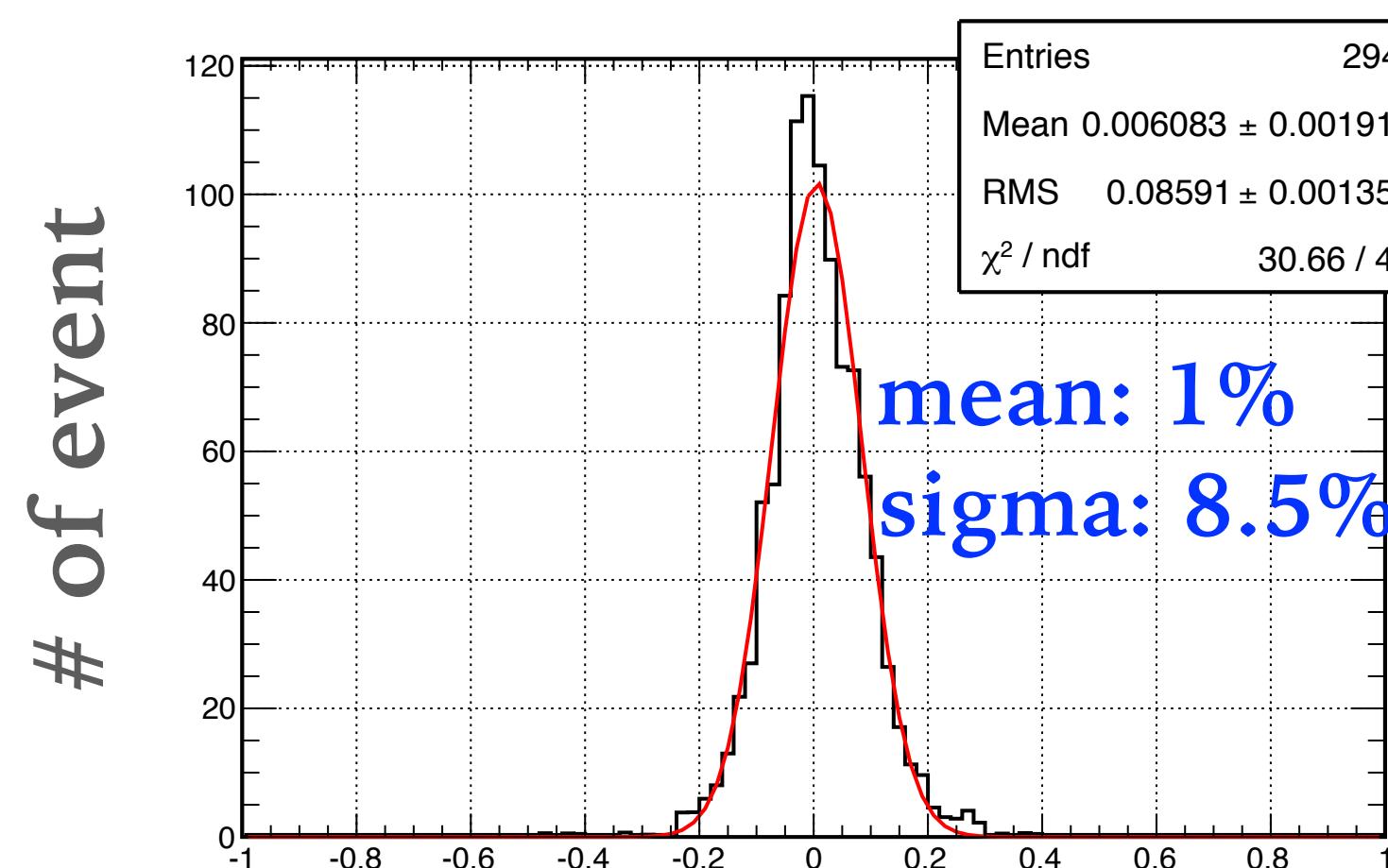
- Light signal fit vs slant depth to determine energy and depth of shower maximum,  $X_{\text{max}}$

Black: data  
 Blue: fit to total signal  
 Red: scintillation  
 Green: Rayleigh scattering  
 Magenta: Aerosol scattering  
 Grey: Direct Cherenkov

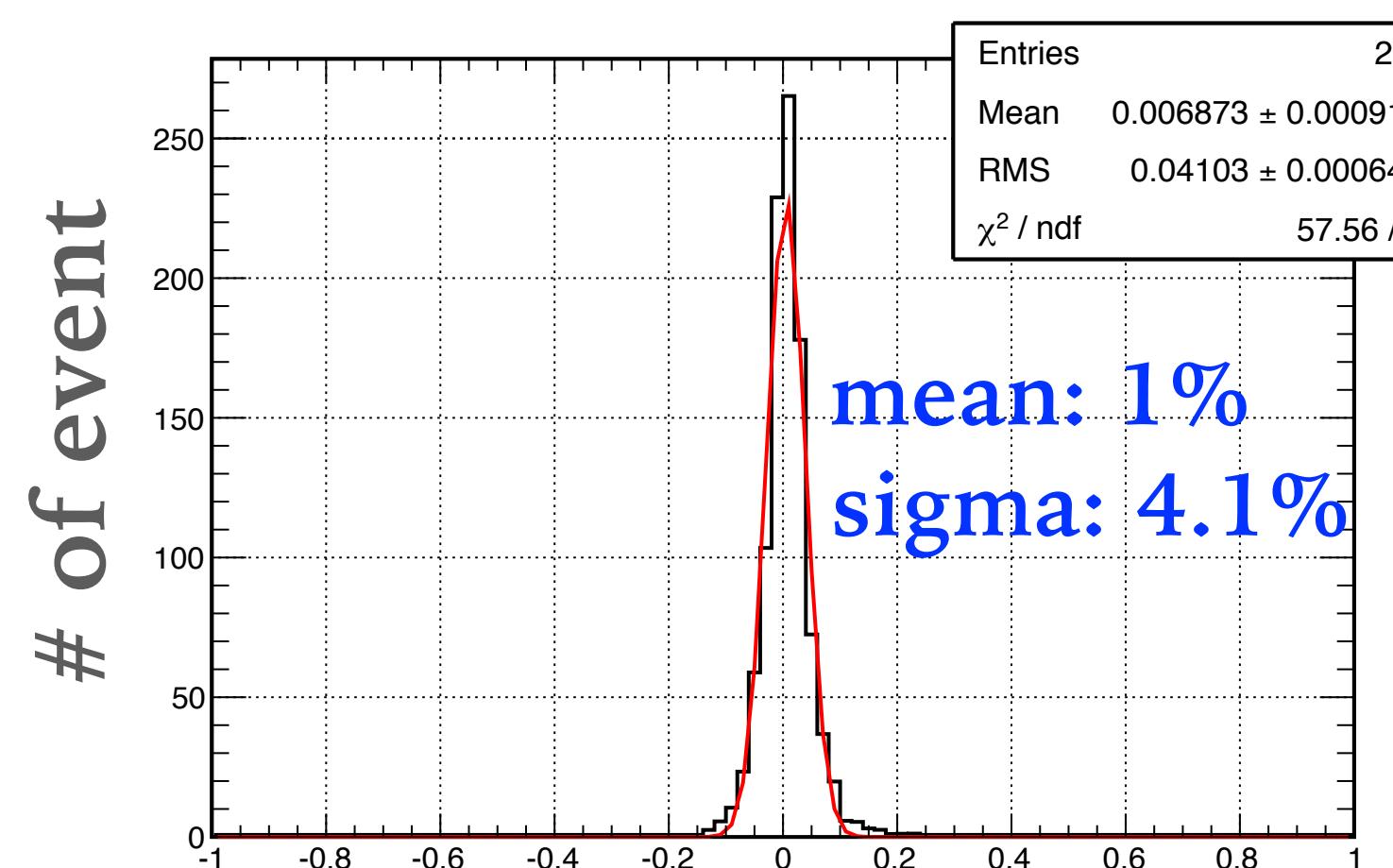


# MONTE CARLO (MC) SIMULATION - RESOLUTIONS

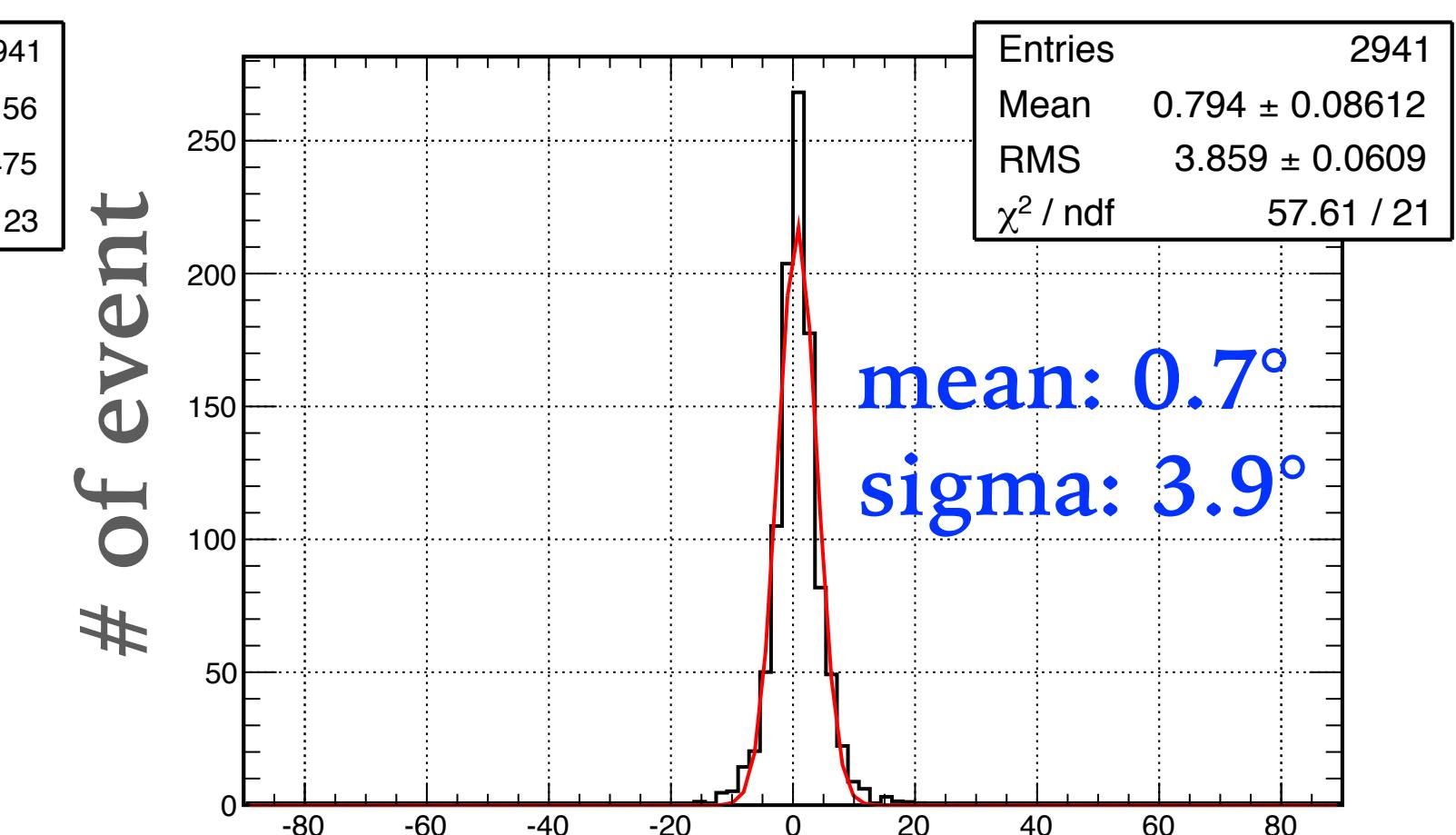
Total Energy ( $E_{\text{tot}}$ )



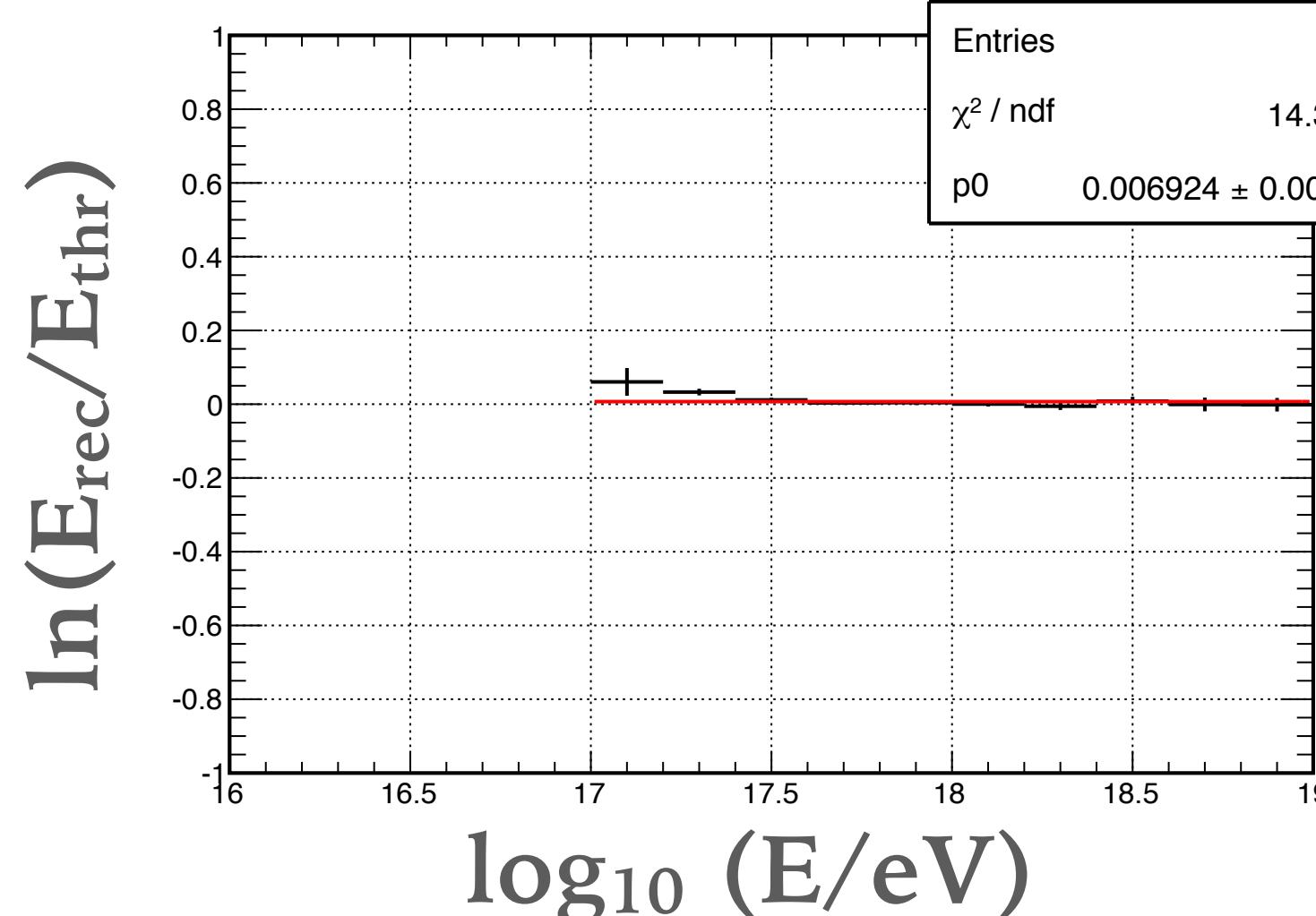
Impact parameter ( $R_p$ )



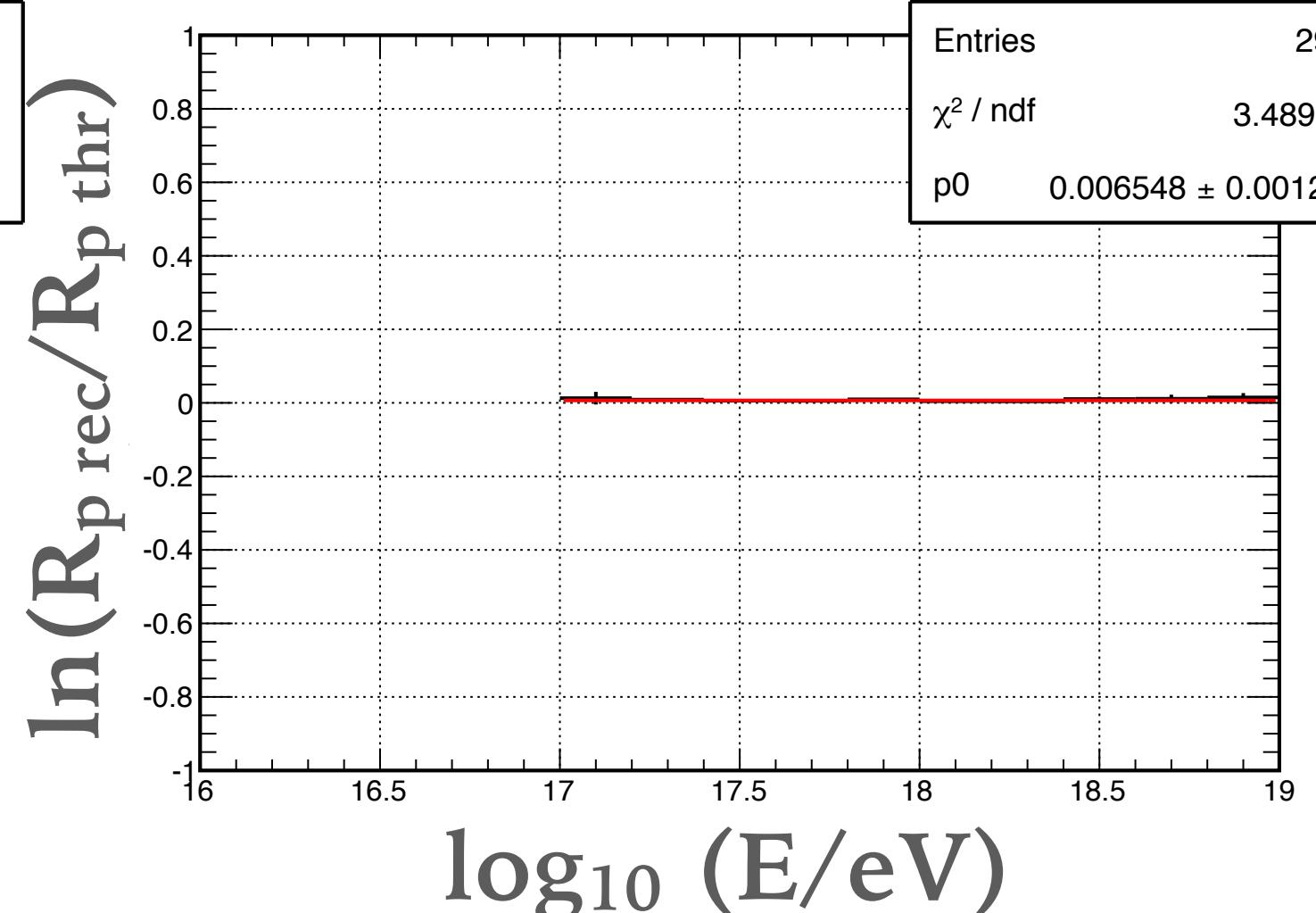
In-plane angle ( $\Psi$ )



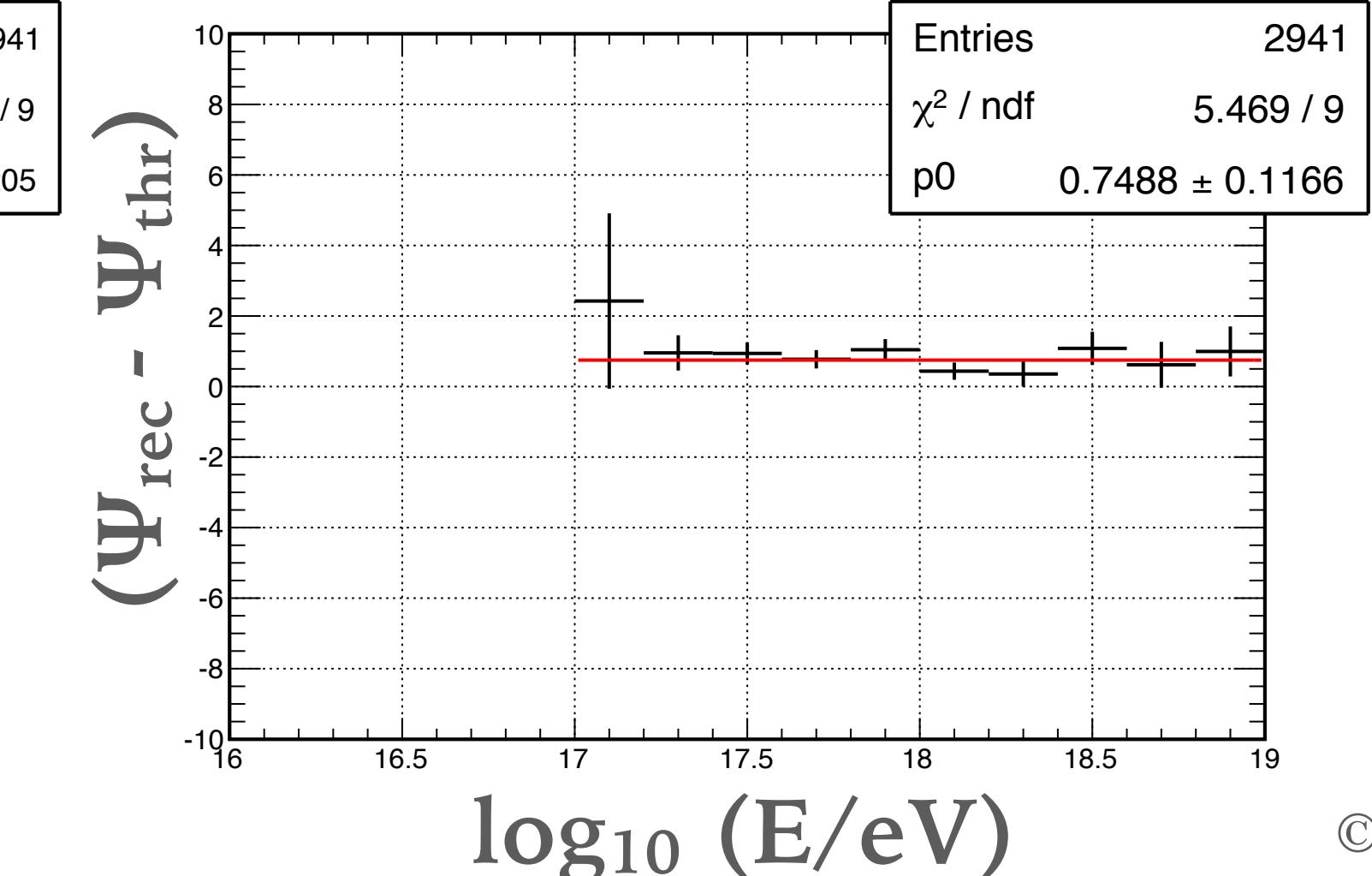
$\ln(E_{\text{rec}}/E_{\text{thr}})$



$\ln(R_p \text{ rec}/R_p \text{ thr})$



$(\Psi_{\text{rec}} - \Psi_{\text{thr}})$



# EVENT RECONSTRUCTION - QUALITY CUT

	TALE	MD	TALE and MD
Cut level 1		Down-going events only, Both MD and TALE running, Good weather	
Cut level 2		$\theta < 70^\circ$	
Cut level 3		$E_{rec\_tot} > 10^{16.5}$ eV	
Cut level 4		No track length cut	
Cut level 5	Crossing time $> 2 \mu\text{s}$	Crossing time $> 6 \mu\text{s}$	Crossing time $> 4 \mu\text{s}$
Cut level 6		No number of good tubes cut	
Cut level 7		An event must be successfully reconstructed (profile fit)	
Cut level 8		$\chi^2/\text{ndf}$ of profile fit $< 10$	
Cut level 9	<b>X<sub>max</sub> bracketing</b> ( $X_{\text{first}} > 200 \text{ g/cm}^2$ , $(X_{\text{last}} - X_{\text{first}}) > 150 \text{ g/cm}^2$ , $X_{\text{first}} < X_{\text{max}} < X_{\text{last}}$ )		
Cut level 10	$S_{\text{fraction}} > 1.05$	$S_{\text{fraction}} > 1.05$	$S_{\text{fraction}} > 1.20$
Cut level 11	$S_{\text{peak}} > 50.0$	$S_{\text{peak}} > 80.0$	$S_{\text{peak}} > 50.0$ , $S_{\text{peak}} \times R_p^2 > 3.2 \times 10^8$
Cut level 12	$d\Psi < 20^\circ$	$d\Psi < 12^\circ$	$d\Psi < 15^\circ$
Cut level 13		$\Psi < 120^\circ$	

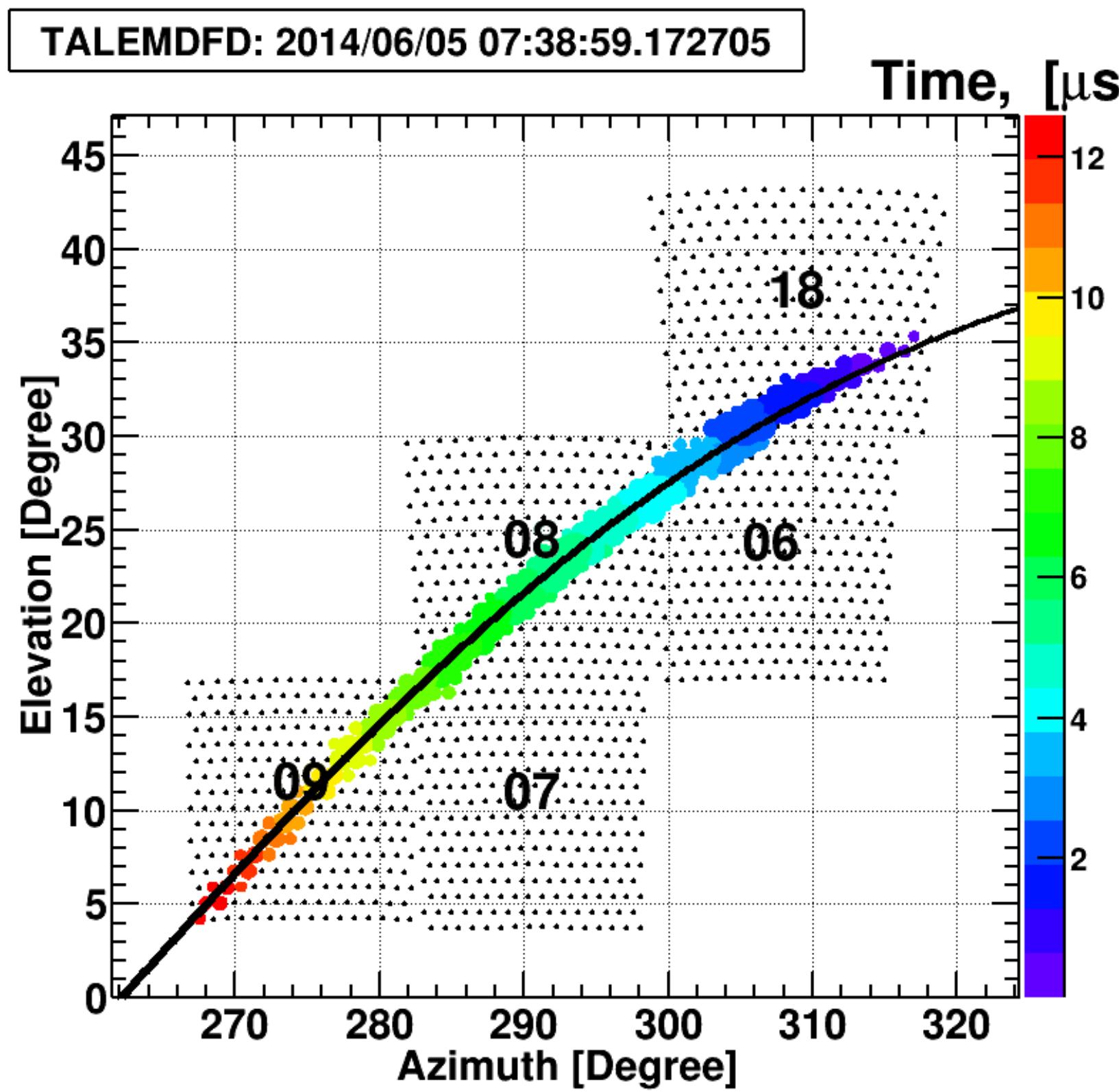
# EVENT RECONSTRUCTION - # OF DATA EVENTS AFTER QUALITY CUT

	TALE	MD	TALE and MD
Cut level 1	112642	9608	4034
Cut level 2	43810	5099	3177
Cut level 3	30439	4754	2805
Cut level 4	-	-	-
Cut level 5	428	1291	1113
Cut level 6	-	-	-
Cut level 7	375	1270	1109
Cut level 8	350	1223	1084
Cut level 9	144	935	886
Cut level 10	83	682	492
Cut level 11	71	139	461
Cut level 12	65	123	461
Cut level 13	65	118	455

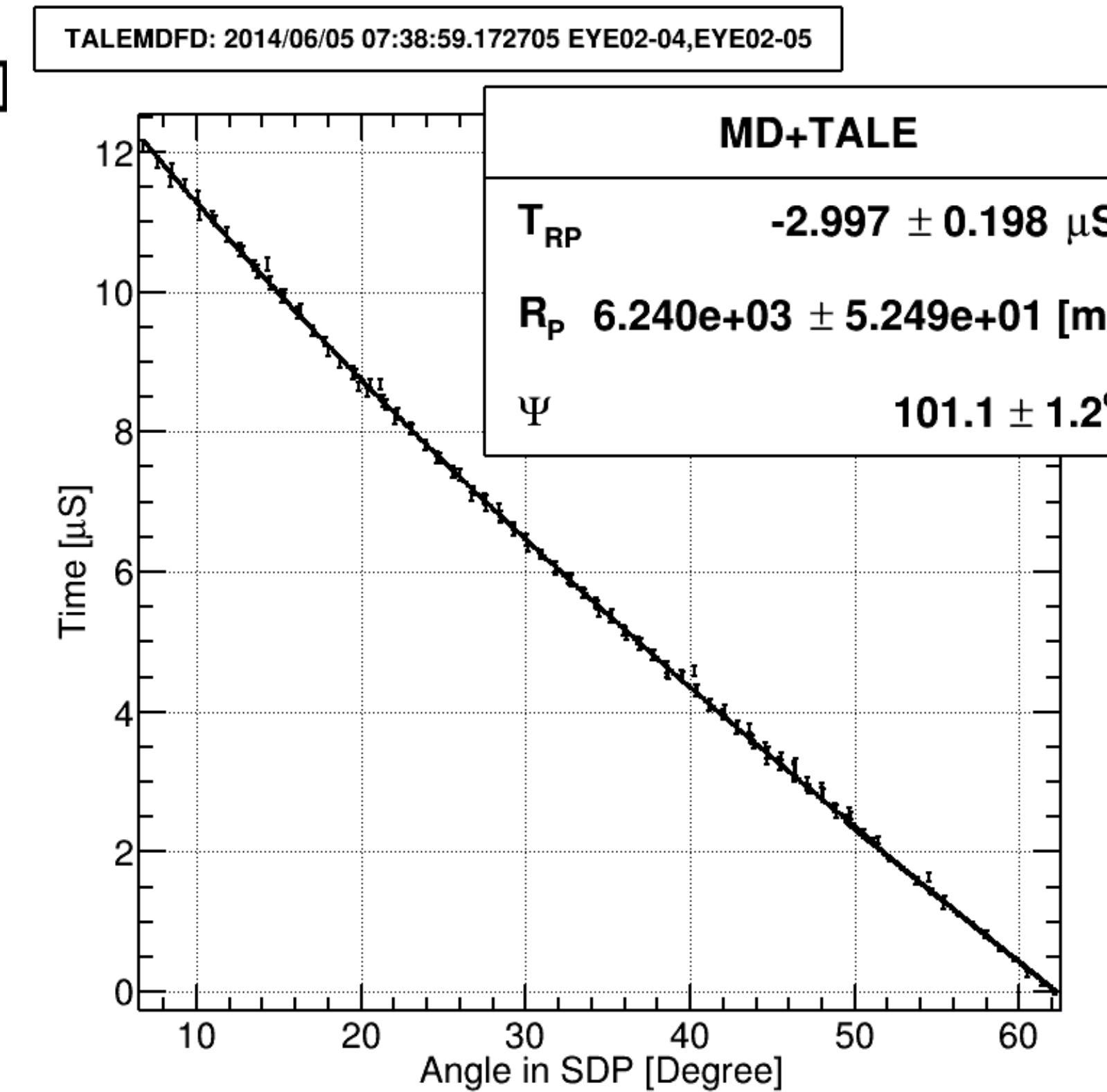
# EVENT RECONSTRUCTION - EXAMPLE EVENT

- An example of the data event triggered both Middle Drum and TALE telescopes

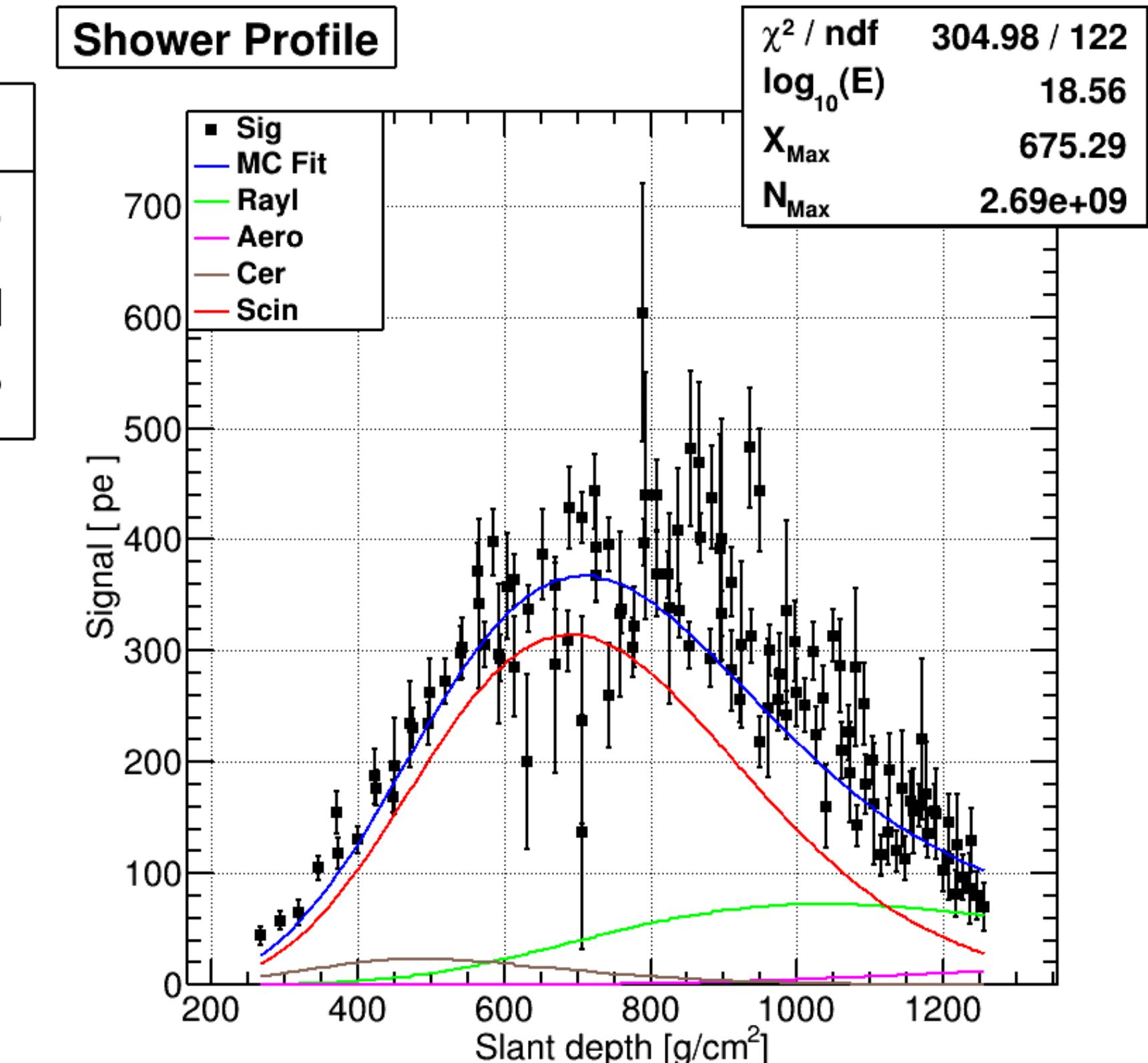
Event Display



Time vs. Angle Fit



Profile Fit



# DATA/MC COMPARISON (1/5) - GEOMETRY CHECK

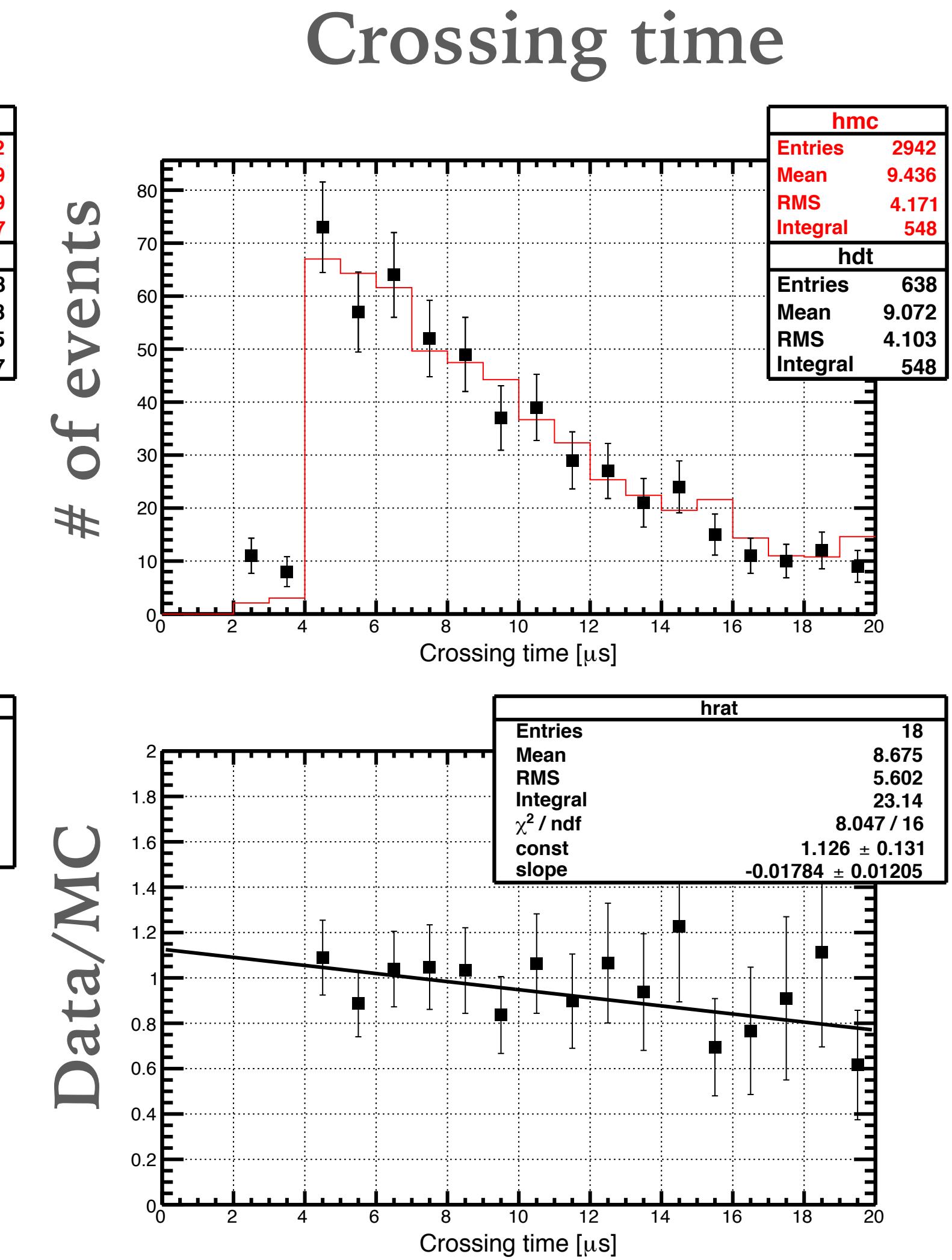
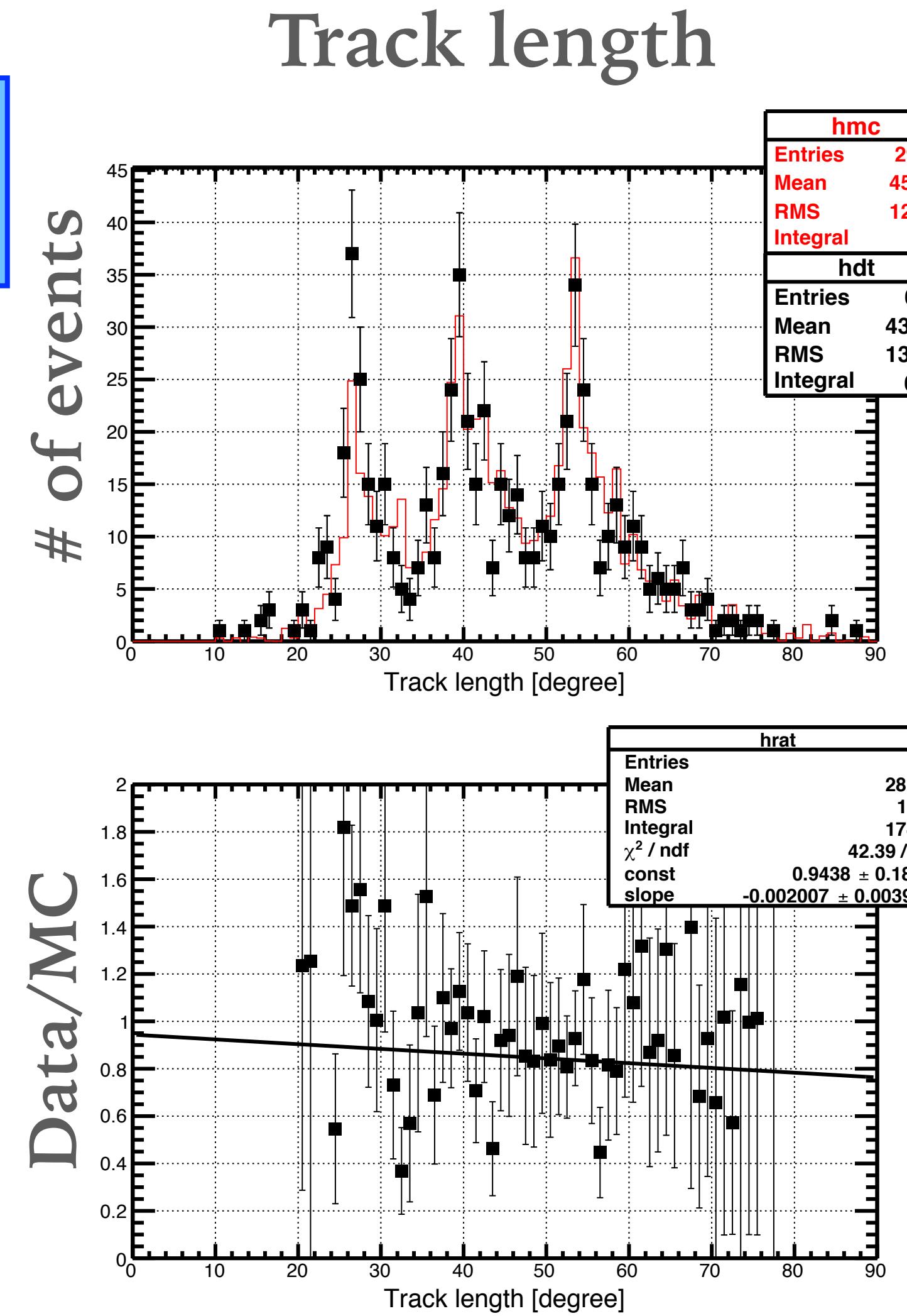
(Top) Data and MC distributions  
 (Bottom) Ratio of Data to MC

## ► Track length

Three peaks corresponding to 2,3, & 4 telescope events

## ► Crossing time

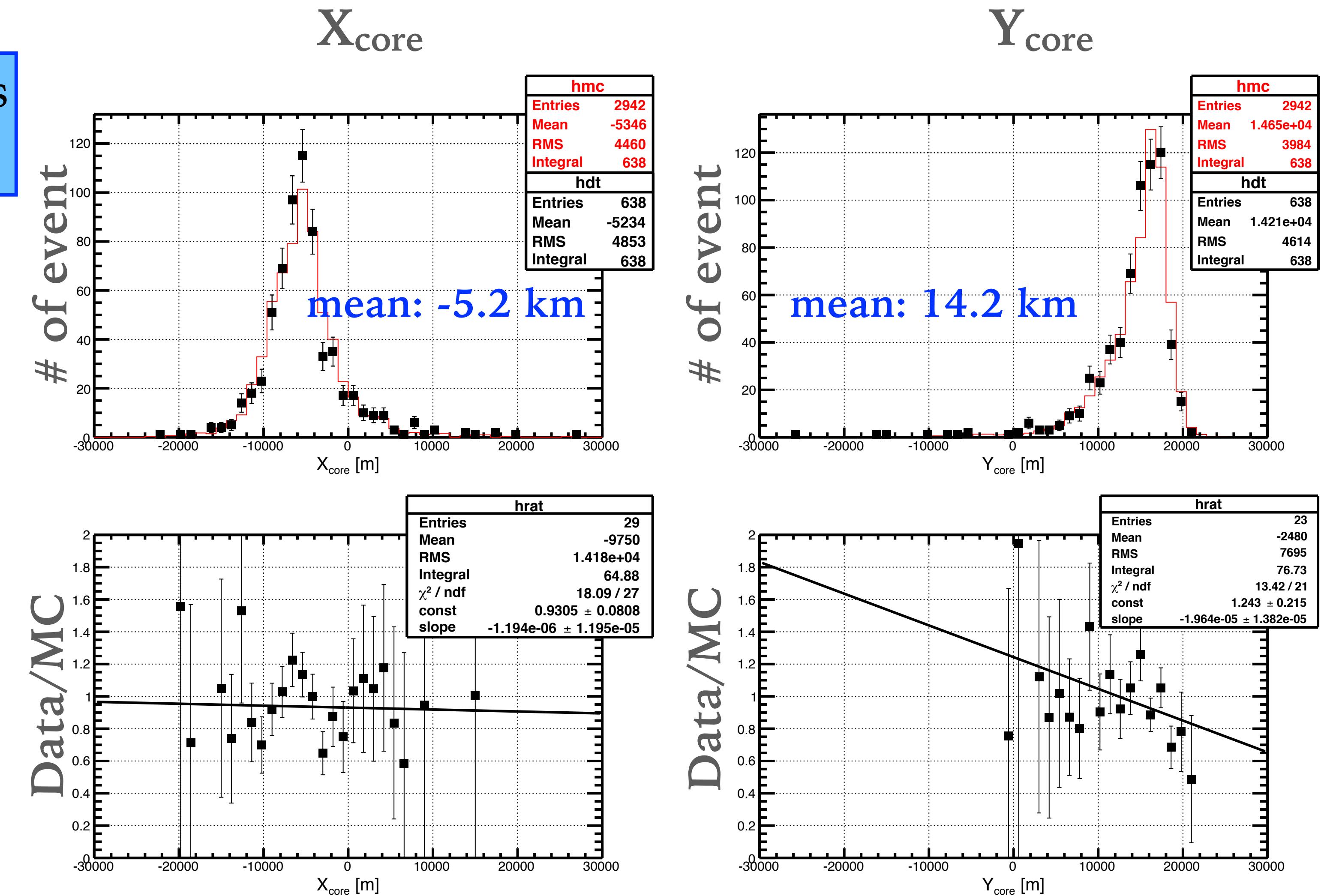
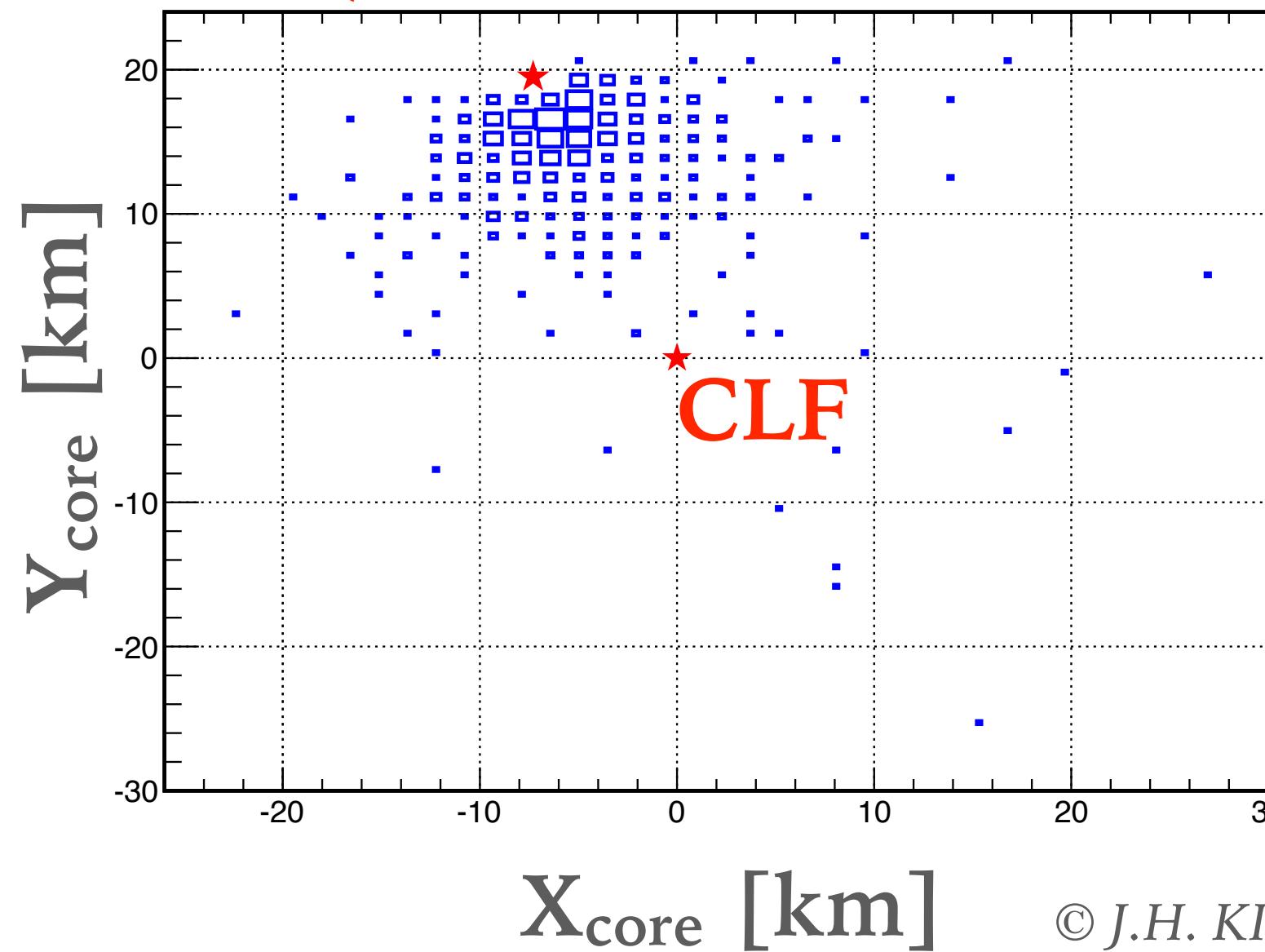
Time first to last tube triggered



# DATA/MC COMPARISON (2/5) - GEOMETRY CHECK

(Top) Data and MC distributions  
 (Bottom) Ratio of Data to MC

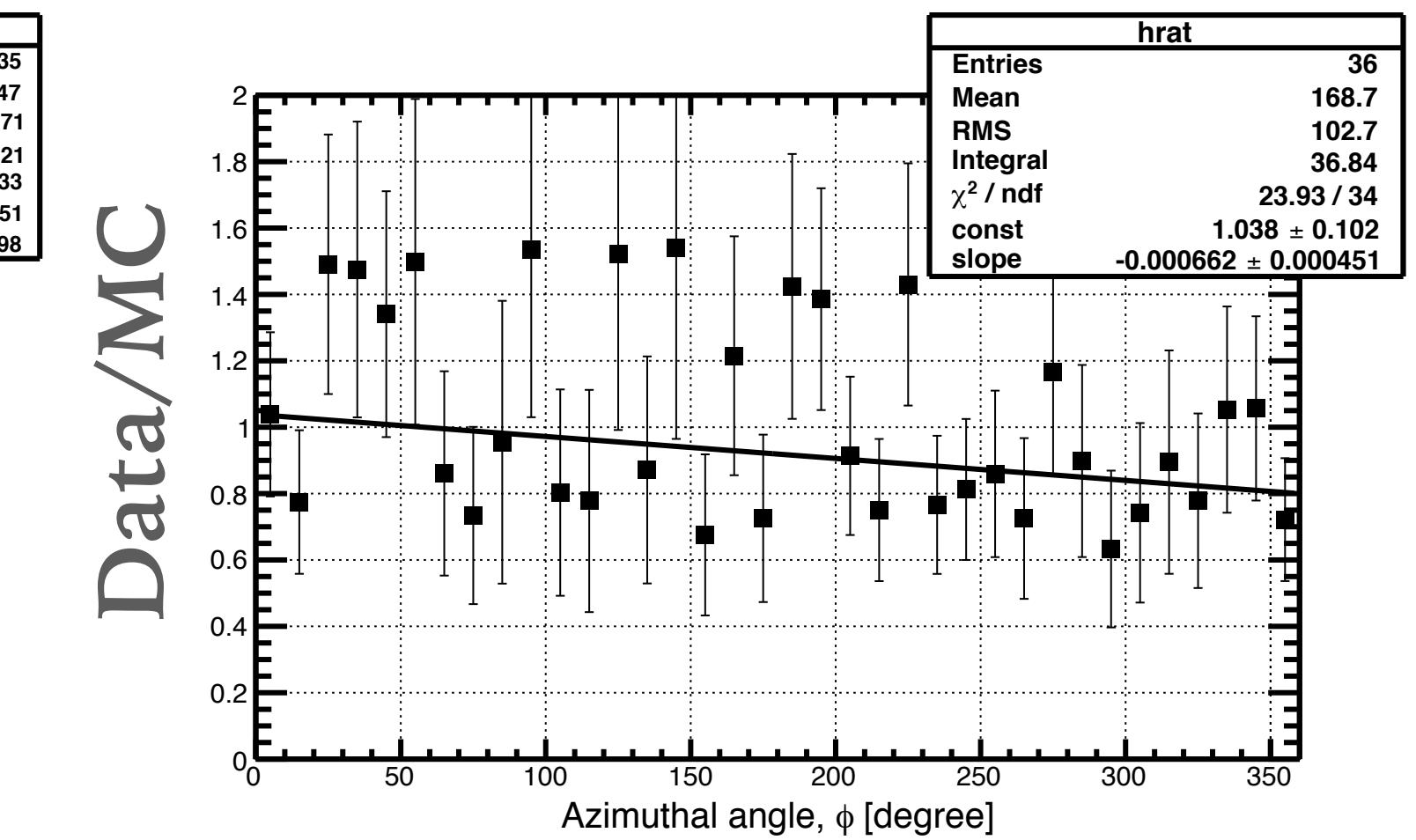
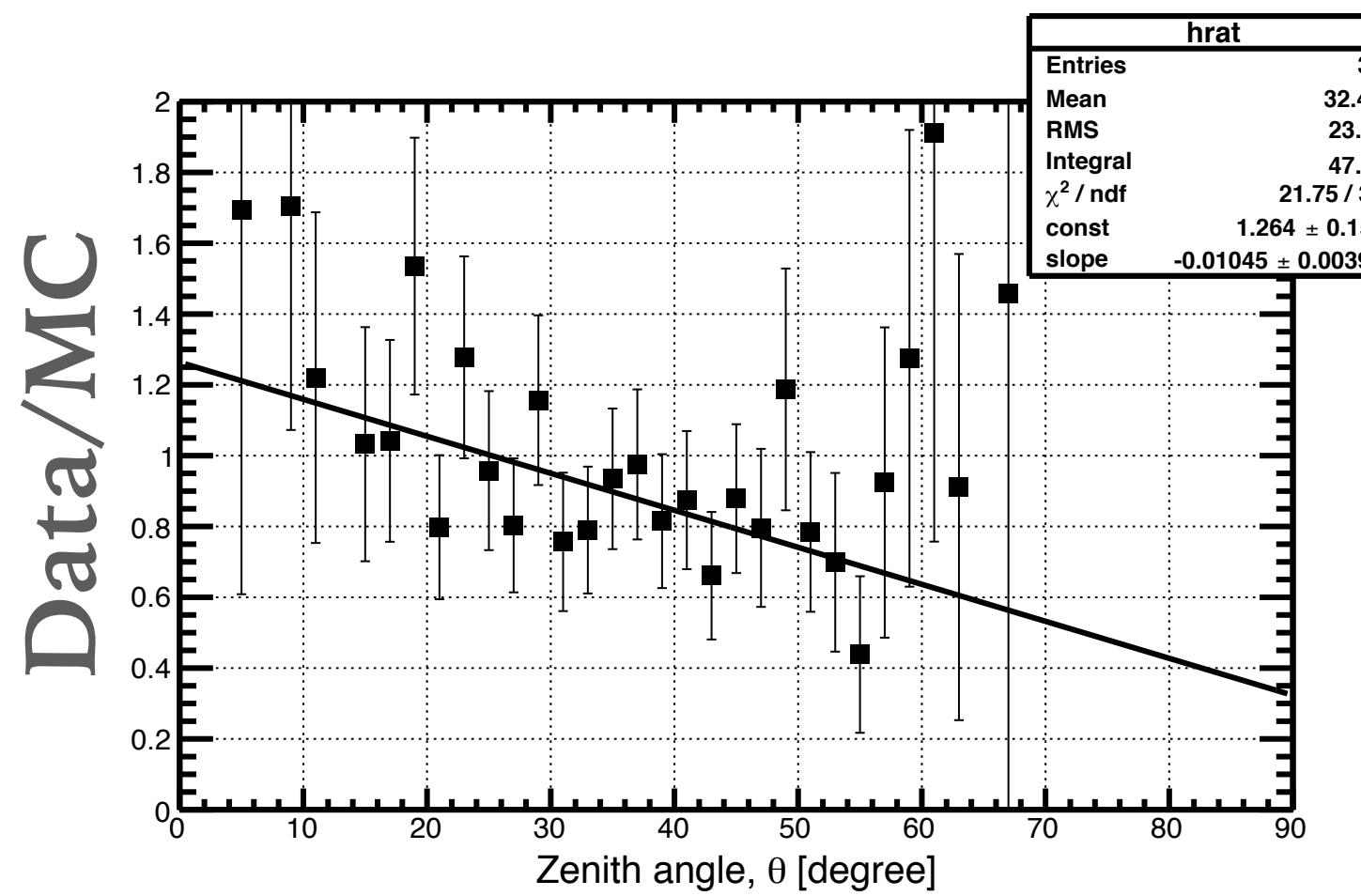
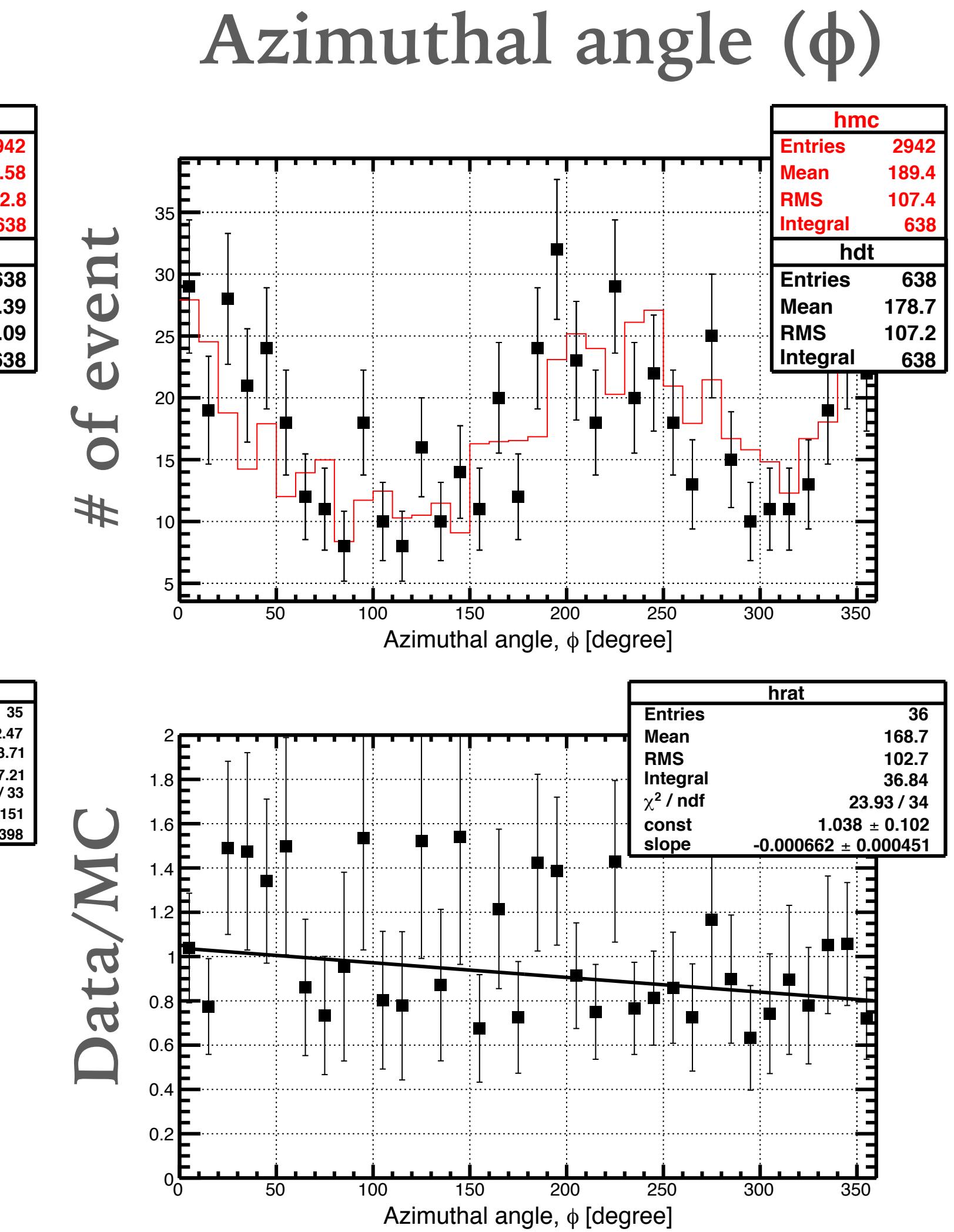
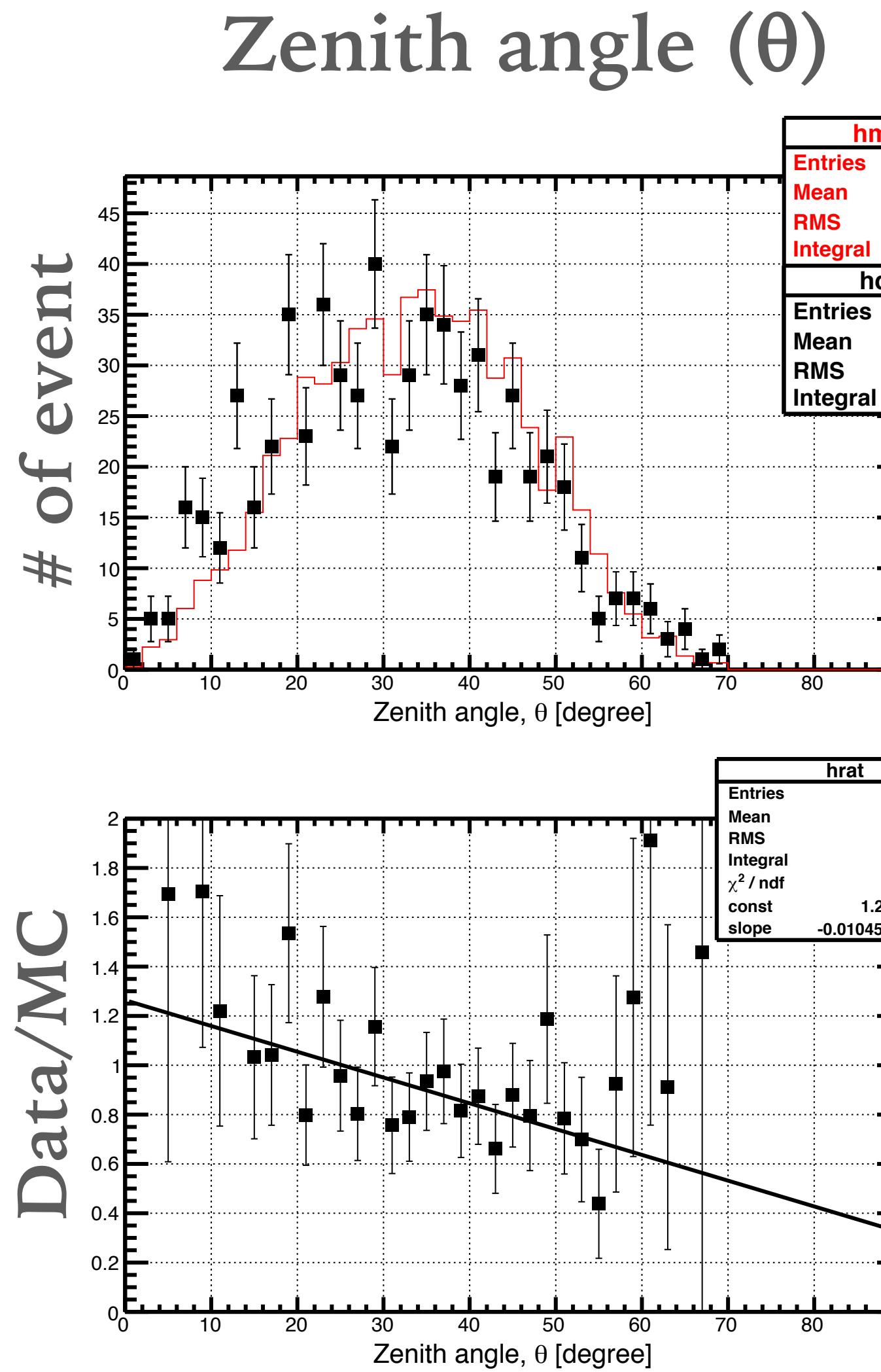
- Shower core position [km] in CLF coordinate
- MD/TALE**



# DATA/MC COMPARISON (3/5) - APERTURE CHECK

(Top) Data and MC distributions  
 (Bottom) Ratio of Data to MC

- Zenith angle  
Inclined of shower
- Azimuthal angle  
Degrees N of E



# DATA/MC COMPARISON (4/5) - APERTURE CHECK

(Top) Data and MC distributions  
 (Bottom) Ratio of Data to MC

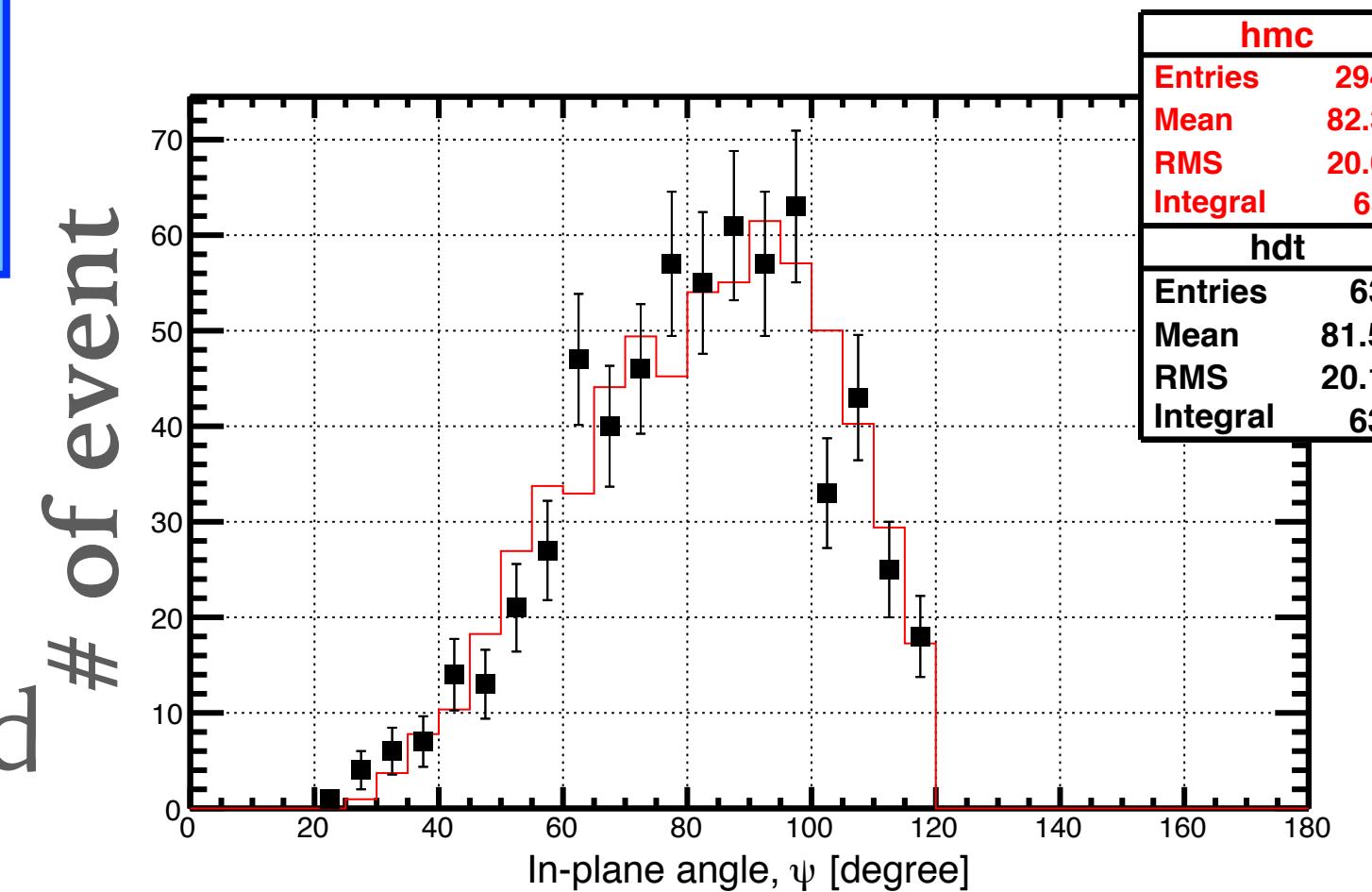
► In-plane angle

Going away or Coming toward

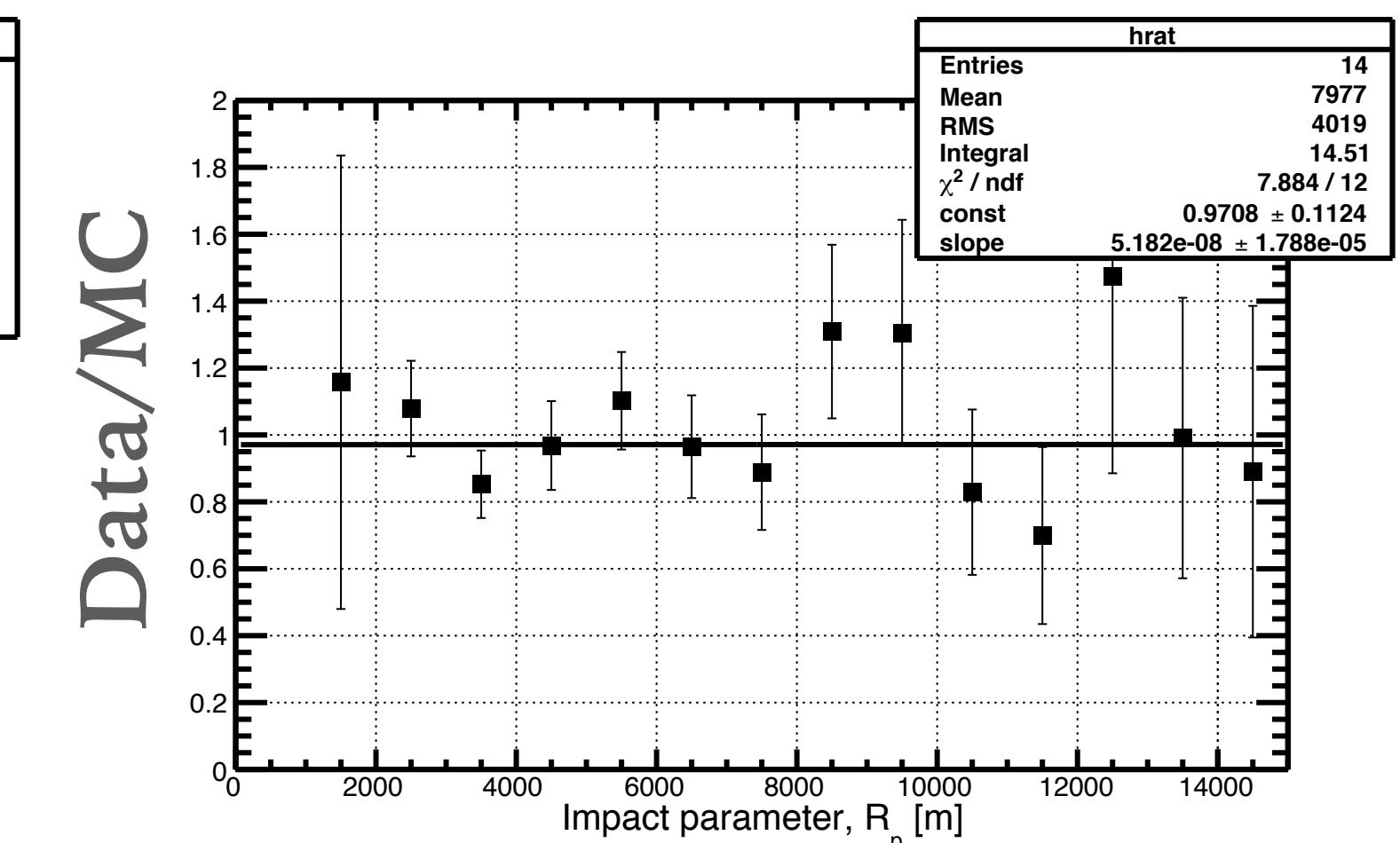
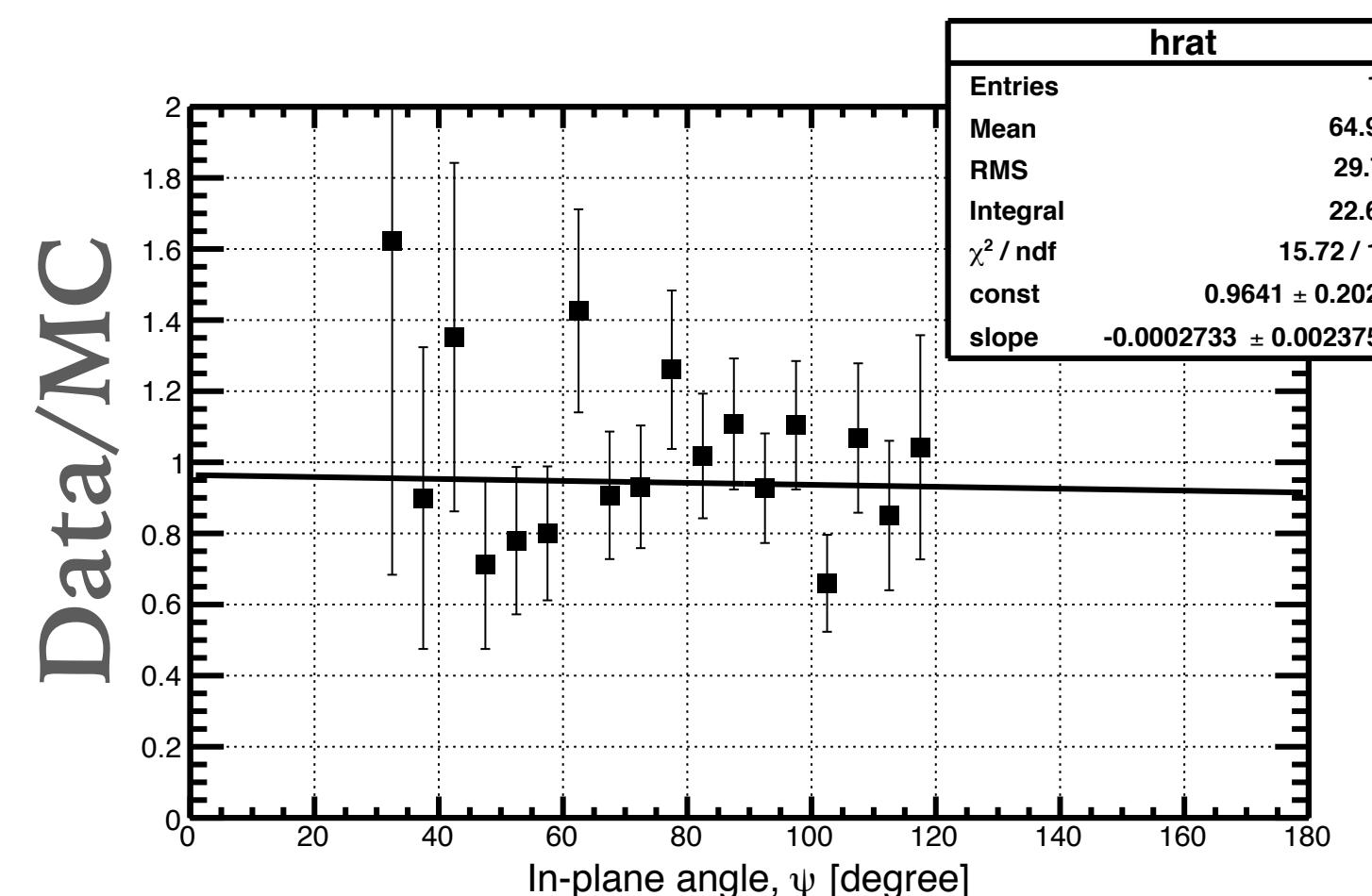
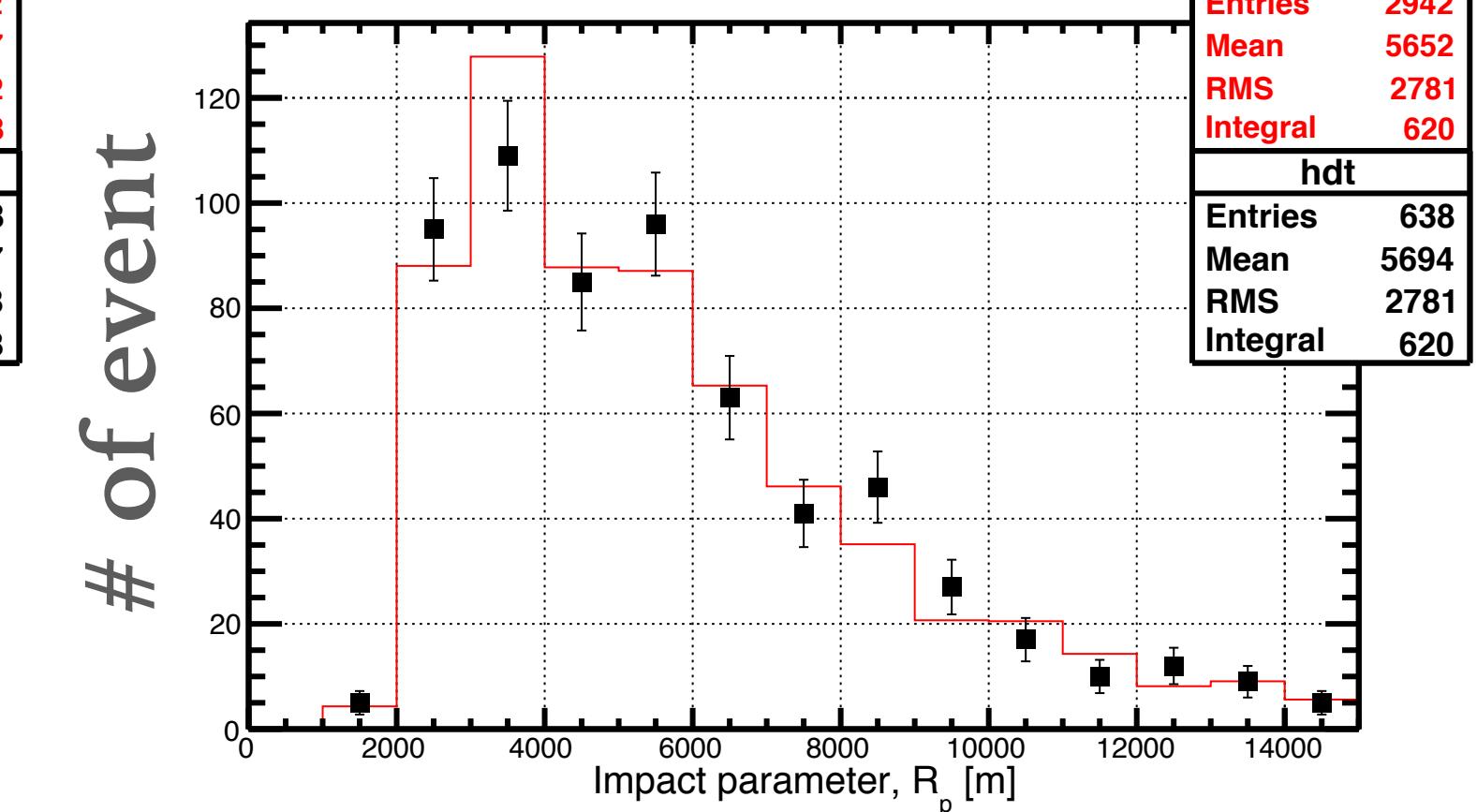
► Impact parameter

Distance at closest approach

In-plane angle ( $\Psi$ )



Impact parameter ( $R_p$ )

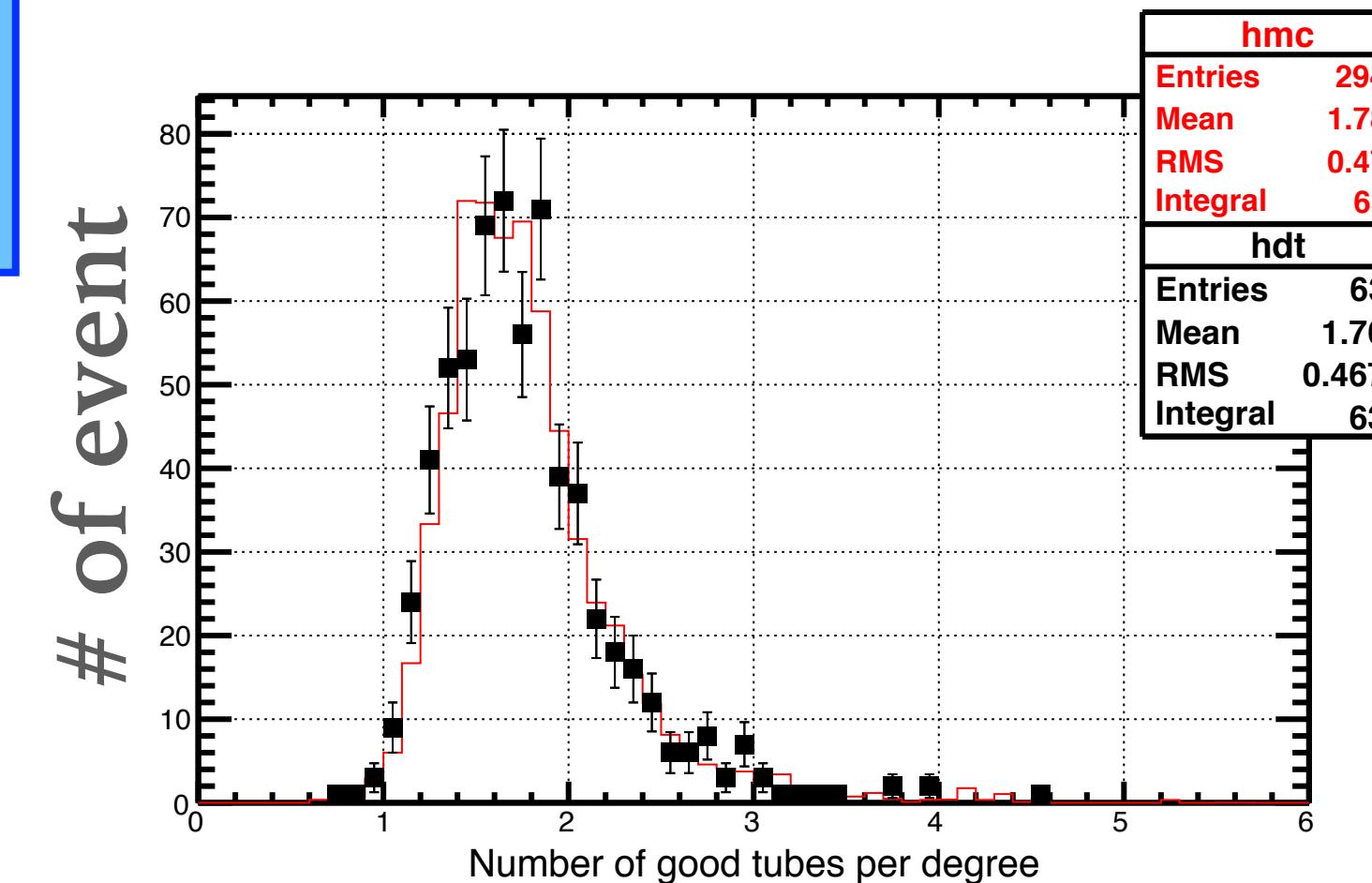


# DATA/MC COMPARISON (5/5) - SENSITIVITY CHECK

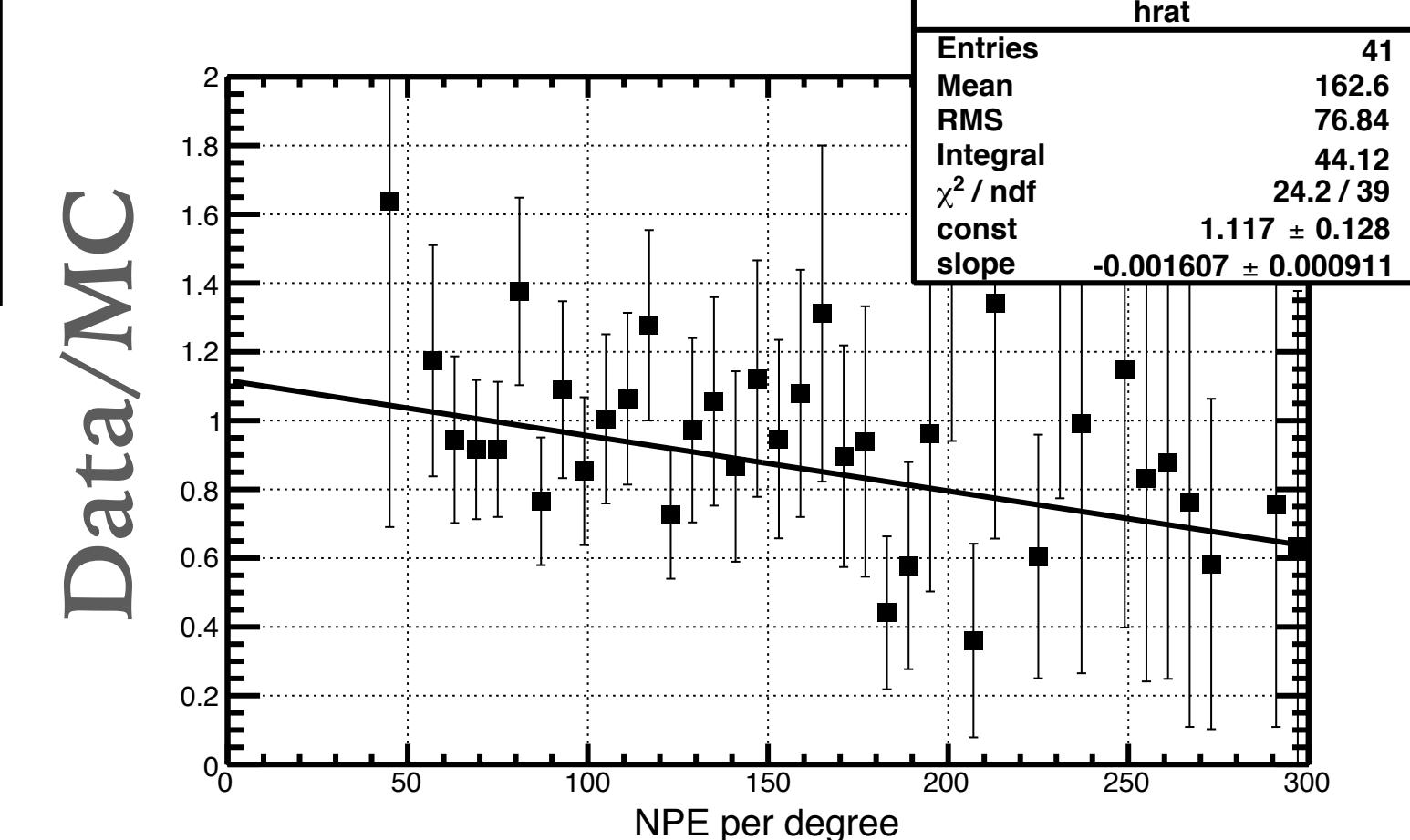
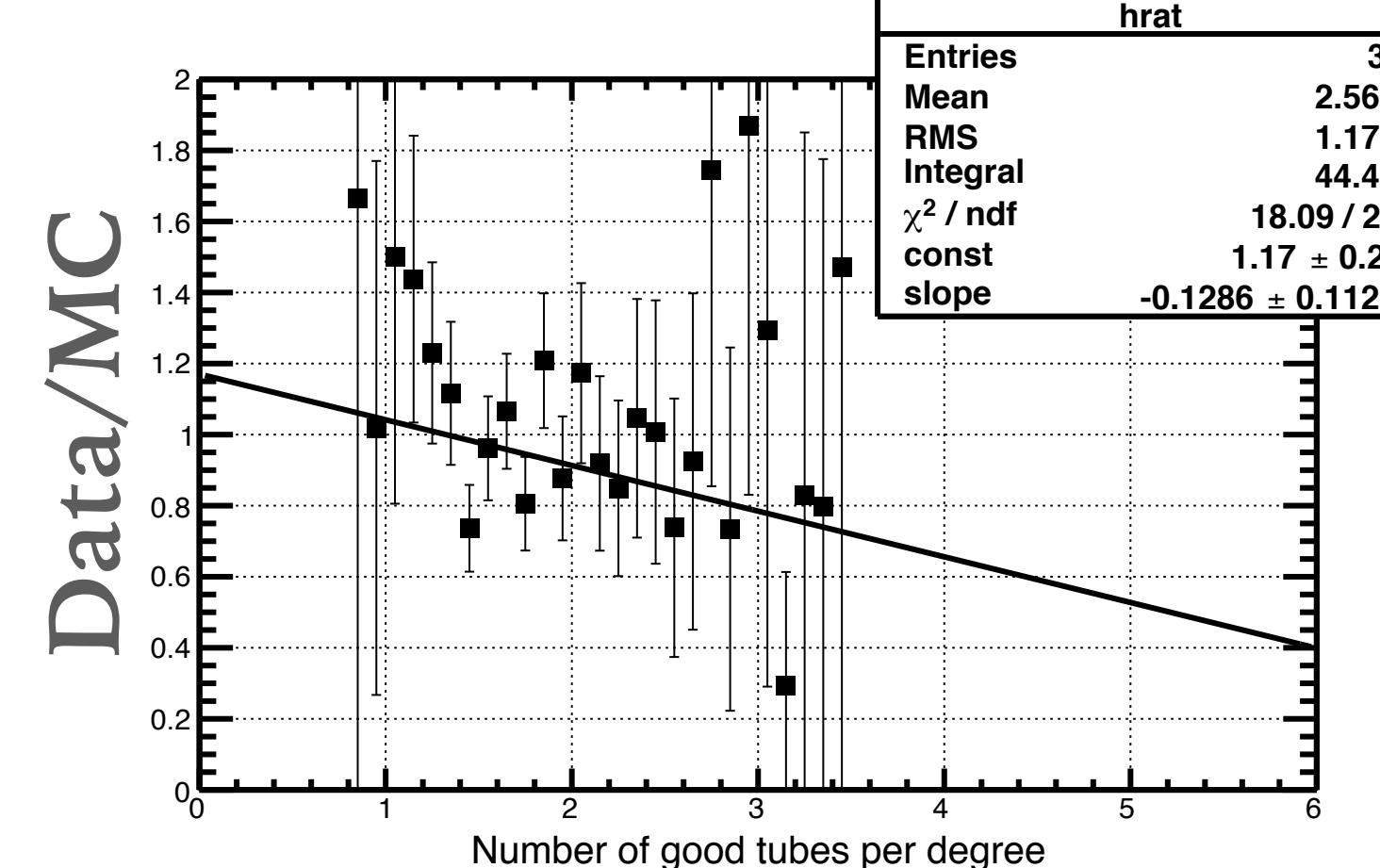
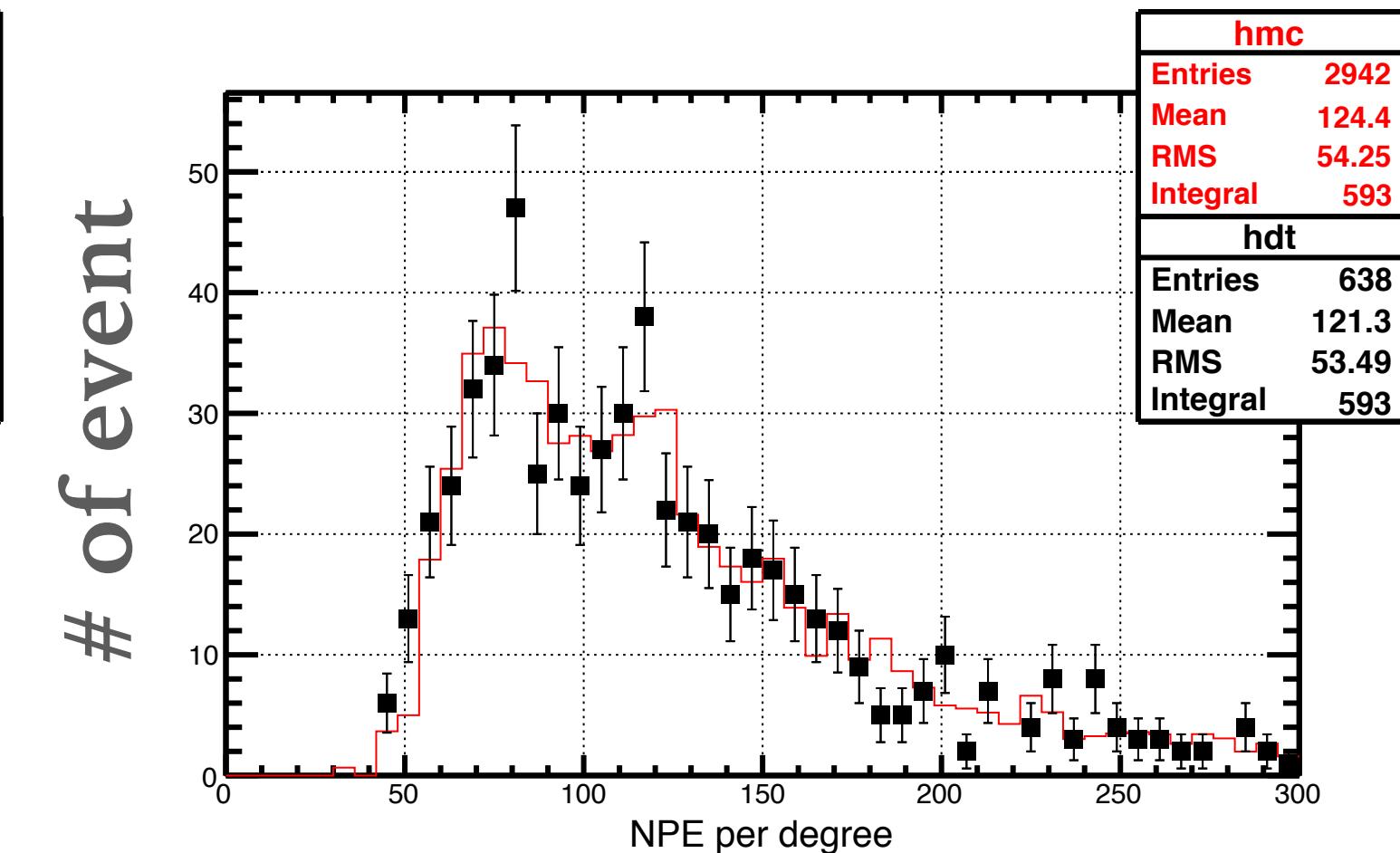
(Top) Data and MC distributions  
 (Bottom) Ratio of Data to MC

- # of good tubes per degree  
 how wide or how near
- NPE per degree  
 signal size per track

# of good tubes per degree



NPE per degree



# ENERGY SPECTRUM MEASUREMENT

- Energy spectrum

$$J(E_i) = \frac{N(E_i)}{A\Omega(E_i) \times T \times \Delta E_i}$$

$J(E_i)$  flux of cosmic rays

$N(E_i)$  # of observed cosmic rays

$A\Omega(E_i)$  energy dependent aperture

$T$  detector on-time

$E_i$  width of energy bin

- Data set:

- 1 June 2014 - 31 January 2015 (about 8 months; on-time 537 hrs)

- 1 June 2014 = start of stable operation

- 31 January 2015 = change in trigger (require different MC)

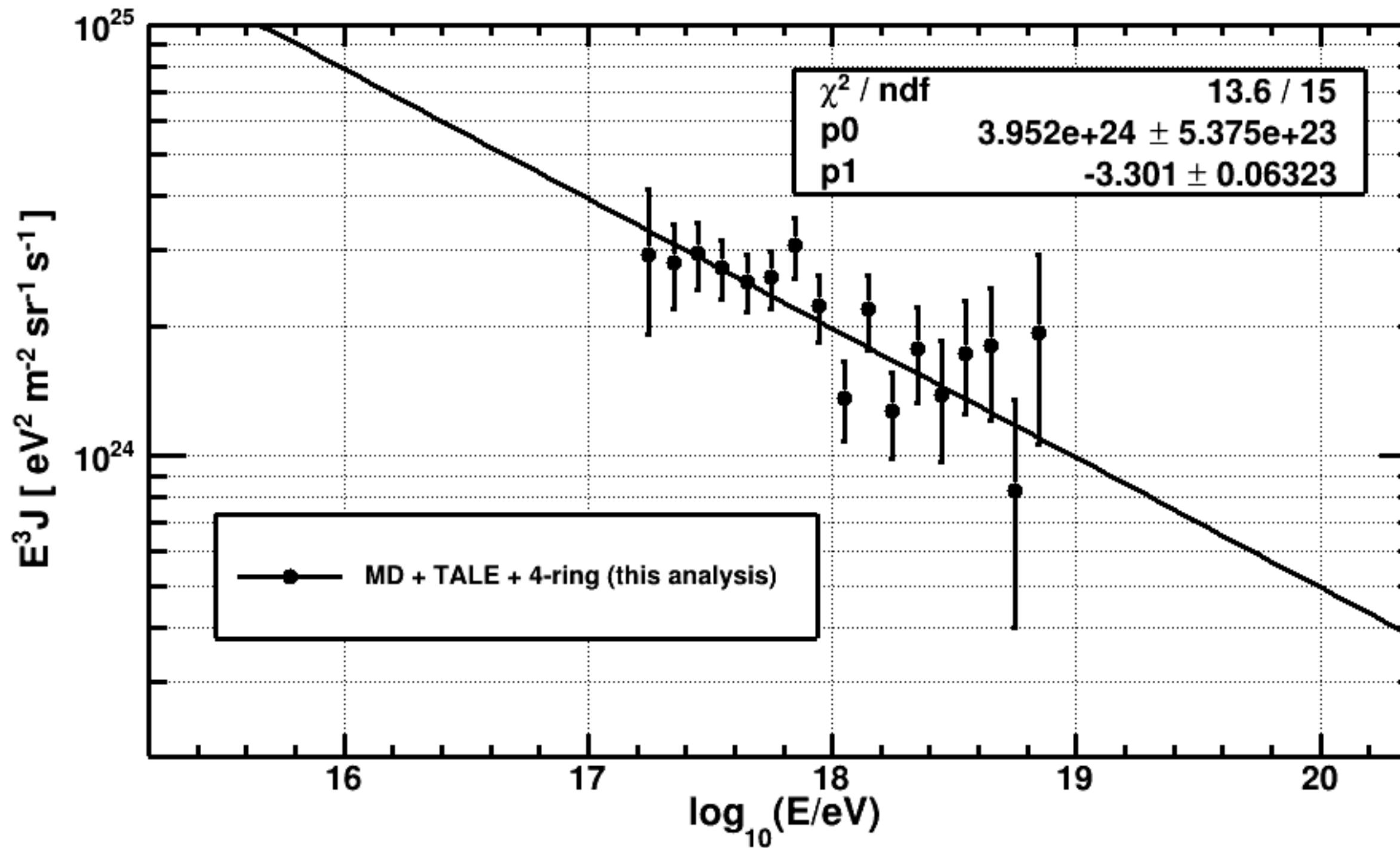
- Good weather 470 hrs

- 638 events after quality cuts

- Events seen by MD or TALE or both

# ENERGY SPECTRUM

- Middle Drum and TALE monocular energy spectrum
- Fit between 2nd knee and ankle to a power law:  
**-3.30±0.06 spectral index**



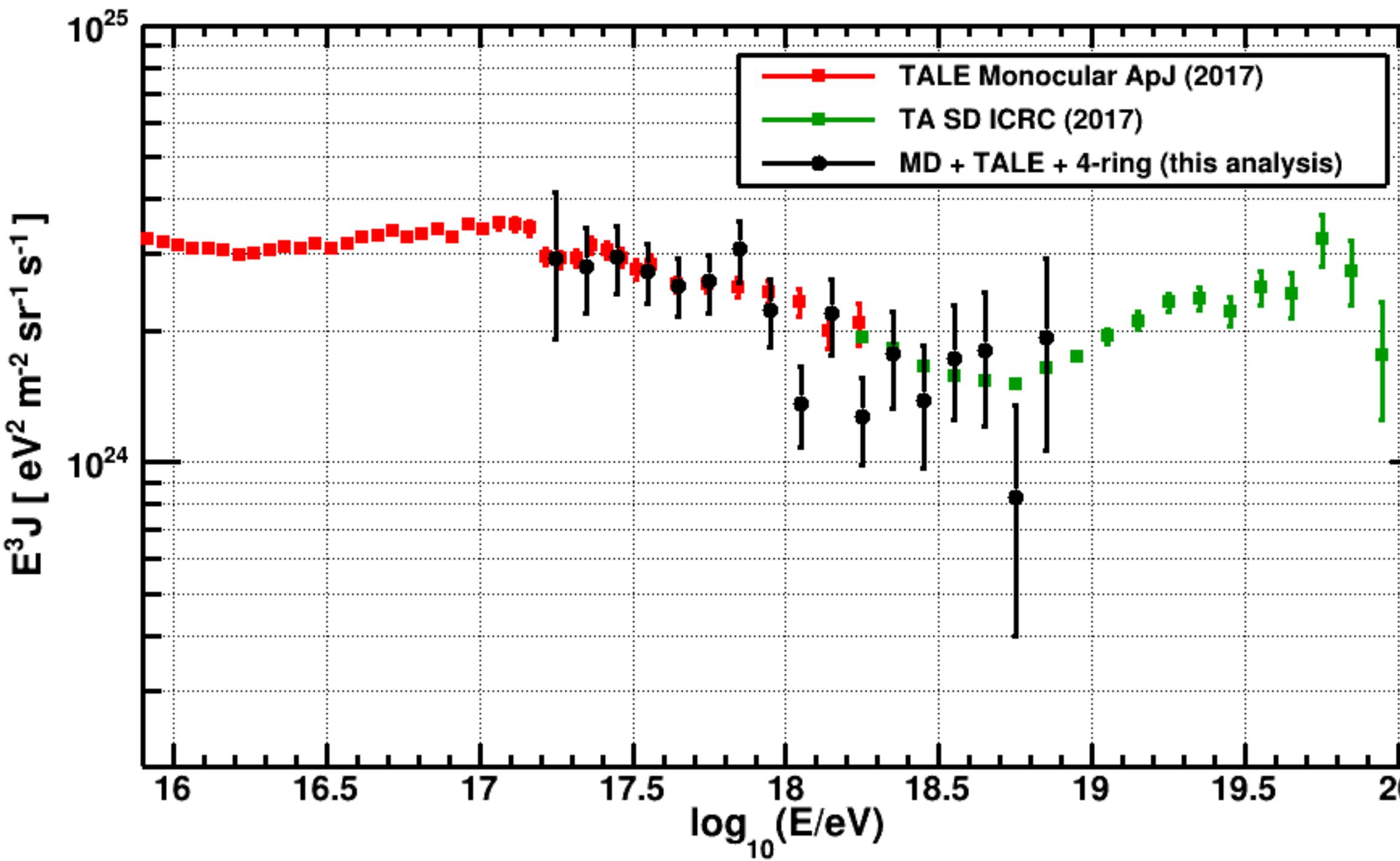
© J.H. KIM

Energy $\log_{10}(E/eV)$	Number of Events
17.25	12
17.35	33
17.45	52
17.55	67
17.65	72
17.75	71
17.85	70
17.95	53
18.05	33
18.15	43
18.25	28
18.35	26
18.45	17
18.55	20
18.65	15
18.75	5
18.85	8

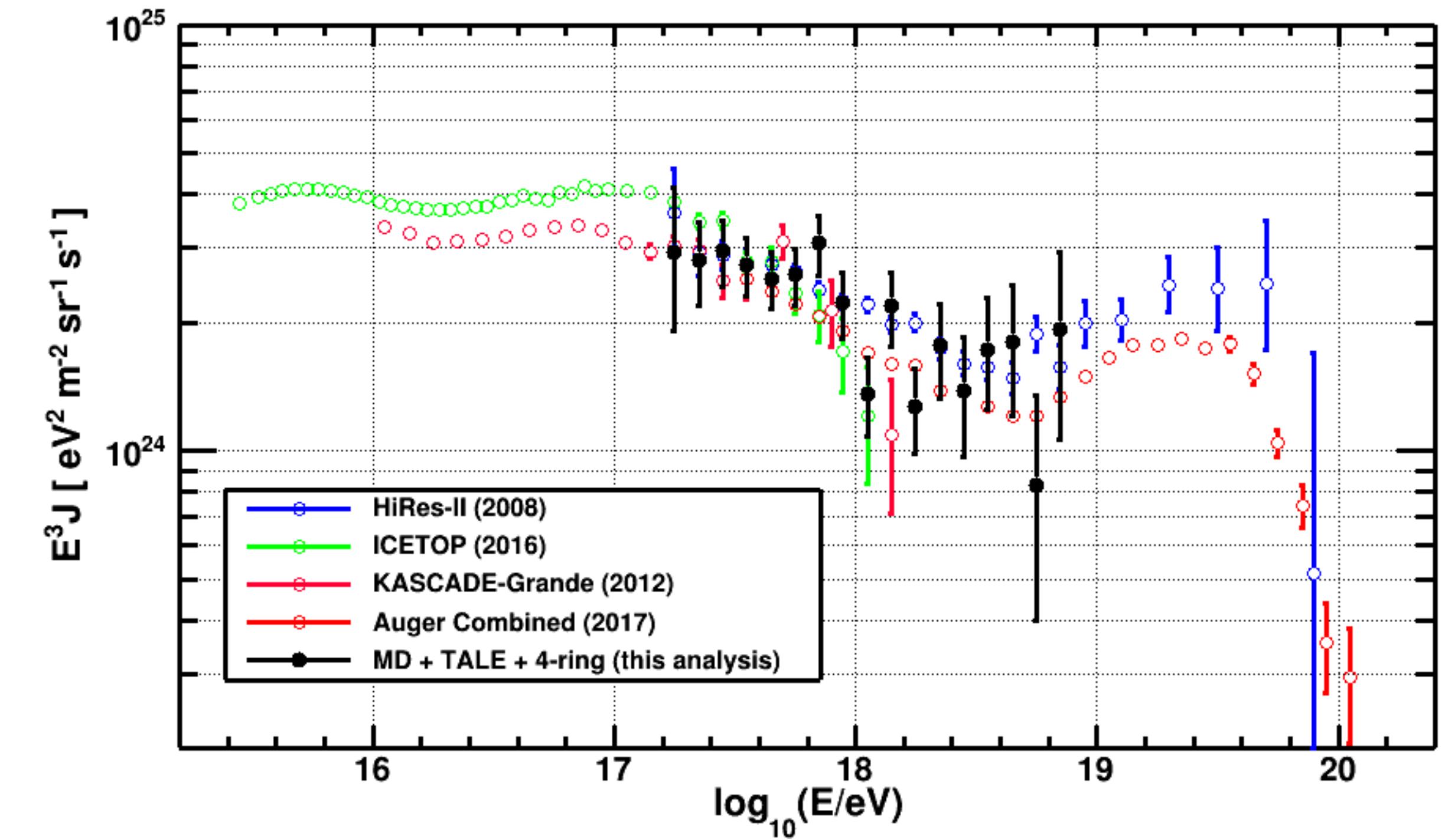
# ENERGY SPECTRUM

- (Left) A bridge between TALE only detector (Red) and Surface detector spectra (Green)
- (Right) HiRes-2 (Blue), IceTop (Green), KASCADE-Grande (Orange), and Auger (Red)

w/ other TA energy spectra



w/ other external energy spectra



# CONCLUSIONS (TAKE-HOME MESSAGE)

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- Monocular Cosmic Ray Energy spectrum Measurement
  - MD telescope - High Energy
  - TALE telescope - Low Energy
- Joint measurement of Cosmic rays using both MD and TALE telescopes
  - 4 ring analysis : optimal technique for this energy region
- Transition from heavy galactic to light extra galactic cosmic rays
- Spectral slope,  $-3.30 \pm 0.06$  in the energy range  $10^{17.2}$  to  $10^{19}$  eV
  - Spectral slope : good agreement with other TA techniques
- Good agreement with other measurements (HiRes, IceTop, KASCADE)

# ACKNOWLEDGEMENT

- Gordon Thomson
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- Dmitri Ivanov, Tareq AbuZayyad
- TA collaborators
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- More Friends: Lauren Simonsen, Sangita Baniya, Jessica Frew, Monica Allen, Jamie Zvirzdin, WomPA members
- Ganymede (Dog therapy while writing dissertation)



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©TA wiki



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# **BACK UP SLIDES**

# NEXT

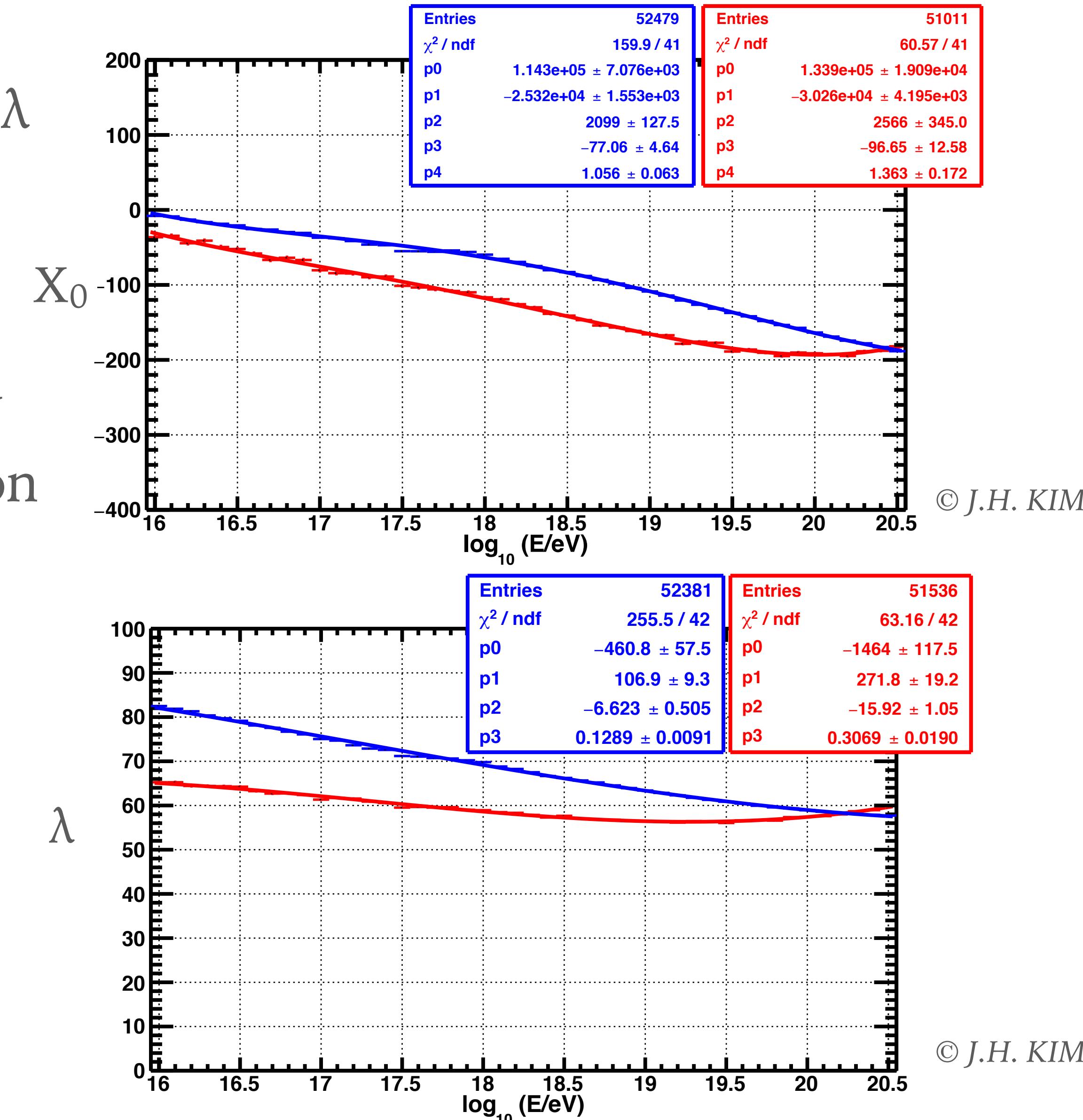
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- Data Set 3,  $\sim 5 \times$  statistics (change MC)
  - may gain 2-3 more data points at lower energy
  - may gain 2-3 more data points at higher energy
  - observation of ankle unlikely
- Extend to higher energy using MD

# EVENT RECONSTRUCTION - PROFILE FIT

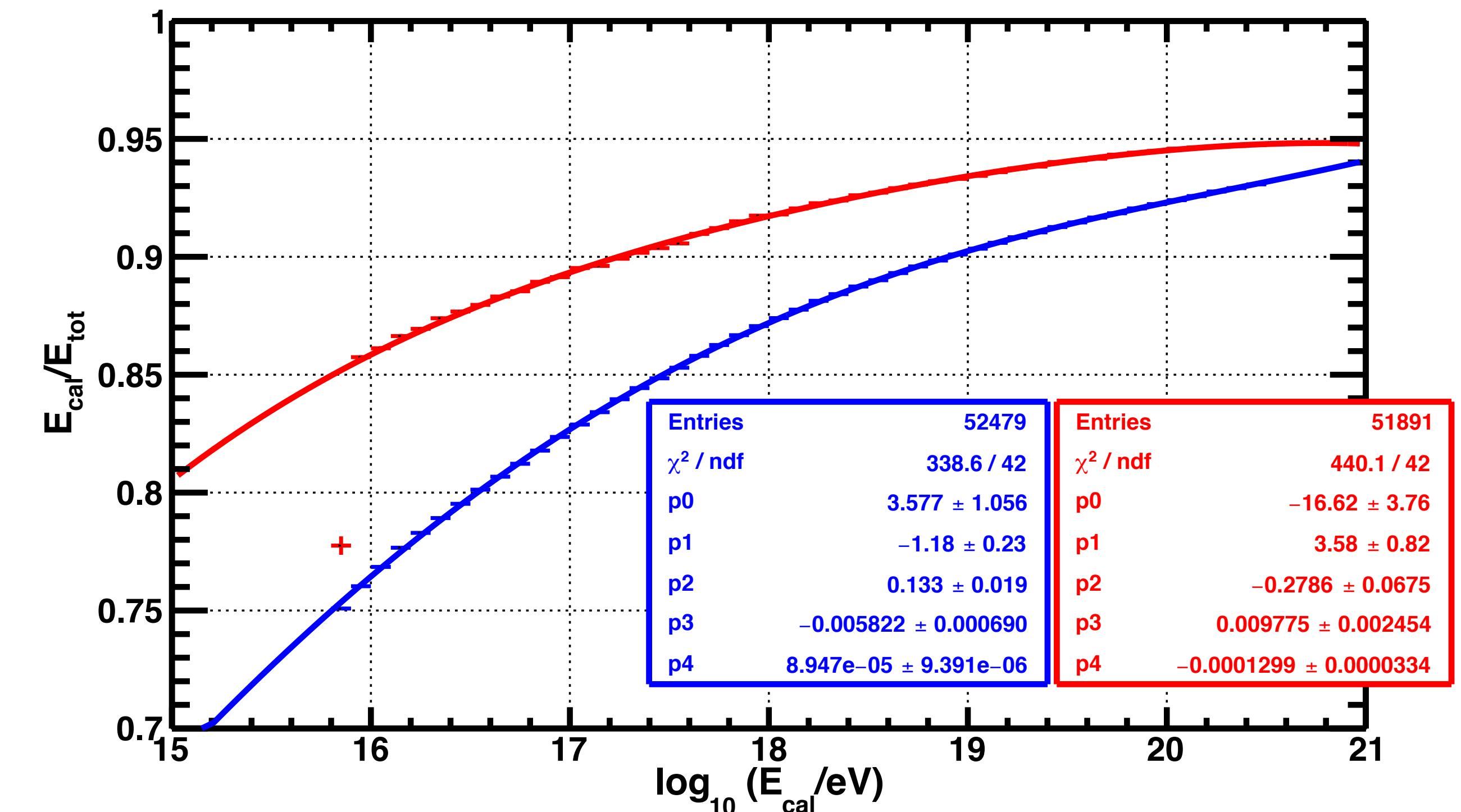
- Found I had an Energy bias when fixed  $X_0$  and  $\lambda$
- Generated look-up table of  $X_0$  and  $\lambda$  from p/Fe CORSIKA events
- Corrected for variation in  $X_0$  and  $\lambda$  with energy during analysis. Weighted based on composition as measured by the HiRes/MIA and HiRes experiments.

Red : Proton MC  
Blue : Iron MC



# EVENT RECONSTRUCTION - MISSING ENERGY CORRECTION

- Calorimetric/Visible energy by telescopes
- Energy carried by  $\mu$  and  $\nu$  missing
- As energy of primary cosmic rays (# of interactions) increases, the required missing energy correction decreases
- As # of interactions increases, energy transferred to electromagnetic/visible component



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Red : Proton MC

Blue : Iron MC

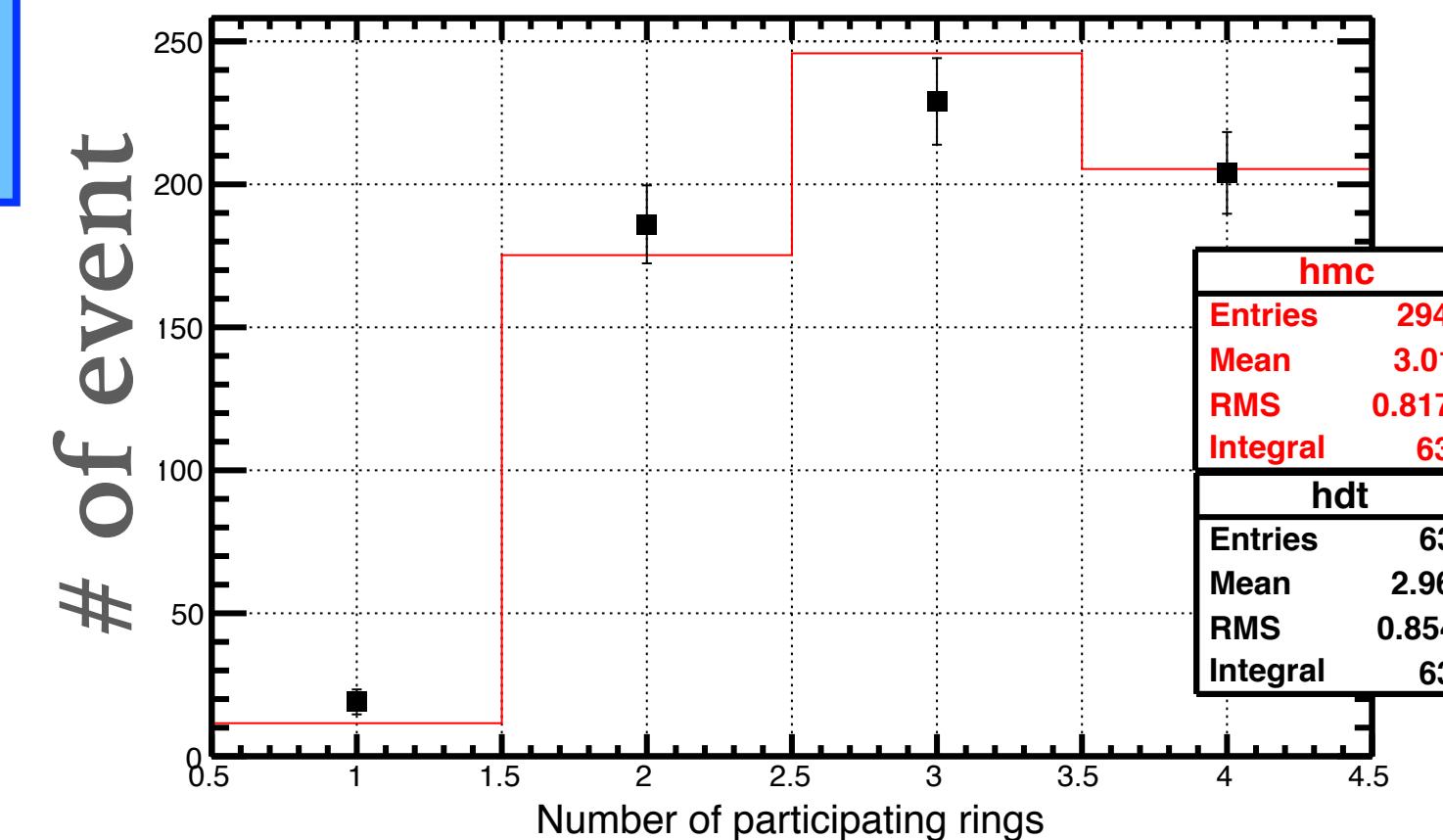
# DATA/MC COMPARISON

(Top) Data and MC distributions  
 (Bottom) Ratio of Data to MC

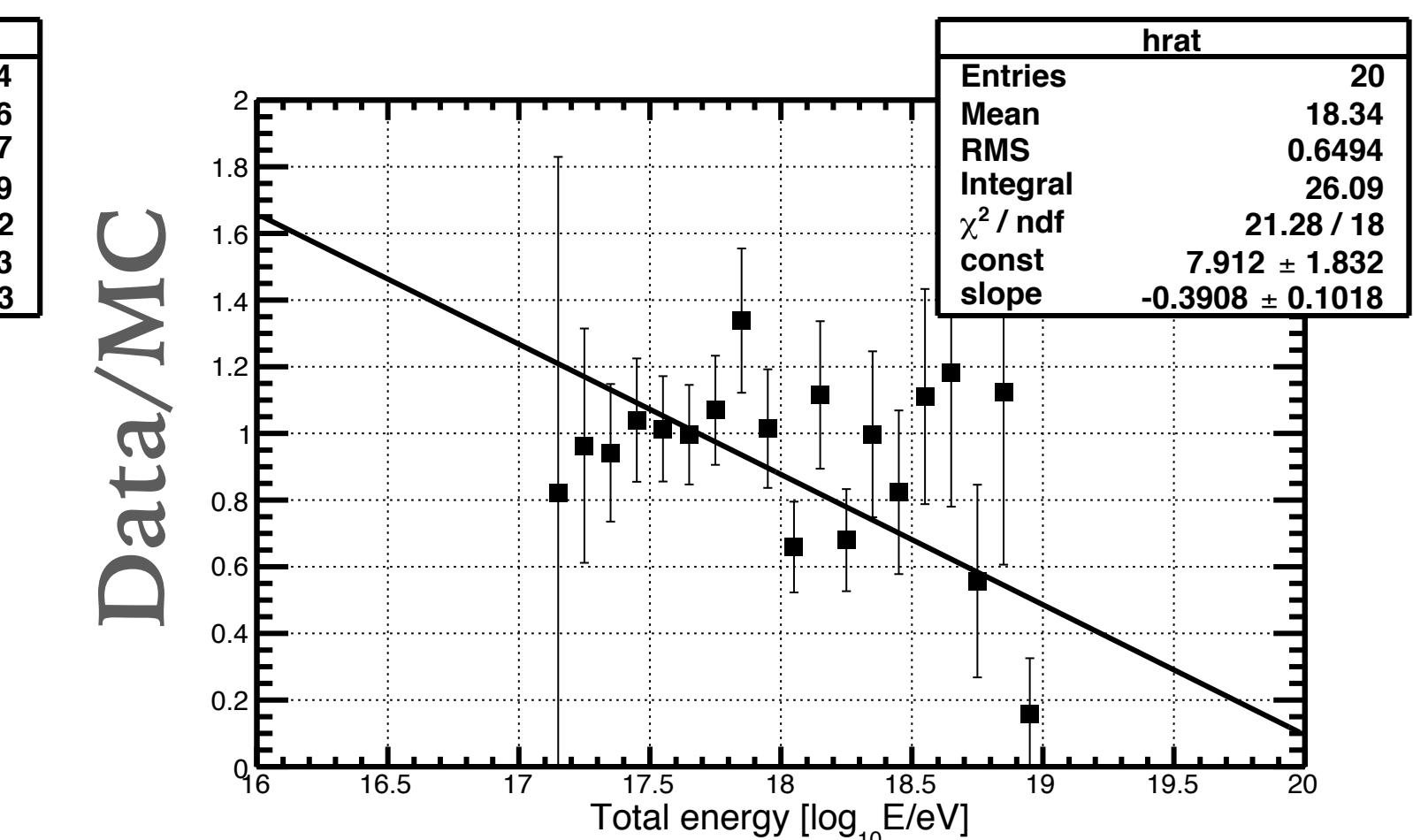
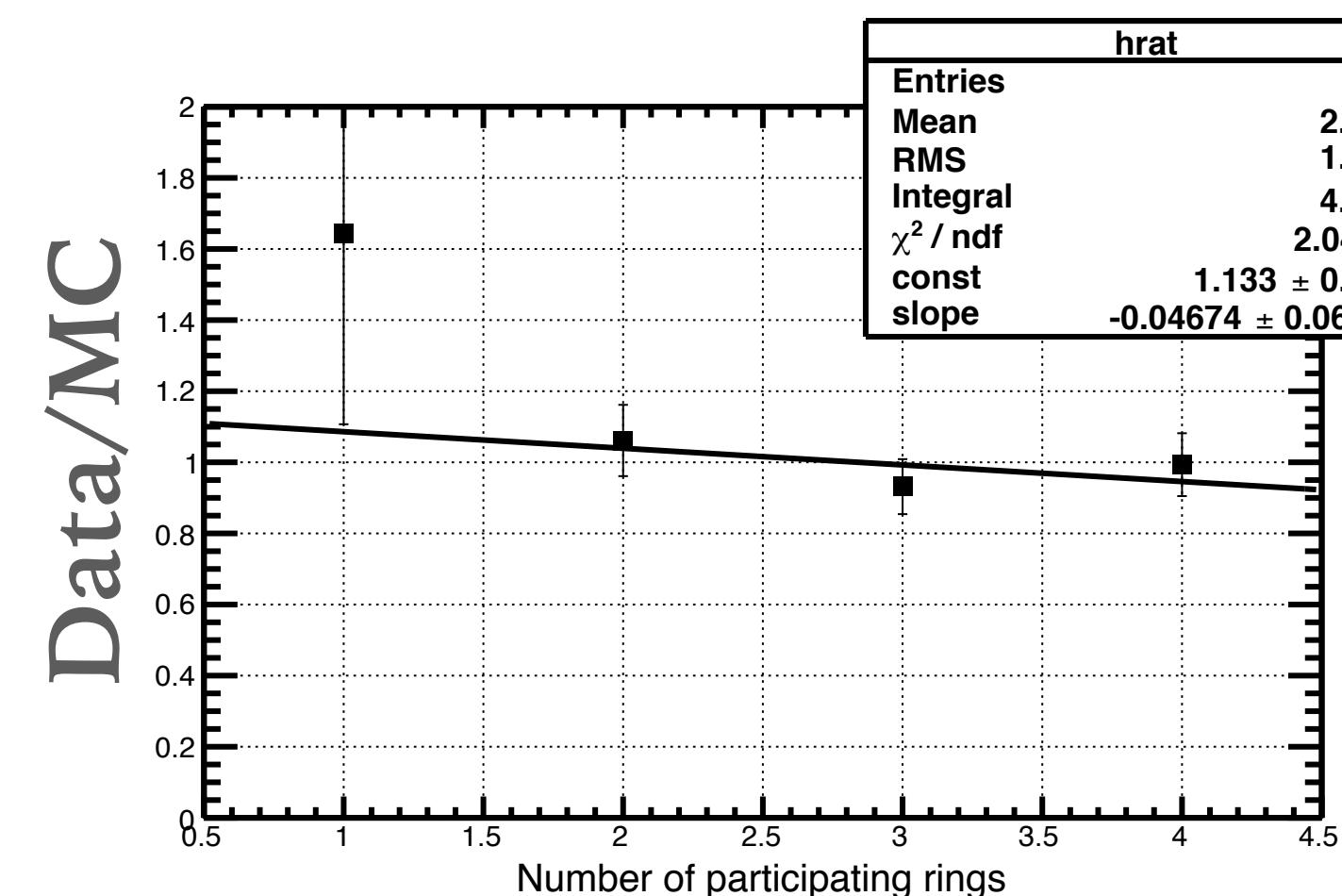
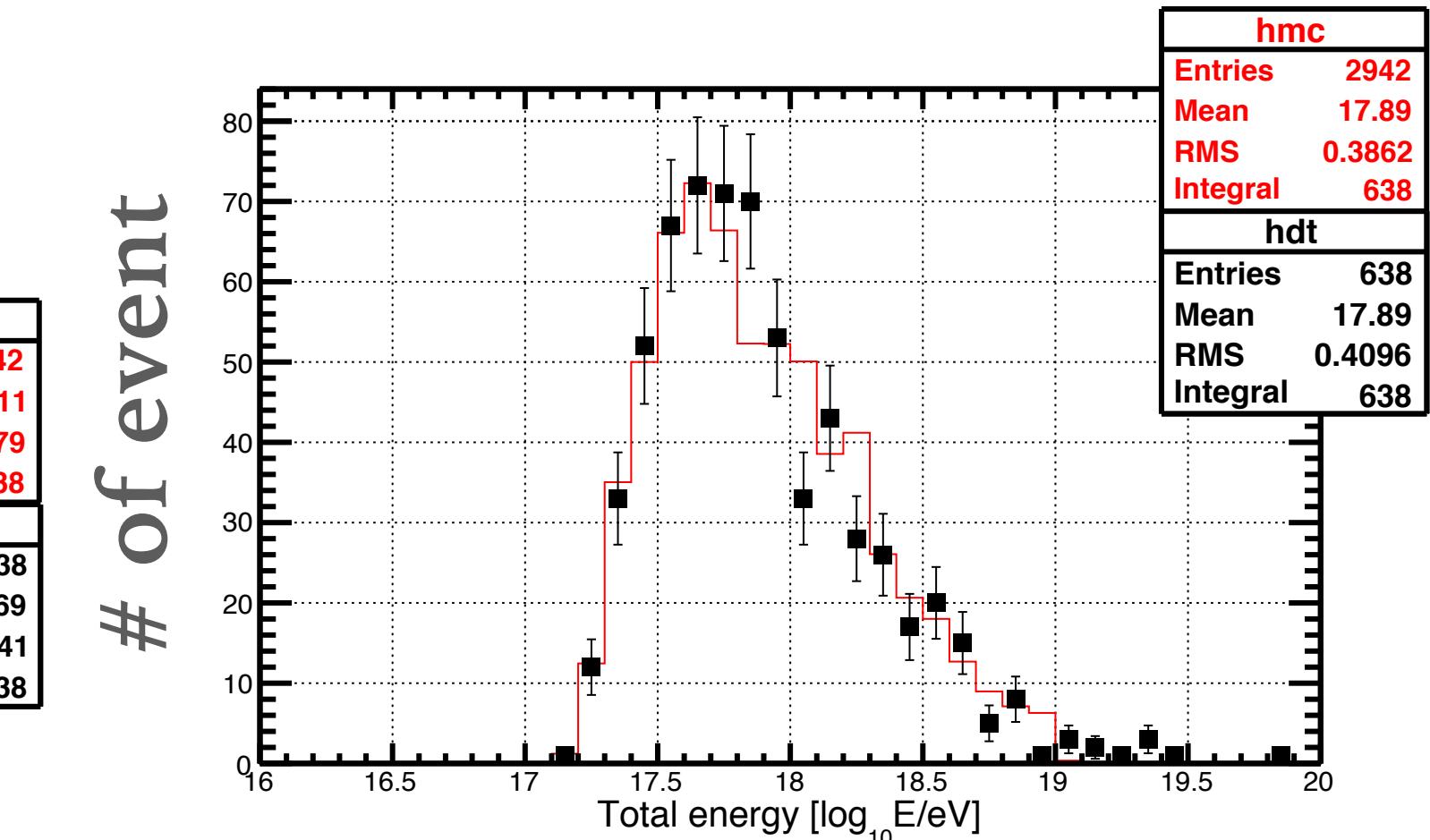
- # of participating rings  
 1, 2, 3, and 4-ring

- Total energy  
 Missing energy corrected

## # of participating rings



## Total energy



# DATA/MC COMPARISON

(Top) Data and MC distributions  
 (Bottom) Ratio of Data to MC

► SDP angle

Dip structure around  $0^\circ$

Related to insensitivity in the trigger

## Shower Detector Plane angle

